Effective activation energy and phase diagram
in the Er-doping MTG-YBa$_2$Cu$_3$O$_{7-\delta}$ crystal

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Abstract

The resistivity of melted textured growth (MTG) Y$_{0.8}$Er$_{0.2}$Ba$_2$Cu$_3$O$_{7-\delta}$ (YErBCO) crystal has been measured as a function of temperature $T$, applied magnetic field $H$ and the angle $\theta$ between the applied magnetic field and $ab$-plane. Based on the Yeshurun–Malozemoff model [Phys. Rev. Lett. 60 (1988) 2202], we investigated the vortex dynamic behavior from the Arrhenius form $\rho(T,H) = \rho_0 \exp(-U_0/T)$ and found that the model can explain the dissipation in the vortex liquid state for the Er-doped YBa$_2$Cu$_3$O$_{7-\delta}$ (YBCO) crystal. The effective activation energies for $H\|c$ in the Er-doped MTG-YBCO are about 2.7 x 10$^3$ K (7.5 T) and 5.6 x 10$^4$ K (0.5 T) less than that for $H\|c$ in pure YBCO. The anisotropy factor $c = 10$ obtained from the angular dependencies of effective activation energy $U(\theta)$ and the zero resistance temperature $T_c(\theta)$ for Er-doped YBCO crystal are larger those that for YBCO crystal. The field dependence of the effective activation energy $U_c$ follows a power law, $U_c \propto H^{-a}$, with $a = 1.0$ for $H\|c$ and for various angles $\theta$ at a fixed magnetic field of 4 T. The phase diagram of the Er-doped YBCO crystal is presented and discussed.

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1. Introduction

The mixed-state flux dynamics in high-$T_c$ superconductors (HTSCs) is an attractive and complex subject. Much attention has been paid to the relationship between the dissipative flux motion and the flux pinning mechanism, but still many issues are to be resolved [1]. Since there exists much shorter coherence length $\xi$ and much higher thermal energy $k_B T$ near the superconducting transition in the HTSCs than that in the conventional superconductors, the thermally activated flux motion plays an important role during the onset of the finite resistance. The lower order-of-magnitude $U_0$, coupled with the higher $T_c$s lead to the observed “giant flux creep” [2]. For example, the typical value of $k_B T_c/U_0$ is of order 10$^{-3}$ in conventional low-temperature superconductors, while of order 0.05 in YBa$_2$Cu$_3$O$_{7-\delta}$ (YBCO) [2]. So the effective activation energy $U_c$, which measures the depth of the activation energy well, is an
indispensable parameter for interpretation of the thermally activated motion behaviors in the mixed state.

The doped samples of rare earth elements (Nd, Sm, Eu, Gd, etc.) [3–5] have been intensively studied due to their greater radius of the atoms than Y, which bring about the stronger pinning strength. While Er-doping polycrystalline samples have been studied from the ESR and SLR techniques [6–8], and it is found that there exist the peculiarities of magnetic interactions between Er3+-ions and Cu2+-spin system on copper-oxide plane [8]. However, the transport property of the textured Er-doped YBCO crystal has rarely performed, so it should be considered for further research. And it is well known that the Yeshurun–Malozemoff model [2] is proved to be suited for the thermally activated flux creep behaviors in typical 2D Bi-2212 [9] and transitional Hg-1223 [10]; while in the case of YBCO [10] with a lower anisotropy ratio, it’s found that Tinkham’s form [11] was valid. In this paper, we measured the resistivity of melted textured growth (MTG)-Y0.8Er0.2Ba2Cu3-O7–δ (YErBCO) crystal as a function of temperature, magnetic field and the angle θ between the applied magnetic field and ab-plane and analysis the effective activation energy by Y–M model. The result shows that there is a larger TAFF region in the sample. The effect of Er-doping on the flux pinning is discussed in the text.

2. Sample and experimental

The Er-doped YBCO (YErBCO + 40 mol% Y2BaCuO(211)) crystal used in this study was prepared by the MTG method. The premeditated powders were ground sufficiently to ensure the uniformity of composition, and then calcined at 900 °C for 24 h. The sintered powder was ground again, then pressed into pellets and sintered at 920 °C for 24 h. The same process like the second times has been done for the third times. The pellets were heated to 1050 °C from room temperature at the rate of 200 °C/h and kept for 1 h, then quickly cooled to 1010 °C, followed by a slow cooling to 950 °C at the rate 2 °C/h and later a quick cooling to 600 °C at 50 °C/h, then a furnace-cooling to room temperature. The samples cleaved from the MTG-YErBCO bulk with a single domain were oxygenated at 400 °C in flowing oxygen gas at 1 atm for more than 50 h for the uniformity of oxygen. A platelet with the size of 8.7 × 4.7 × 0.5 mm3 cut from a larger crystal was held on a rotatable sample holder, where the angle between the applied magnetic field H and the surface of the film could be adjusted conveniently and the resolution of the angle was 0.1°. The resistance was performed by standard four-probe technique using the method of plus and minus current. A programmable Keithley 220 current supplier was used as the current source. A Keithley 182 nanovoltmeter was used to detect the voltage signal with a resolution of 2 nV. The magnetic field up to 8 T was supplied by superconducting solenoid magnet system. The temperature was measured by a calibrated Rh–Fe resistance thermometer and corrected for the effect of magnetic field. The zero resistance temperature of the sample is 87.7 K, and the magnetic critical current density Jc is 2.4 × 10⁴ A/cm² at 77.3 K in zero magnetic field. The X-ray data, microstructure and magnetization of the sample have been reported elsewhere [12].

3. Results and discussion

3.1. Effective activation energy U_{eff} in TAFF region

Fig. 1 shows the temperature dependence of the resistivity at the magnetic field parallel to the c-axis up to 7.5 T. The broadening of the resistive transition with the increasing of applied magnetic field is observed obviously. The Arrhenius plots of ρ(T, H) for external magnetic fields from 0.5 to 7.5 T as a function of inverted temperature 1/T is shown in the inset of Fig. 1. From the inset of Fig. 1, we can clearly see that the slope d(ln ρ)/d(1/T) of the Arrhenius plot strongly depends on the temperature. Fig. 2 shows the slope –d(ln ρ)/d(1/T) versus the temperature at various magnetic fields for H||c. We can find that at a fixed field the absolute of slope decreases with the increasing of temperature, showing a linear behavior, below a certain temperature T^*, as indicated by a straight solid line; above the temperature T^*, the slope...
increases with the decreasing of temperature, following the Yeshurun–Malozemoff model, as indicated by a solid curve. We defined the crossover from the Y–M model to the straight line as the characteristic temperature $T^*$. To keep the picture clear to see, we only mark the position of the temperature at 5 T, indicated by the arrow, in the inset of Fig. 2. The physical meaning of the characteristic temperature $T^*$ will be explained in the following.

It is well known that the thermally activated flux creep can produce dissipation suggested by Palstra et al. [9] as follows:

$$\rho(T, H) = \rho_0 \exp(-U_0/kT)$$  \hspace{1cm} (1)

where $\rho_0$ is the pre-exponential factor independent of field and orientation, $k$ is the Boltzman constant and $U_0$ is the actual activation energy that generally depends on the temperature $T$, the current density $J$ and the applied magnetic field $H$. Generally, the current density dependence of activation energy is a constant when the measuring current density is lower than $10^3 \text{ A/cm}^2$ [13,14]. From Eq. (1), we can understand that the slope $-d(\ln \rho)/d(1/T)$ of $\ln \rho \sim 1/T$ plot is the effective energy $U_{\text{eff}}$. $U_{\text{eff}} = -d(\ln \rho)/d(1/T)$. Therefore, Fig. 2 gives us an information of the activation energy that the value of $U_{\text{eff}}$ is slowly increasing with the decreasing of temperature above a certain temperature $T^*$; below the temperature $T^*$, the effective activation energy increases rapidly with the decreasing of temperature, indicating that the flux lines are softened. The similar behavior of the activation energy is also reported in HgBCCO samples [10] and BSCCO single crystal [15]. Safar et al. [15] and Carruzzo and Yu [16] claimed that the rapid increasing of effective energy with the decreasing temperature shows the vortex lines into a vortex-glass state. However, the vortex-glass line in the YBCO thin films showed that it is lower than the irreversibility line determined by the criteria of $R/R_0 = 0.05\%$ [17]. The characteristic temperature $T^*$ is not consistent with the vortex-glass transition temperature. In addition, we will find that the temperature dependence of pinning energy follows the thermally activated flux creep behavior above the temperature $T^*$, as shown in Fig. 2. Therefore, we contest that the vortices are softened below the characteristic temperature $T^*$. The characteristic temperature $T^*$ might be a crossover from the vortex softened state to the thermally activated flux creep state.
In fact, considering the field and temperature dependencies of activation energy \( U_0 \) in Eq. (1) at a constant measuring current density, we can write the activation energy as \( U_0(H, T) = U(H)U(T) = U(H)(1 - T/T_c)\beta \). Therefore, we can obtain the effective activation energy,

\[
U_{\text{eff}} = -\frac{d \ln \rho}{d(1/T)} = U_0(H, T) - T \frac{dU_0(H, T)}{dT} = U(H)\left(1 - \frac{T}{T_c}\right)^\beta \left[1 + \beta \frac{T/T_c}{1 - T/T_c}\right].
\]

(2)

If we accept the temperature dependence of activation energy, \( U(T) = (1 - T/T_c)^\beta \) with \( \beta = 3/2 \), suggested by Yeshurun and Malozemoff in the thermally activated flux flow region, the effective activation energy should be followed in the form,

\[
U_{\text{eff}} = U(H)\left(1 - \frac{T}{T_c}\right)^{3/2} \left[1 + \frac{3}{2} \frac{T}{(T_c - T)}\right]
\]

(3)

where \( T_c \) is determined the temperature where the reduced resistance \( R/R_n = 0.01 \) at zero magnetic field and \( U(H) \) is a fitting parameter dependent on the applied magnetic field \( H \). The solid curves presented in Fig. 2 are the temperature dependence of the effective activation energy \( U_{\text{eff}} \) calculated by Eq. (3) for various magnetic fields. From Fig. 2, we can see that, besides below \( T^* \), there is another deviation of the experimental data from the theoretical curve at a constant magnetic field near the critical temperature. In general, the deviation is considered as the boundary between the thermally activated flux flow and the flux flow region where the temperature was symbolized as \( T_{irr} \) in Fig. 2. At the temperature \( T_{irr} \) the activation energy starts to become comparable to the thermal \( T \). The boundary has been discussed in YBCO thin films using the transport measurement by Cao et al. [18]. Therefore, we consider the flux lines are in the free flow region above the temperature \( T_{irr} \). Fig. 2 shows that the calculated results fit well with the part of \( U_{\text{eff}} \sim T \) curves obtained from the experiment results, indicating that the value of \( U_c \) in the limited temperature region \( T^* < T < T_{irr} \) are well described by the theoretical calculation suggested by Yeshurun and Malozemoff [2].

### 3.2. Anisotropy factor \( \gamma \)

It is also well known that the HTSCs are higher anisotropic. The anisotropy factor is usually defined as \( \gamma = (m_c/m_{ab})^{1/2} = \lambda_c/\lambda_{ab} = \xi_c/\xi_{ab} = H_{c2}^c/H_{c2}^a > 1 \) [19]. Generally, the anisotropy factor can be determined by the angular dependence of resistive transition curves at a constant magnetic field. According to GL theory, the resistive broadening in the external magnetic field \( H \) is equal to that in the effective magnetic field \( H_e \) along the \( c \)-axis when \( H \) tilted away from the \( ab \)-plane. The effective magnetic field \( H_e \) follows the formula,

\[
H_e(\theta) = H(\sin^2 \theta + \cos^2 \theta/\gamma^2)^{1/2}
\]

(4)

where \( \theta \) is the angle between the applied magnetic field and the \( ab \)-plane.

Combining Eq. (4) with the field dependence of irreversibility temperature \( T_{irr}, H = H_0(1 - t)^n \) for \( H||c \), we can obtain the angular dependence of the irreversibility temperature \( T_{irr}(\theta) \) at a fixed magnetic field \( H \), expressed by the following form [20,21]:

\[
T_{irr}(H, 0^\circ) - T_{irr}(H, \theta) \propto H^{1/n}(\sin^2 \theta + \cos^2 \theta/\gamma^2)^{1/2n}
\]

(5)

Meanwhile, the angular dependence of activation energy \( U \) at a fixed magnetic field \( H \) can be given in the form

\[
U_0(H, \theta) = U(H_e).
\]

(6)

Fig. 3 shows the temperature dependence of resistance for various angles from \(-6^\circ \) to \( 90^\circ \) at a constant magnetic field \( 4 \) T. The resistive transition becomes broader as the angle increases from \( 0^\circ \) to \( 90^\circ \). The inset of Fig. 3 can help us to see clearly the smaller part of resistance values. From Fig. 1, we can also extract the field dependence of the irreversibility temperature \( T_{irr} \), which is defined by the criteria \( R/R_n = 0.01 \% \), where \( R_n \) is the normal state resistance. Fig. 4 displays the information about the relations of \( T_{irr} \) and \( \theta \). From Fig. 4, we can see that \( T_{irr} \) changes monotonously with the increasing of angle \( \theta \) from \( 0^\circ \) to \( 90^\circ \). The cusp happens at \( 0^\circ \).

As shown in Fig. 4, the irreversibility temperature decreases with the increasing of the applied magnetic field \( H \) and shows a good power law
behavior, \( H \propto (T_{irr}(0) - T_{irr}(H))^n \) with \( n = 1.29 \) for \( H \parallel c \), in agreement with the “irreversibility line”, namely, \( H \propto (T_c - T_{d0})^{3/2} \).

According to Eq. (5), we can scale the angular dependence of irreversibility temperature at a constant magnetic field with different anisotropy value of \( \gamma = 5, 10, 20, 50, \) respectively. The scaling of \( T_{irr}(H, 0^\circ) - T_{irr}(H, \theta) \) vs \( H^{1/2}(\sin^2 \theta + \cos^2 \theta/\gamma^2)^{1/2n} \) displays a good linear behavior only when \( \gamma \) has a value of about 10. It is also consistent with the field dependence of irreversibility temperature for \( H \parallel c \). The scaling behavior shows that the anisotropy in the Er-doped YBCO crystal is larger than that in pure YBCO. This result gives us an information that the Er substitution can induce a larger anisotropy.

3.3. Field and angular dependencies of the activation energy \( U(H) \)

From Fig. 5, we can obtain the temperature dependence of the slope \(-d(\ln \rho)/d(1/T)\) of Arrhenius plot for various angles \( \theta \) at a fixed magnetic field 4 T. The slope behavior of Arrhenius plot for various angles \( \theta \) is similar to that for \( H \parallel c \), as observed in Fig. 2. Therefore, the calculation of effective energy \( U_e \) by the Yeshurun–Malozemoff model in the TAFF region is presented for different angle \( \theta \), as seen the solid curves of Fig. 5.

Fig. 4. Angular dependence of irreversibility temperature \( T_{irr} \) at a fixed field of 4 T. Inset displays the relationship of \( T_{irr}(0) - T_{irr}(H) \) vs \( H^{1/2}(\sin^2 \theta + \cos^2 \theta/\gamma^2)^{1/2n} \) with different anisotropy factor \( \gamma \) at 4 T and the field dependence of \( T_{irr}(0) - T_{irr}(H) \) for \( H \parallel c \).

Fig. 5. Temperature dependence of the slope of the Arrhenius curve \( U_e = -d(\ln \rho)/d(1/T) \) for various angles \( \theta \) at a constant magnetic field of 4 T. The scatter symbols are the experimental data for the various angles. The solid curves are calculated by the equation, \( U_e(T, H) = U(H)(1 - T/T_c)^{1/2} + 1.5T/(T_c - T) \). The straight solid lines are guides for the eyes.
Meanwhile, the value of \( U_0(H, \theta) \) from the fitting process was obtained for various angles \( \theta \).

Fig. 6 shows the field dependence of the fitting parameter \( U(H) \) for \( H \parallel c \) and/or for \( H_c \) at a fixed field of 4 T. From Fig. 6, the magnitude of the effective energy \( U \) for the YErBaCuO crystal is around from \( 2.7 \times 10^3 \) K at 7.5 T to \( 5.6 \times 10^4 \) K at 0.5 T for \( H \parallel c \), a little less than that for YBCO [9]. In order to compare the consistence of field dependence of activation energy for \( H \parallel c \) with that for various angles \( \theta \), we plot the effective magnetic field of activation energy with different anisotropic factor \( \gamma \). The angular dependence of activation energy with \( \gamma \approx 10 \) is quantitatively consistent with the field dependence of that for \( H \parallel c \). The value of \( U(H) \) decreases with the increasing of applied magnetic field and follows a power law behavior, \( U = AH^{-\gamma} \) with \( A \approx 2.14 \times 10^4H^{-1} \). The dash line in Fig. 6 is the fitting line. From this figure the results in the effective magnetic field \( H_e \) when \( H \) tilted away from the CuO\(_2\) plane, are consistent with those when \( H \parallel c \). As reported by Yeshurun and Malozemoff [2], we can get the intrinsic planar pinning and extrinsic point pinning from the magnetic field behavior of activation energy, \( U \propto H^{-\alpha} \), \( \alpha = 0.5 \) and 1 are responsible for the intrinsic planar pinning and extrinsic point pinning, respectively. For our sample, \( \alpha \approx 1.0 \) indicates that the extrinsic point pinning is main flux pinning. The extrinsic point pinning might be resulted from the Er addition. The Er\(^{3+}\) substitution for Y\(^{3+}\) possibly destroyed the strength of coupling between the CuO\(_2\) because of the highly anisotropic g value in Er\(^{3+}\) ions [8] and changed the anisotropy of the sample.

### 3.4. Phase diagram in Er-doped MTG-YBCO crystal

According to above discussions, the field dependence of the characteristic temperature \( T^* \), \( T_{ff} \) and the irreversibility temperature \( T_{irr} \) can be drawn in a picture, as shown by the solid symbols in Fig. 7. The field dependence of \( T_{ff} \), \( T^* \) and \( T_{irr} \) shows the same behavior \( H \propto (1 - t)^n \) with \( n = 1.29 \). The angular dependence of \( T_{ff} \), \( T^* \) and \( T_{irr} \) at a fixed magnetic field for different angle \( \theta \) is also shown by the open symbols in Fig. 7. From Fig. 7, we can see that the phase diagram of Er-doped MTG-YBCO crystal is separated into several regions, namely flux flow, thermally activated flux flow, flux softened and vortex solid regions by three lines of \( H - T_{ff} \), \( H - T^* \) and \( H - T_{irr} \). At a fixed magnetic field, when the temperature decreases from above \( T_c \), the vortex lines firstly undergo a transition from flux flow to thermally activated flux creep. In the region, the extrinsic point defects might be main flux pinning centers. As the temperature decreases further, the flux lines go through a transition from thermally activated flux creep to the softened vortices. When the vortices are softened, the pinning energy increases rapidly with the decreasing...
temperature. In the region, the co-action of point defects and planar defects is responsible for the flux pinning [12]. In final, the vortex lines go into solid below the irreversibility temperature, $T_{irr}$. The existence of flux softened region might indicate that the melting transition of flux lines is a second order phase transition [22,23] in our sample with correlated disordered defects. Compared with the typical 2D BSCCO $T^* (\approx 0.45T_c)$ [15] and the transitional Hg-1223 $T^* (\approx 0.65T_c)$ [10] in 5 T, the $T^*$ value of YErBCO is about 0.92$T_c$. The width $\Delta T$ of the TAFF region at 5 T is about 18 K in Hg-1223 [10] and 8.4 K in YErBCO crystal, respectively. These comparisons show the much narrower TAFF region in YErBCO crystal.

4. Conclusions

We have measured the resistance property of Er-doped MTG-YBCO crystals as a function of temperature and magnetic field $H$ up to 7.5 T. The field dependence of effective activation energy for $H||c$ is consistent with the effective magnetic field dependence of effective activation energy at a fixed field of 4 T for different angle $\theta$. Er$^{3+}$ substitution for Y$^{3+}$ increases the anisotropy of the MTG-YBCO sample possibly because of the highly anisotropic $g$-value of Er. The effective activation energy is discussed by the Yeshurun–Malozemoff model. The results indicate that the phase diagram of Er-doped MTG-YBCO crystal can be separated into four regions, namely flux flow, thermally activated creep, soft vortex liquid and vortex solid regions by three lines of $H-T_{ff}$, $H-T_{C3}$ and $H-T_{irr}$. In the thermally activated creep region, the extrinsic point defects might be main flux pining centers. In the soft vortex liquid region, the co-action of point defects and planar defects is responsible for the flux pinning.

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