

Lattice QCD + Hydro/Cascade Model of Heavy Ion Collisions

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Outline

- Calculation of T_c via lattice QCD – domain wall fermion method
- Parameterization of LQCD EoS
- Model of heavy ion collision including:
 - Initial, non-equilibrium flow (Pratt)
 - 2D viscous hydrodynamics (Romatschke's vh2)
 - Parton cascade (URQMD)

Lattice QCD with Domain Wall Fermions

Staggered

- Many recent high-precision calculations are performed with some variant of staggered fermion discretization (stout-link, asqtad, p4, HISQ)
- Single quark flavor for staggered fermions correspond to 4 flavors of continuum quark flavor.
- Spontaneous breakdown of SU(4) chiral symmetry \rightarrow 15 Goldstone bosons.
- However, lattice effects explicitly break SU(4) chiral symmetry \rightarrow U(1). Only one GB. Other pions have non-zero mass of $O(a^2)$
- To recover a one flavor theory on the lattice, take $\frac{1}{4}$ root.

Domain Wall Fermions

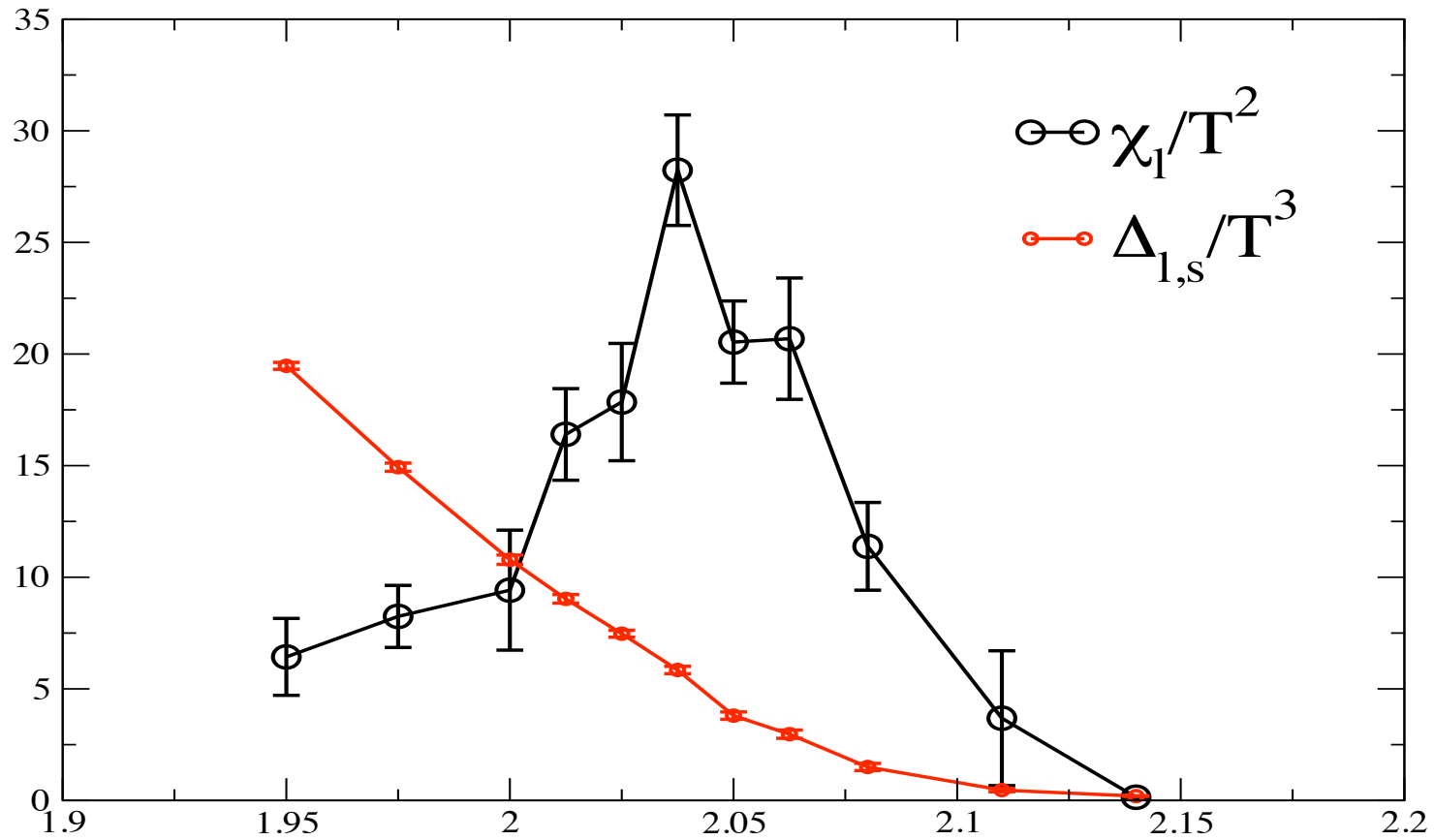
- Domain Wall Fermions (DWF) faithfully preserve $SU(N_f)$ chiral symmetry to arbitrary accuracy even at finite lattice spacing.
- Therefore, meson spectrum, e.g. 3 light pions, is more correctly reproduced by DWF method.
- Penalty: QCD with DWF is recovered as a 4-d space-time slice of a 5-d theory.

Staggered v. DWF

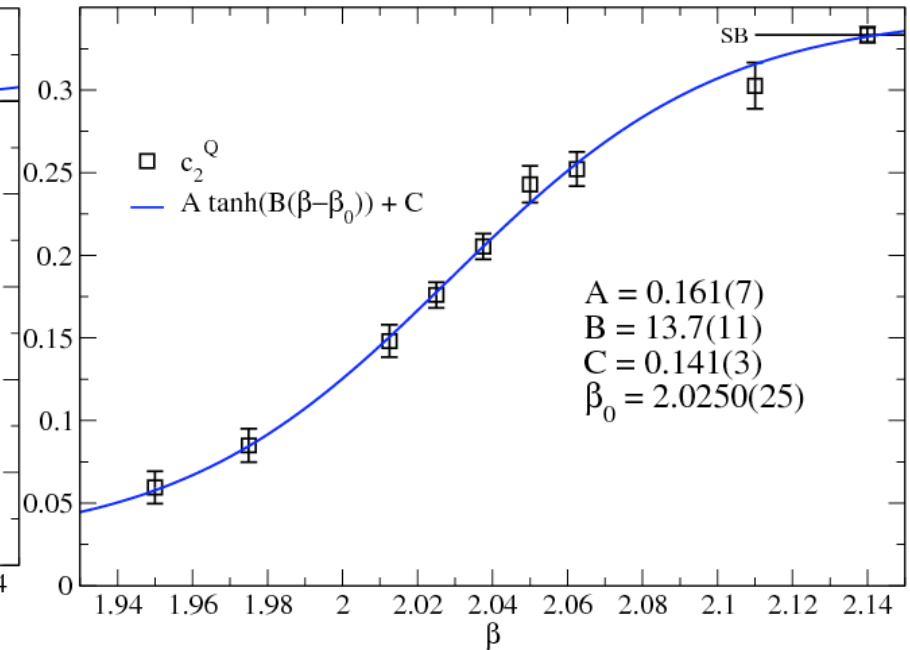
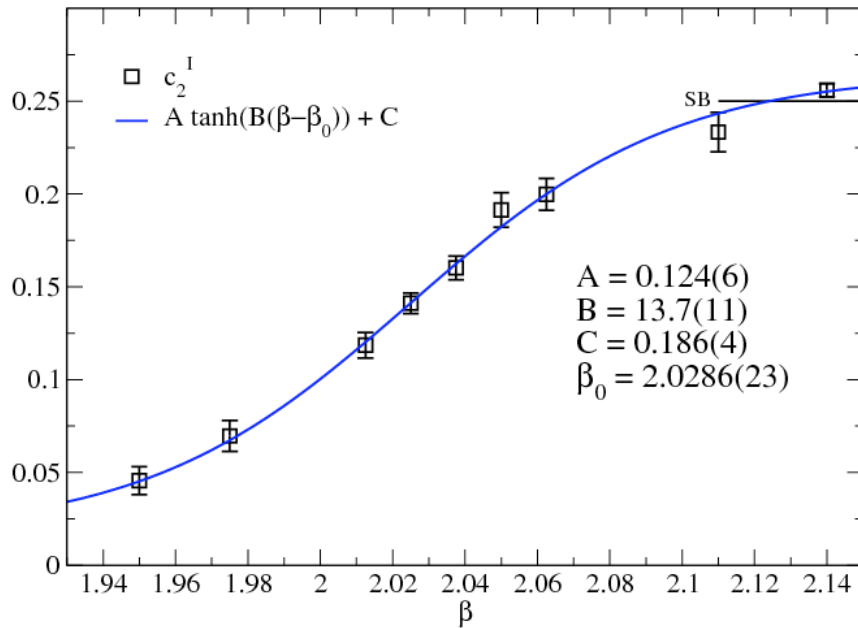
- Primary reason to use staggered fermions: cost.
- Size of fifth dimension in DWF calculations: 8-32.
- Staggered fermions approach smaller lattice spacing at high precision faster than DWF.
- Since $T = 1/(N_t a)$, lattice calculations are done at fixed N_t and varying lattice spacing.
- Until recently, only large lattice spacings feasible for exploration of finite T QCD ($N_t=4, 6$). In this regime, DWF formulation does not work so well

DWF at $N_t = 8$

- Well-known disagreement for T_c among staggered fermion calculations. Cannot agree on whether chiral, deconfining transitions are distinct. $T_c = 150\text{-}200$ MeV
- Calculations at $N_t=8$ for DWF are feasible. Useful check on the staggered calculations.
- Work done in collaboration with RBC Collaboration (arXiv:0911.3450)
- Vary lattice coupling ($\beta=6/g^2$) to change temperature.
- Calculate chiral, deconfinement observables.



- χ_1/T^2 -> Chiral susceptibility. Peaks in transition region
- $\Delta_{1,s}/T^3$ -> Chiral condensate. Non-zero at low temperature, zero at high temperature.

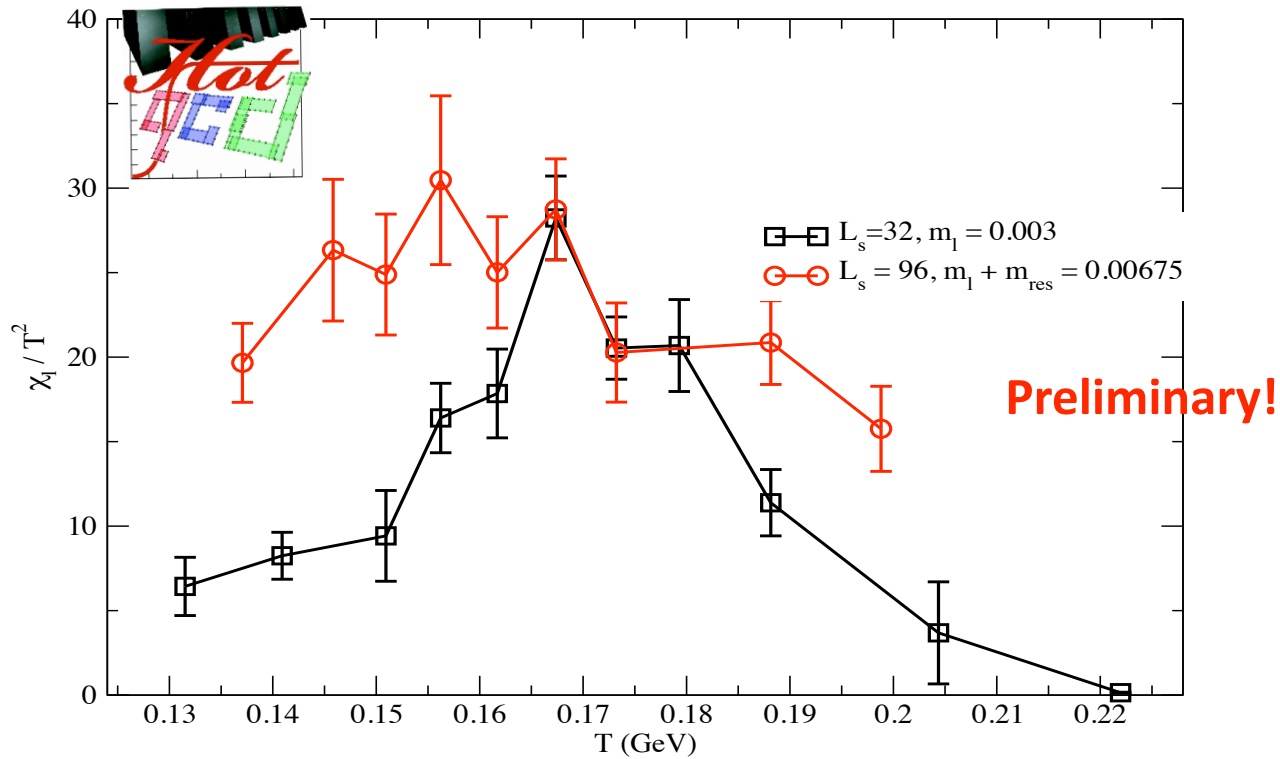


- Deconfinement observables: isospin and charge susceptibilities.
- Inflection point determined by fitting data to ansatz.
- Consistent with peak in chiral susceptibility.
- However, SB limit already saturated at low temperature, as expected as DWF formulation is unimproved at high temperature.

Caveats

- Limitations in this calculation:
 - Small volume (Finite volume effects not controlled)
 - Lacks precision of staggered studies.
 - Quark mass not held constant in this calculation -> $m_\pi \approx 300$ MeV at $T = 170$ MeV, but larger at low temperature, smaller at high temperature.
 - Single lattice spacing – cannot make continuum extrapolation (4-7% error suggested by other calculations)
 - Single set of masses – guess at extrapolation to physical quark masses.

Comparison with $L_s = 96$ calculation



$$T_c = 171(17)(10) \text{ MeV}$$

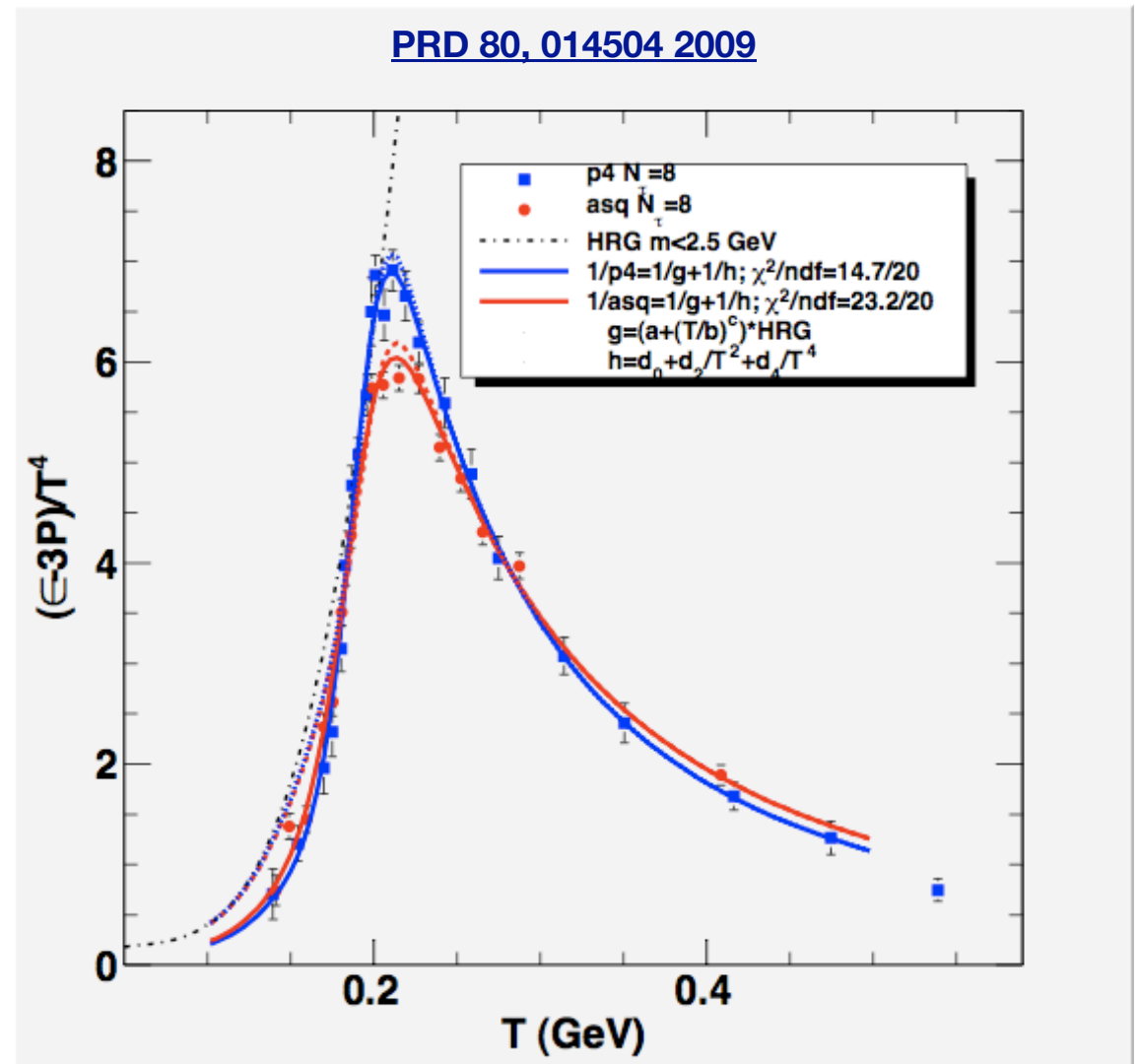
Hydro/Cascade Model

Description of Model

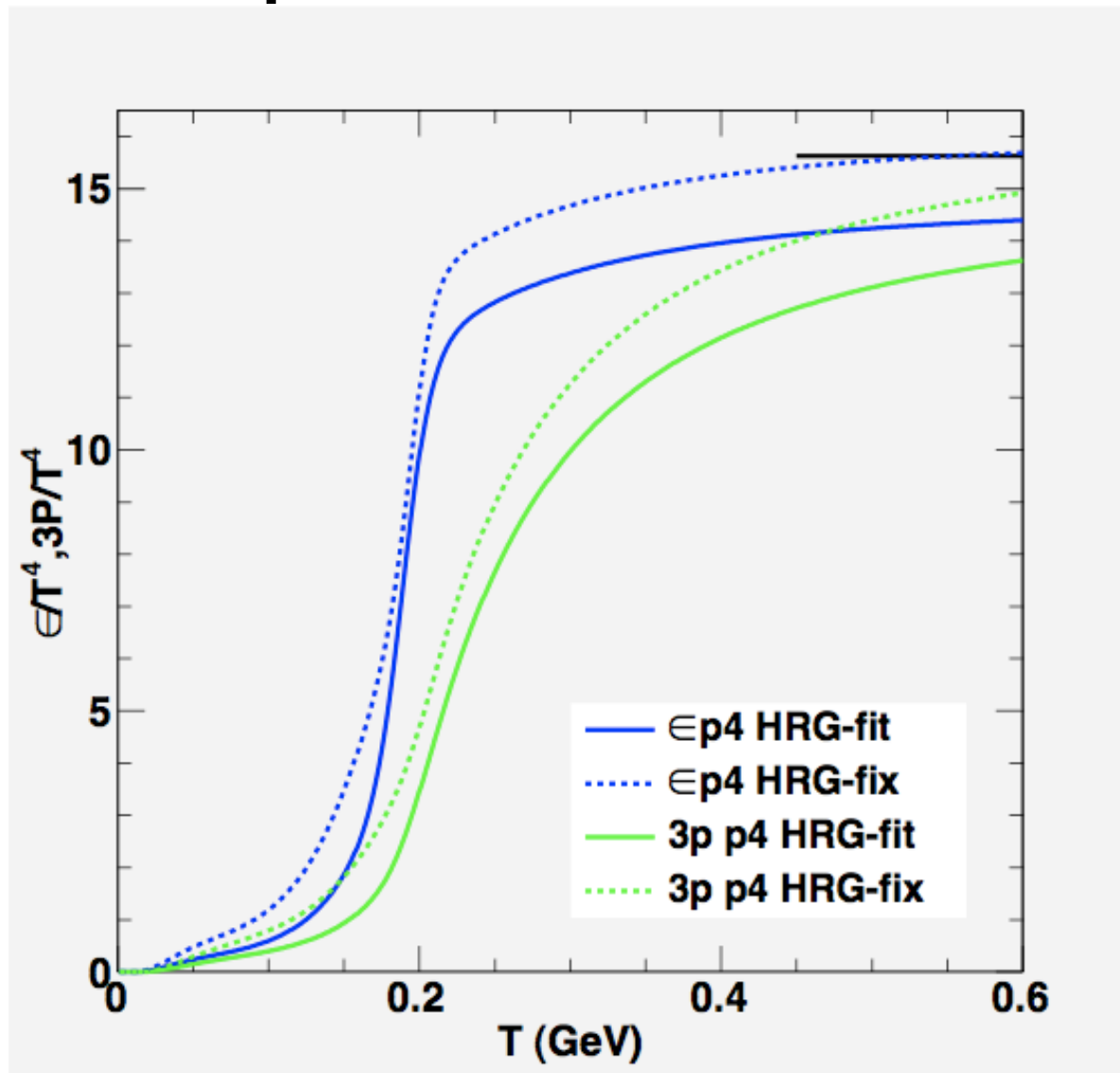
- Hybrid model includes:
 - Pre-thermalization flow (Pratt arXiv:0810.4325)
 - 2D viscous hydrodynamic evolution (Romatschke's vh2)
 - Hadron cascade, after Cooper-Frye freezeout (URQMD)
- Examine the effect of varying:
 - Equation of state (LQCD EoS vs. 1st order transition)
 - Viscosity
 - Pre-thermalization flow.
 - Initial conditions/freezeout temperature
- Collaborators:
 - Ron Soltz, Andrew Glenn, Jason Newby (LLNL and ORNL)
 - Scott Pratt
- Talk by R. Soltz at CATHIE/TECHQM

Parameterizing LQCD EoS

- Already saw a more detailed study in talk by Petreczky, but also many others.
- Let $f(T)$ be parameterization of EoS
- Suggestion by K. Rajagopal:
- $1/f(T) = 1/g(T) + 1/h(T)$
- $g(T)$ -> low temperature
- $h(T)$ -> high temperature
- $h(T) = d_2/T^2 + d_4/T^4$
- $g(T) = (a + (T/T_0)^b) * \text{HRG}(T)$
- Fix low T to HRG by setting $a = 1.0$

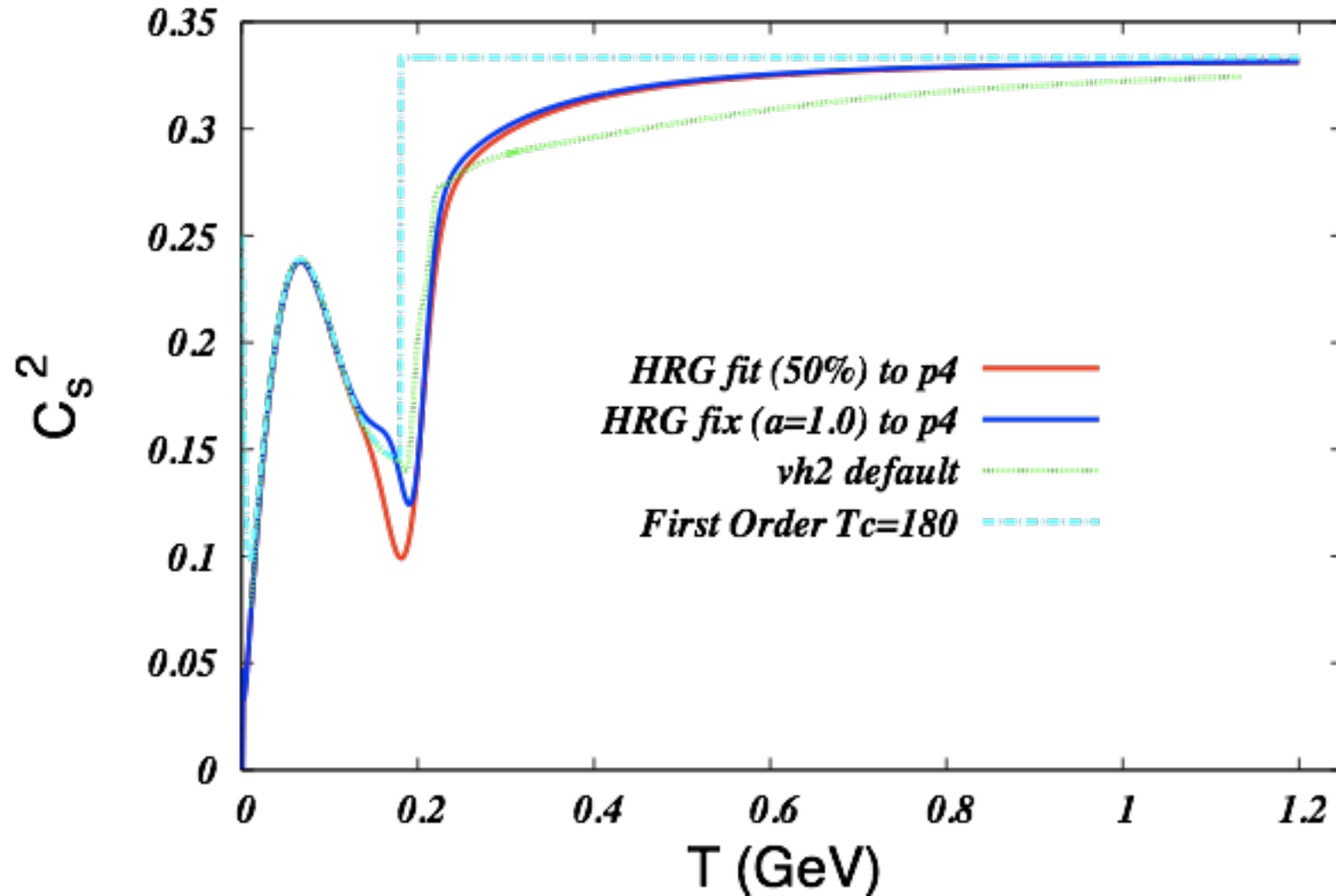


Re-parameterized EoS



Speed of Sound

Hydro EOS Comparison

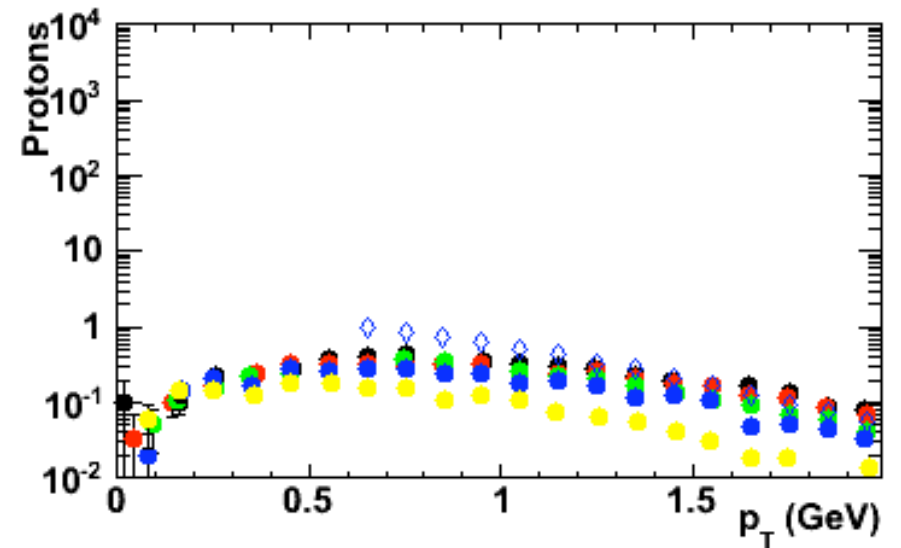
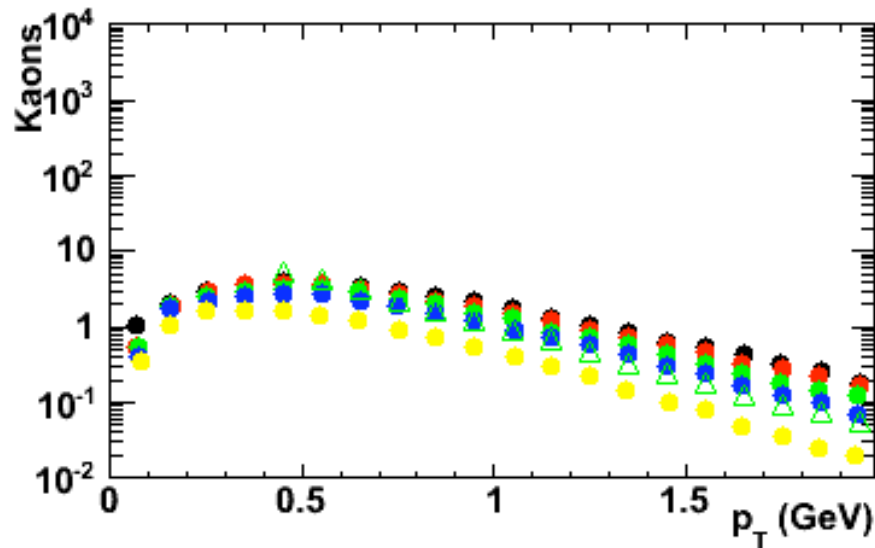
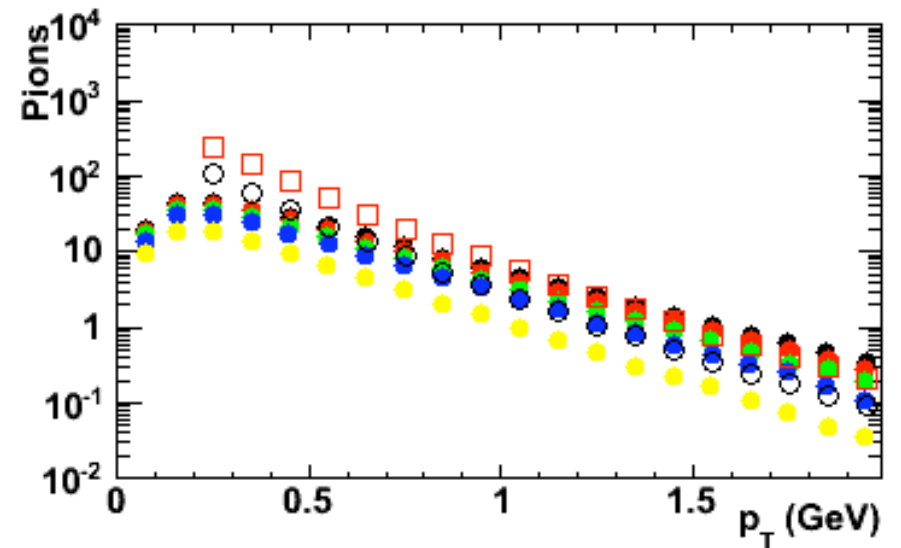


Description of existing runs

- Initial Flow
 - From Glauber profile.
 - $b = 3.4, 5.5 \text{ fm.}, T_{\text{initial}} = 250\text{-}350 \text{ MeV}$
- Vh2 2-D hydro:
 - $\eta/s = 0.08 - 0.40$
 - EoS = Romatchske EoS, LQCD, LQCD+HRG
- Cooper-Frye freezeout
 - $T_{\text{freezeout}} = 120 - 170 \text{ MeV}$
- URQMD for hadronic cascade
- Match spectra to tune parameters

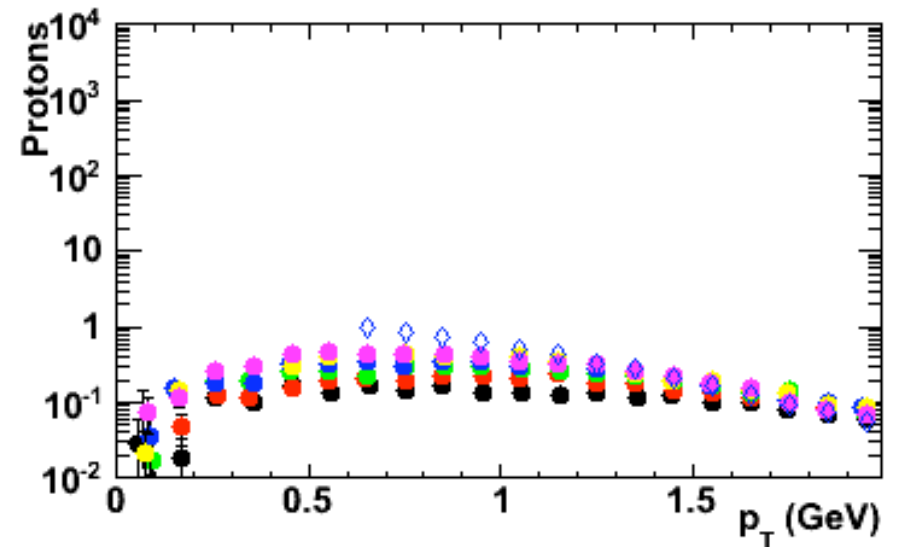
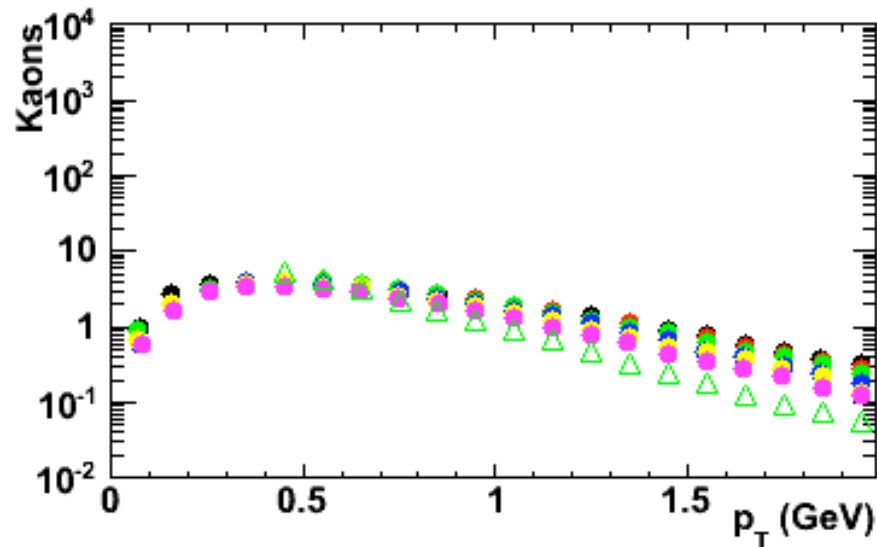
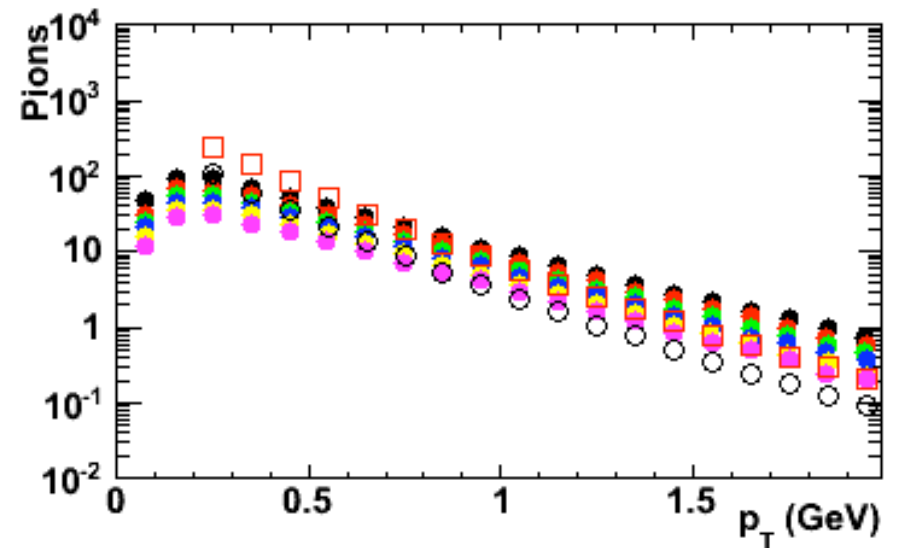
Spectra

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- j5.5_0.340_0.08_0.15_1_qcdIEOS.dat
- j5.5_0.320_0.08_0.15_1_qcdIEOS.dat
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- π 10-15% PhysRevC.69.034909
- △ K mb PhysRevC.69.034909
- ◇ p mb PhysRevC.69.034909



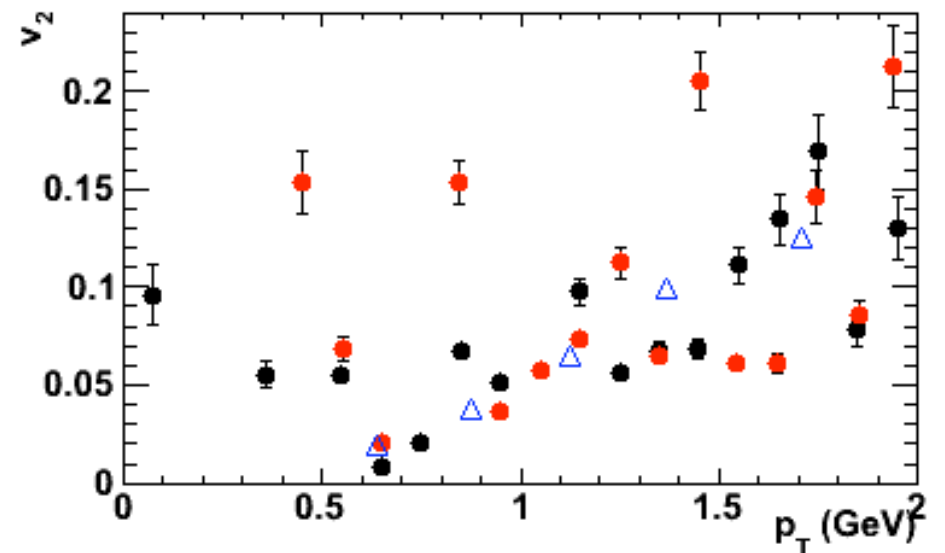
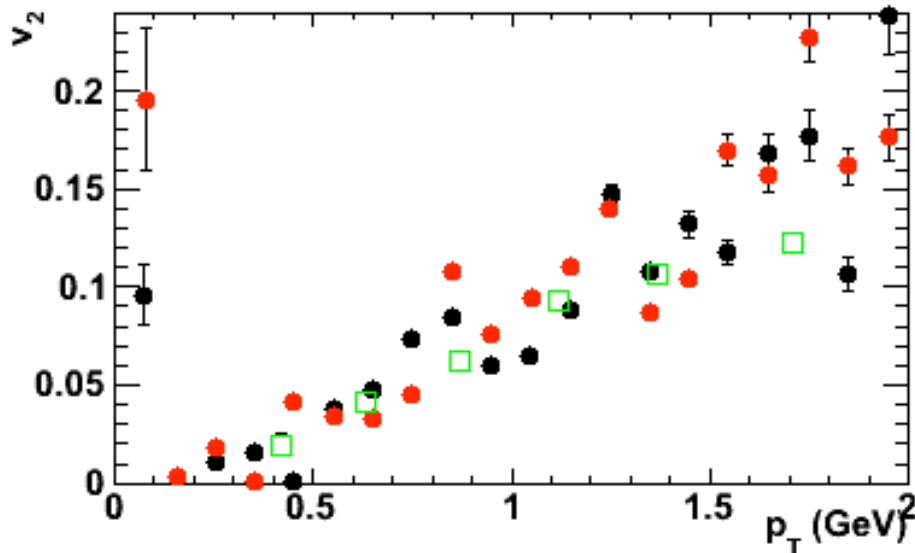
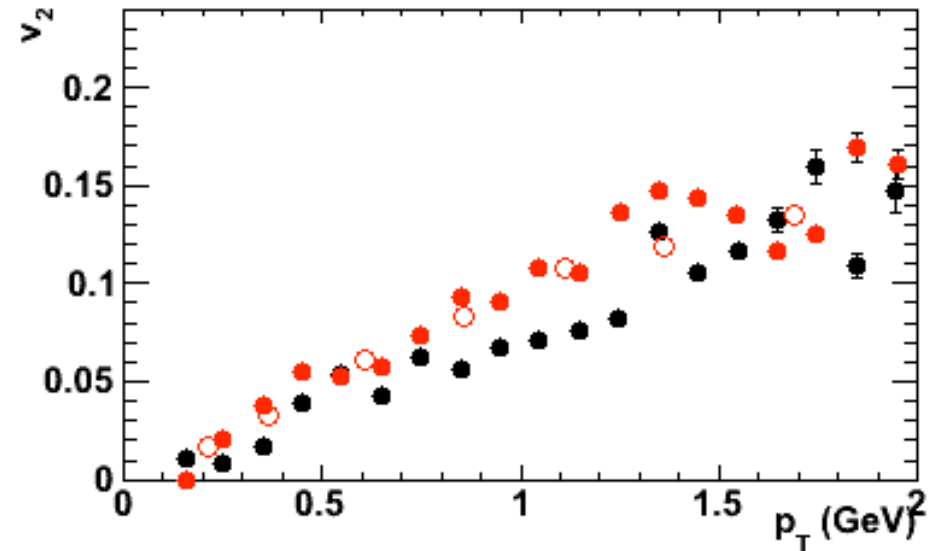
Spectra, $T_f=120-170$ MeV

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- j5.5_0.350_0.08_0.16_1_qcdIEOS.dat
- j5.5_0.350_0.08_0.17_1_qcdIEOS.dat
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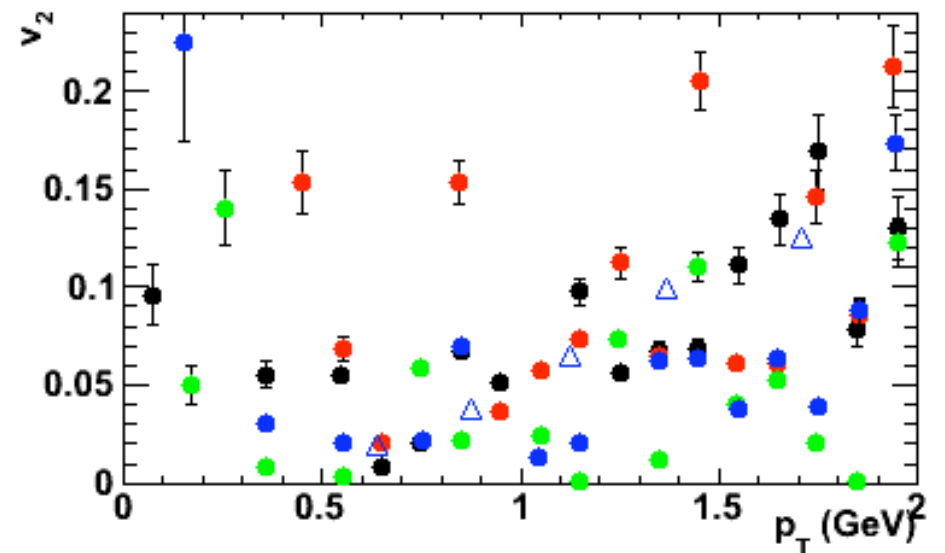
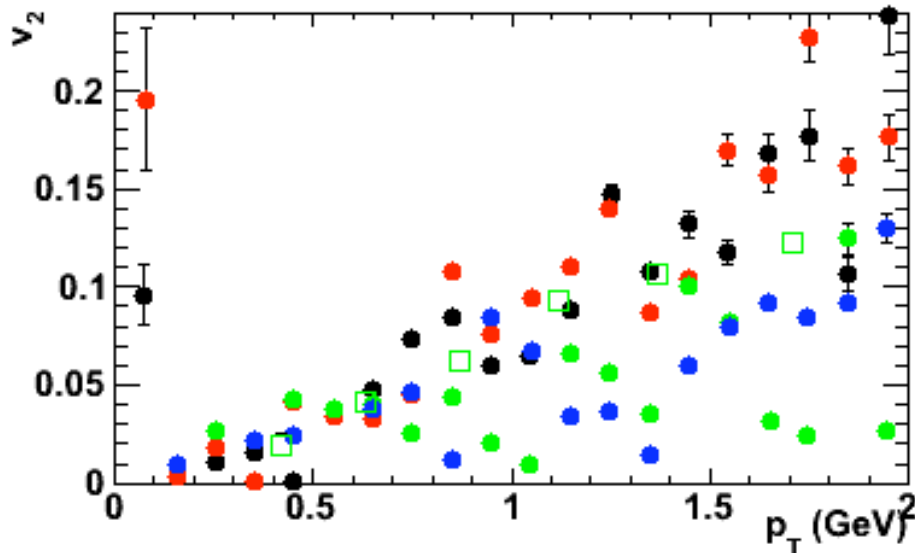
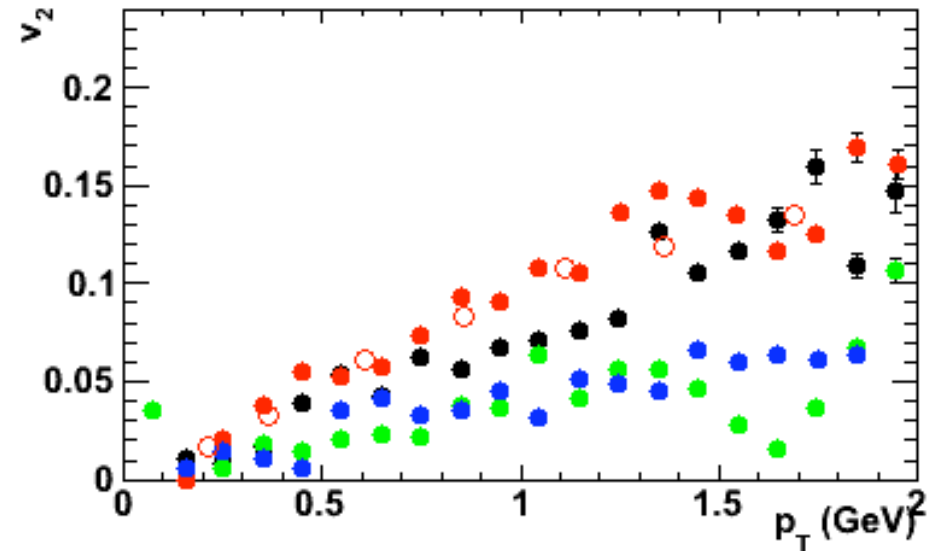
V_2 – with/without initial flow

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- j5.5_0.350_0.08_0.15_1_qcdIEOS.dat
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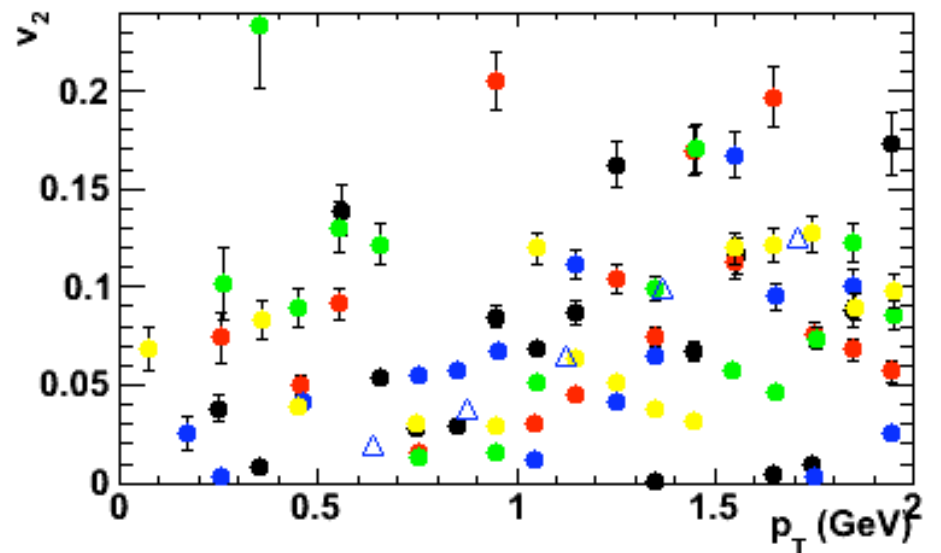
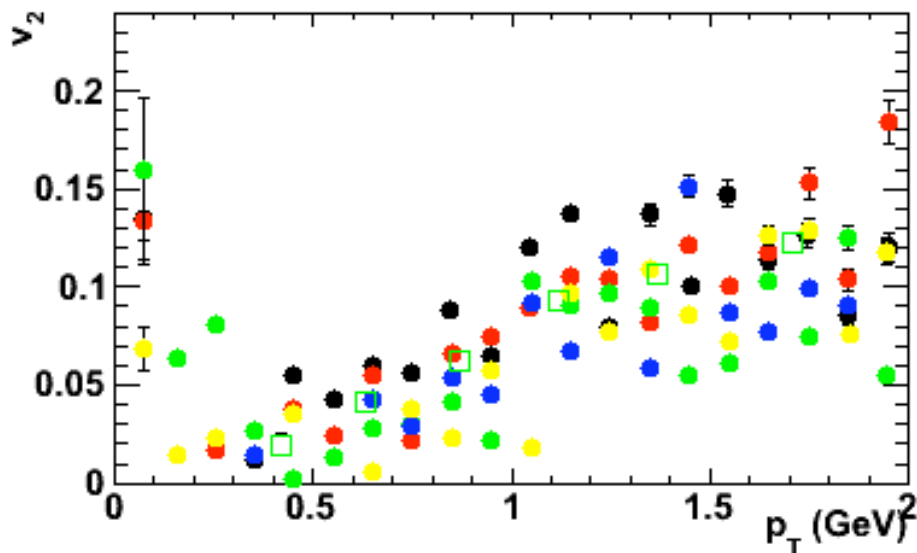
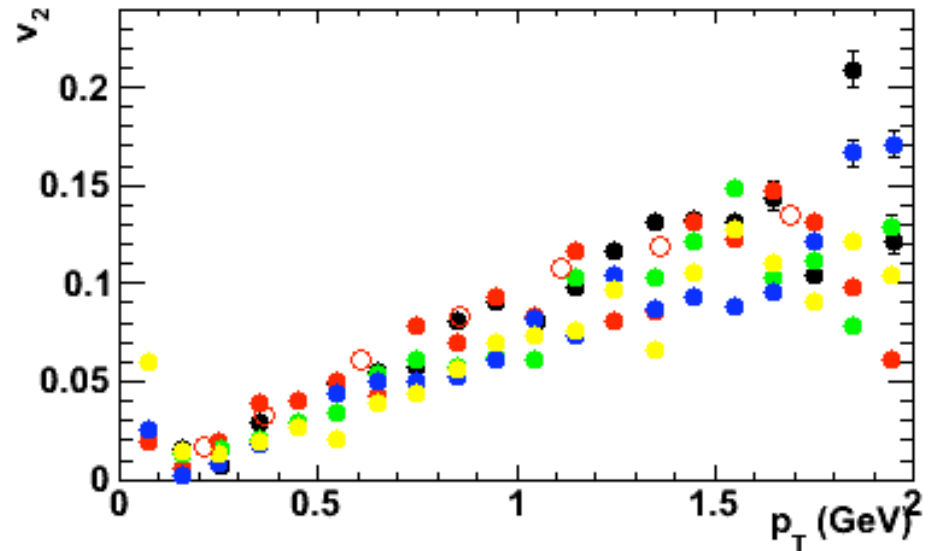
V_2 , $b = 3.4, 5.5$ fm.

- j5.5_0.350_0.08_0.15_0_qcdEOS.dat
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- j3.4_0.350_0.08_0.15_0_qcdEOS.dat
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V_2 , $\eta/s=0.08-0.40$

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- j5.5_0.350_0.16_0.15_1_qcdEOS.dat
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Conclusions

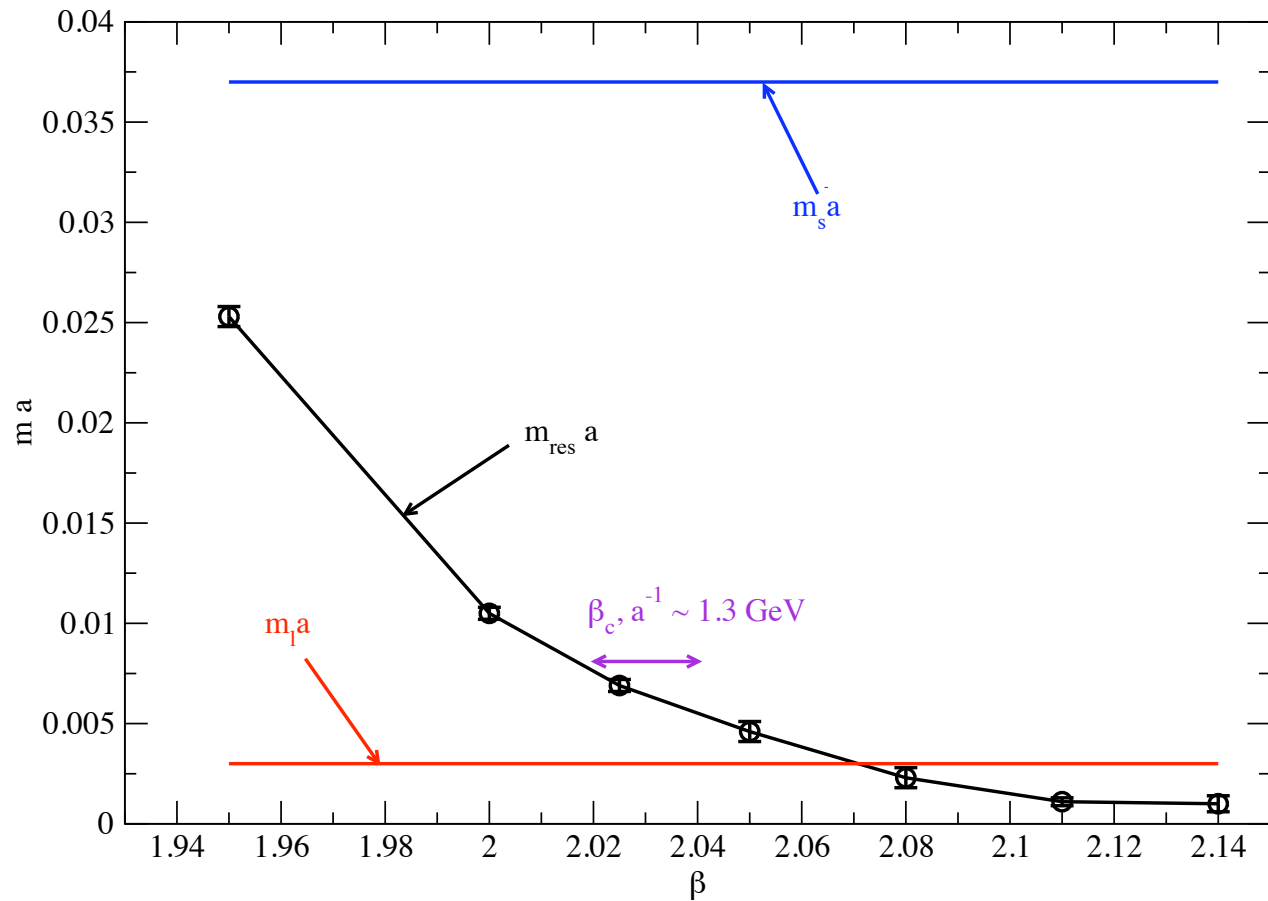
- Calculation of crossover temperature with DWF to compare with staggered-type calculations.
- $T_c \sim 170$ MeV, but with large error because of statistics and several systematic uncertainties.
- No splitting evident for deconfinement, chiral observables
- Not really in disagreement with either of conflicting staggered calculations.
- Exploratory calculation – need to do a calculation that corrects many of the flaws of current calculation.
- One is underway, thinking about other methods, but still computationally too expensive...

Conclusions (cont.)

- Hybrid model including pre-thermalization flow + 2D viscous hydrodynamics + URQMD (almost) working.
- Still work in progress.
- Goals:
 - Study collective flow, femtoscopy.
 - Effects of varying η/s , initial conditions, $T_{\text{freezeout}}$
 - Does pre-thermal flow help explain HBT puzzle?
 - Quantify effects of varying EoS
 - Systematic comparison to experimental data.

Backup

Residual Mass at $L_s = 32$



HBT Radii, varying viscosity

