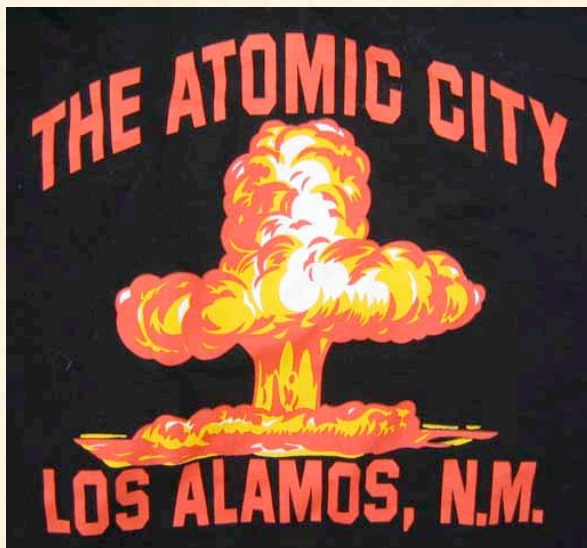


# $Z^0$ Tagged Jets as a Probe of the QGP

**Bryon Neufeld**

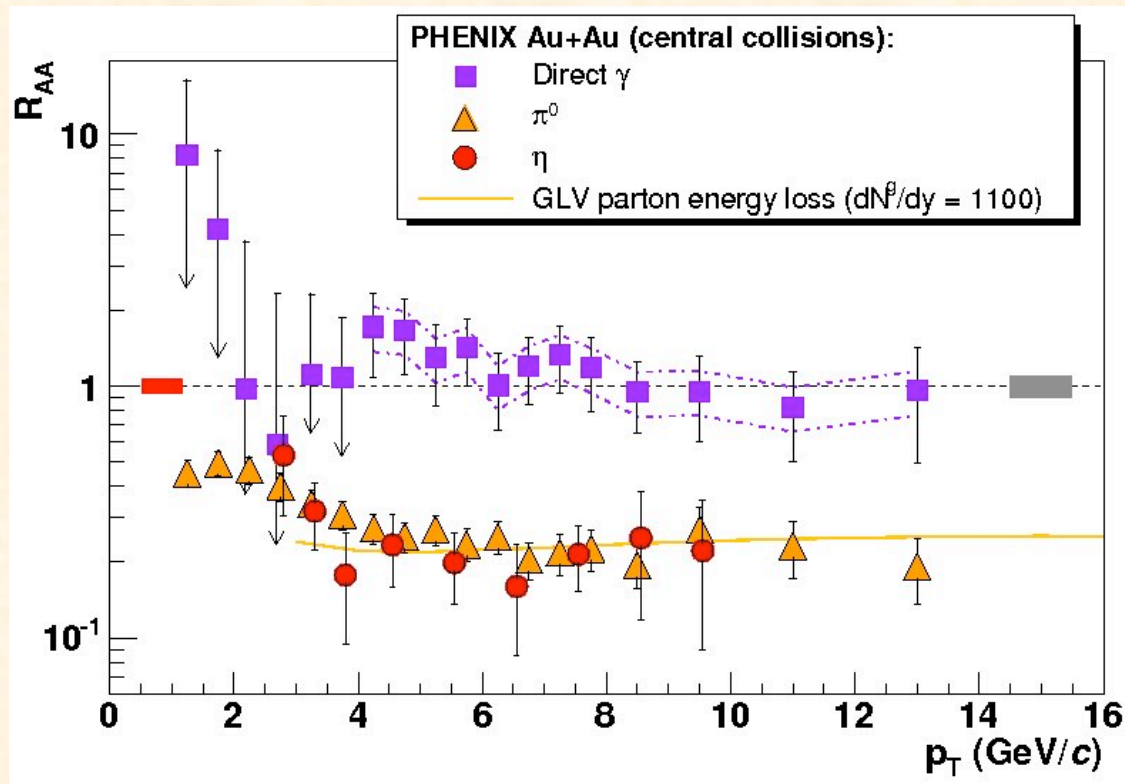
In collaboration with  
**Ivan Vitev and Ben-Wei Zhang**



Presentation of work done at  
***Los Alamos National Lab***

# Introduction

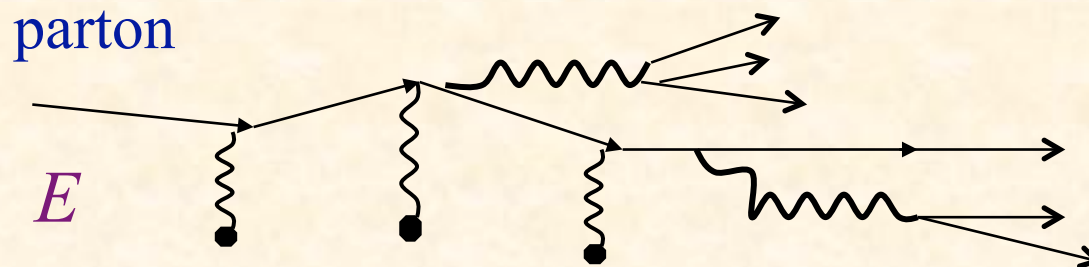
# Jet Quenching at RHIC – experimentally well established



$$R_{AA}(p_T, \eta) = \frac{1}{\langle N_{coll} \rangle} \cdot \frac{d^2\sigma^{AA} / d\eta dp_T}{d^2\sigma^{NN} / d\eta dp_T}$$

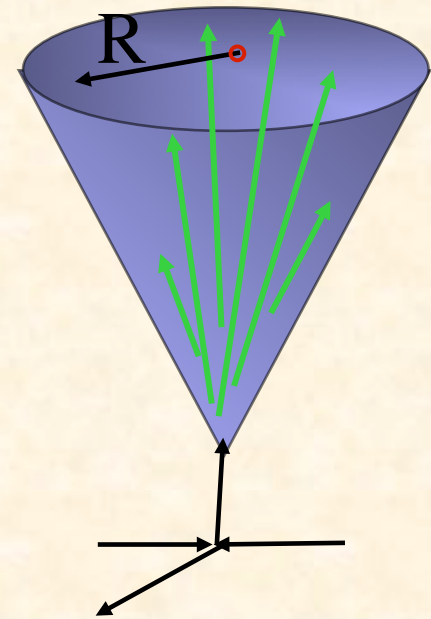
# Jet quenching as a probe of QGP

- ◎ Large leading particle suppression strong evidence for formation of QGP in HIC
- ◎ Parton energy loss sensitive probe of medium density, Debye scale, strong coupling, transport coefficients



# Limitations of leading particle suppression

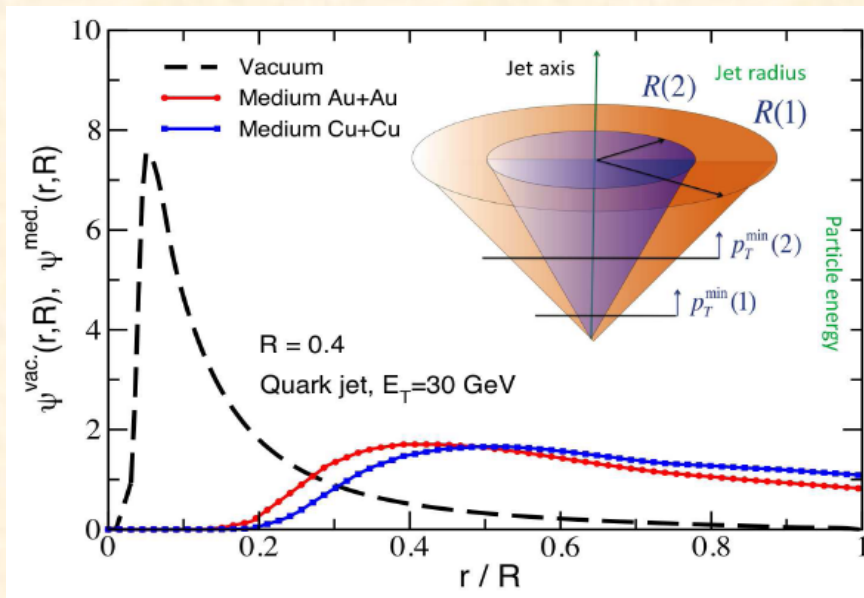
- $R_{AA}$  for single particle or  $I_{AA}$  for two particle correlations only measure the leading fragments of a jet.
- Jets: a spray of final-state particles moving roughly in the same direction.
- LP  $R_{AA}$  can be fit by formalisms with very different assumptions



$$R_{ij} = \sqrt{(y_i - y_j)^2 + (\phi_i - \phi_j)^2}$$

# The future of jet quenching physics- Jet shapes and jet cross sections

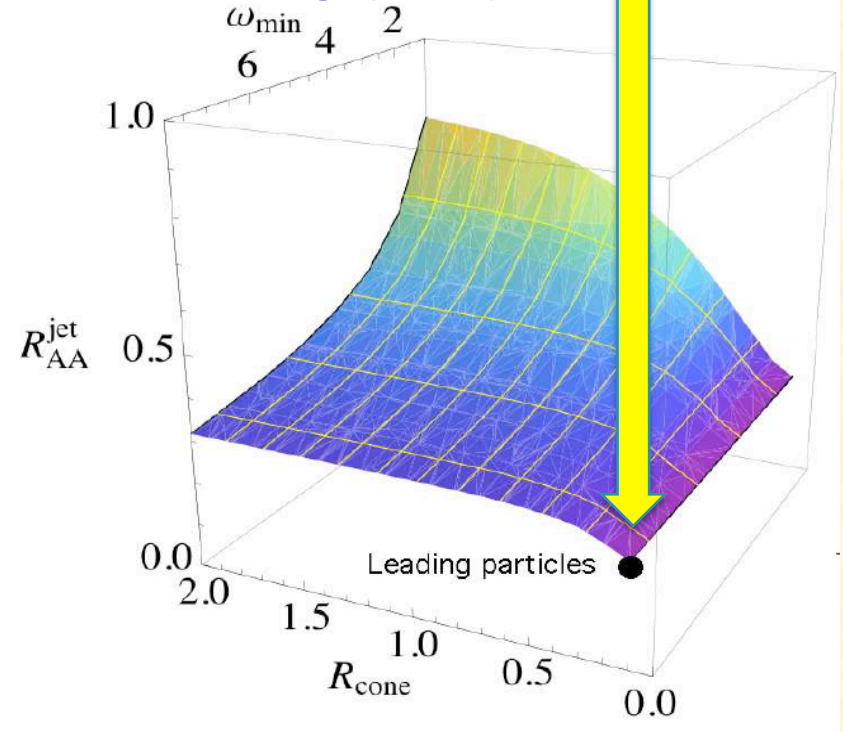
Explore the fraction of energy lost and variation of  $R_{AA}$  with changing cone radius/ $p_{Tmin}$



$$\Psi_{int}(r; R) = \frac{\sum_i (E_T)_i \Theta(r - (R_{jet})_i)}{\sum_i (E_T)_i \Theta(R - (R_{jet})_i)},$$

$$\psi(r; R) = \frac{d\Psi_{int}(r; R)}{dr}.$$

IV, B.-W Zhang, (2008)





# A theory of jet shapes and cross sections: from hadrons to nuclei,

I Vitev, S Wicks, BWZ, JHEP 0811,093 (2008)

Investigated for inclusive jets using  
GLV energy loss formalism

Number of scatterings

Momentum transfers

$$k^+ \frac{dN_g}{dk^+ d^2k_\perp} = \sum_{n=1}^{\infty} k^+ \frac{dN_g^n}{dk^+ d^2k_\perp} = \sum_{n=1}^{\infty} \frac{C_R \alpha_s}{\pi^2} \left[ \prod_{i=1}^n \int_0^{L - \sum_{j=i+1}^n \Delta z_j} \frac{d\Delta z_i}{\lambda_g(z_i)} \int d^2q_i \left( \frac{1}{\sigma_{el}} \frac{d\sigma_{el}}{d^2q_i} - \delta^2(q_i) \right) \right]$$

$$\times \left[ -2C_{(1\dots n)} \cdot \sum_{m=1}^n B_{(m+1\dots n)(m\dots n)} \left( \cos \left( \sum_{k=2}^m \omega_{(k\dots n)} \Delta z_k \right) - \cos \left( \sum_{k=1}^m \omega_{(k\dots n)} \Delta z_k \right) \right) \right]$$

Color current propagators

Coherence phases  
(LPM effect)

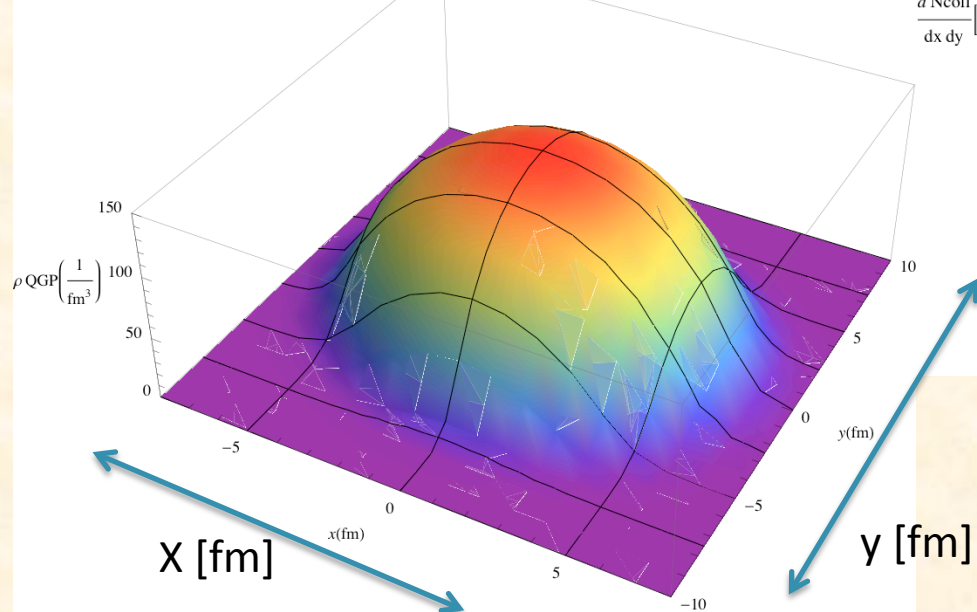
# Initial Geometry

$$S^{1/2}_{NN} = 5.5 \text{ TeV}, \sigma_{in} = 65 \text{ mb}$$

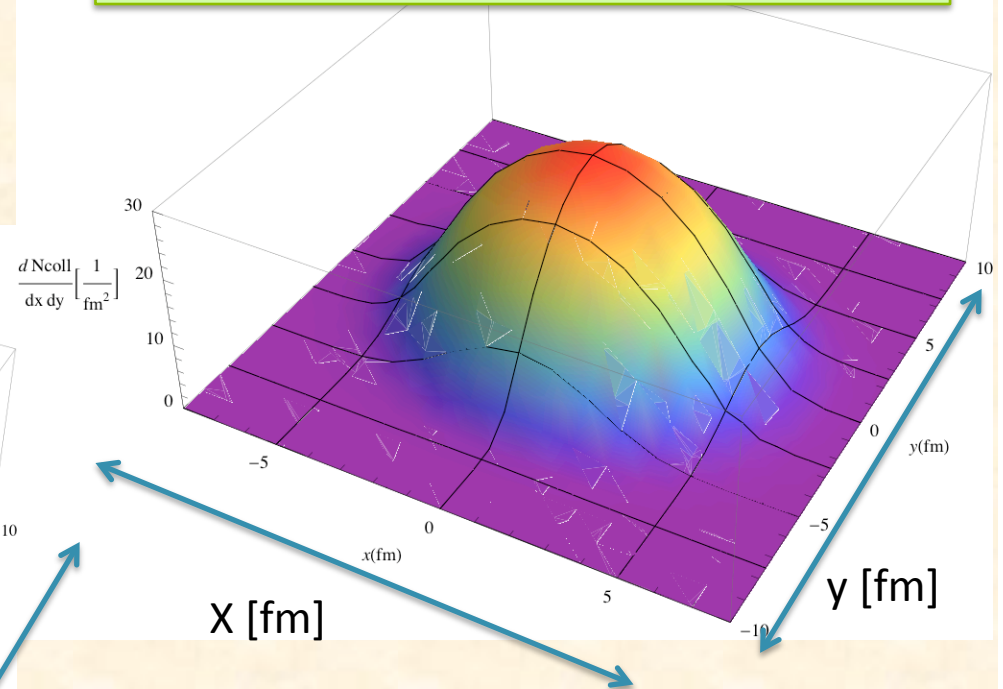
Optical Glauber

QGP density (3D) ~ **participant density (2D)**

Pb+Pb at  $b=3 \text{ fm}$



**Binary collision density (2D)** – corresponds to jet production

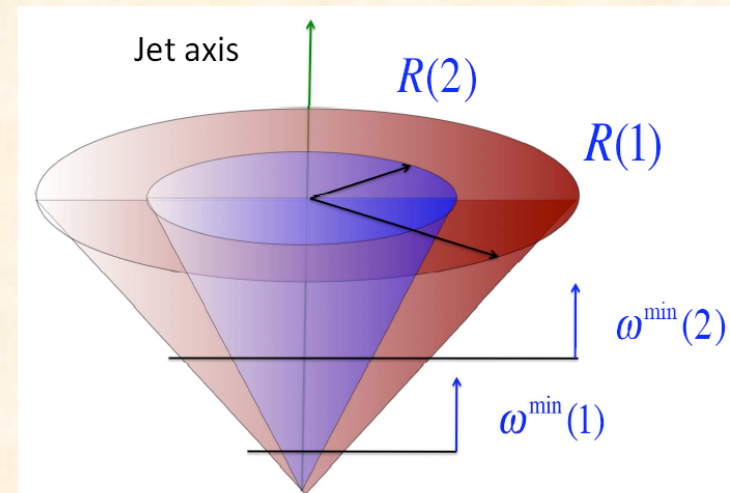
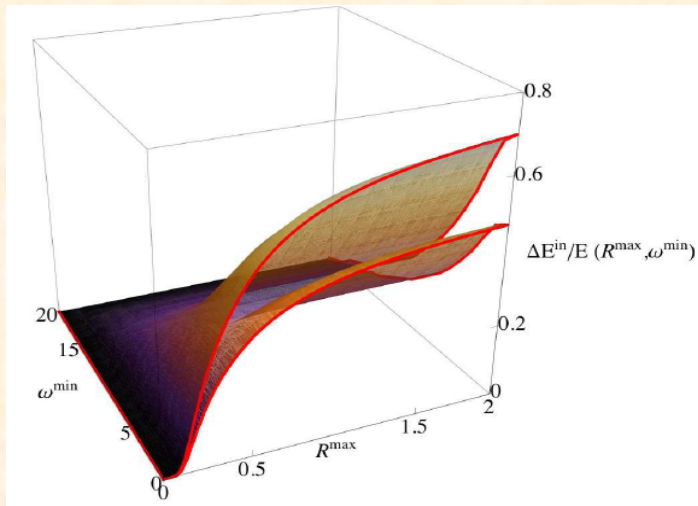


- Note the difference in the distributions

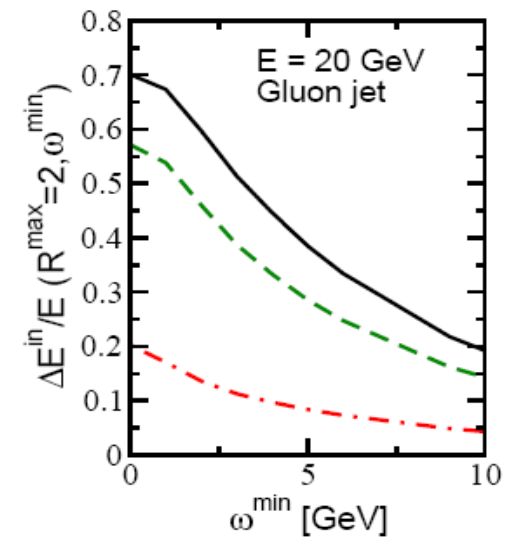
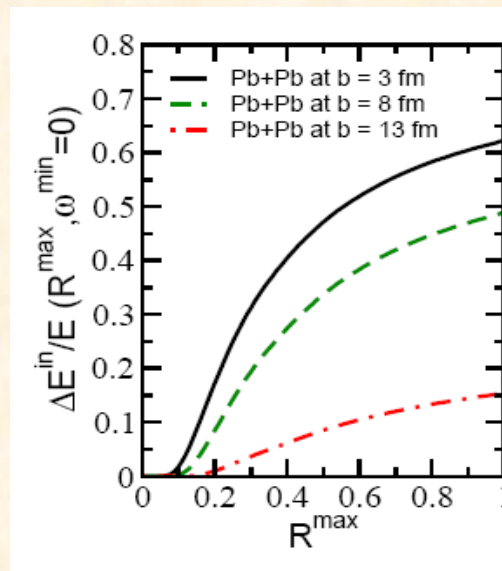


# Energy loss distribution

$$\frac{\Delta E^{in}}{E}(R^{\max}, \omega^{\min}) = \frac{1}{E} \int_{\omega^{\min}}^E d\omega \int_0^{R^{\max}} dr \frac{dI^g}{d\omega dr}(\omega, r)$$



- Energy ratio goes down with larger  $b$ .
- Energy ratio becomes smaller with smaller  $R$  and larger  $\omega^{\min}$



# Inclusive Jet cross section @HIC and $R_{AA}$

$$\frac{\sigma^{AA}(R, \omega^{\min})}{d^2 E_T dy} = \int_{\epsilon=0}^1 d\epsilon \sum_{q,g} P_{q,g}(\epsilon) \frac{1}{(1 - (1 - f_{q,g}) \cdot \epsilon)^2} \frac{\sigma_{q,g}^{NN}(R, \omega^{\min})}{d^2 E'_T dy}$$

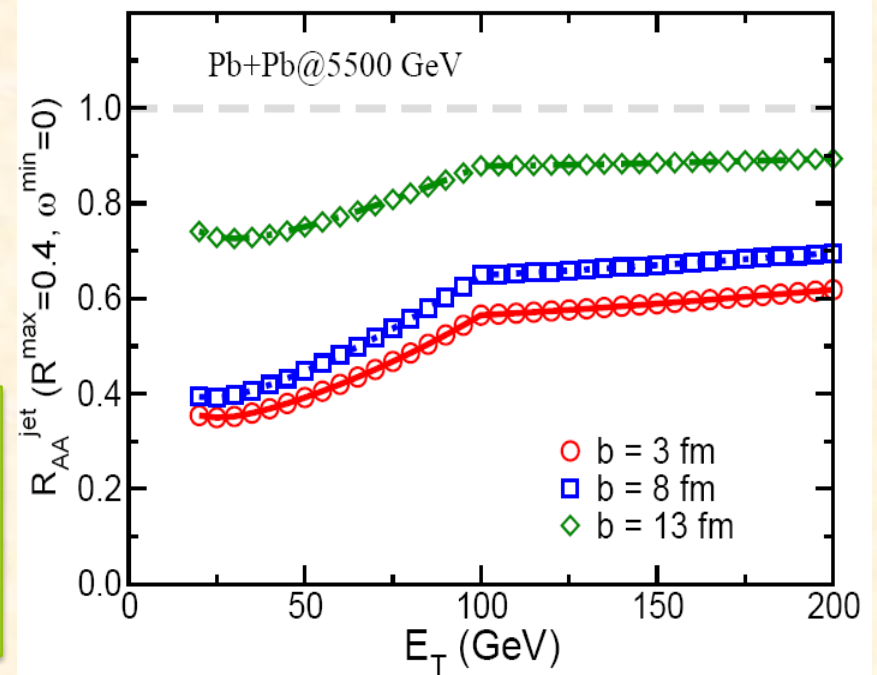
$$E'_T = E_T / (1 - (1 - f_{q,g}) \cdot \epsilon)$$

$$f = \frac{\Delta E_{\text{rad}} \{ (0, R); (\omega^{\min}, E) \}}{\Delta E_{\text{rad}} \{ (0, R^\infty); (0, E) \}}$$

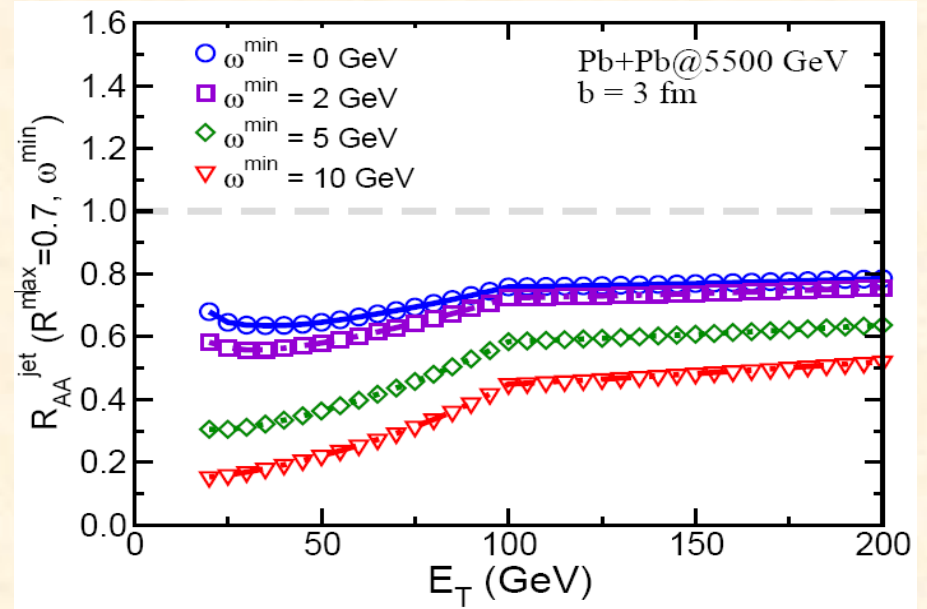
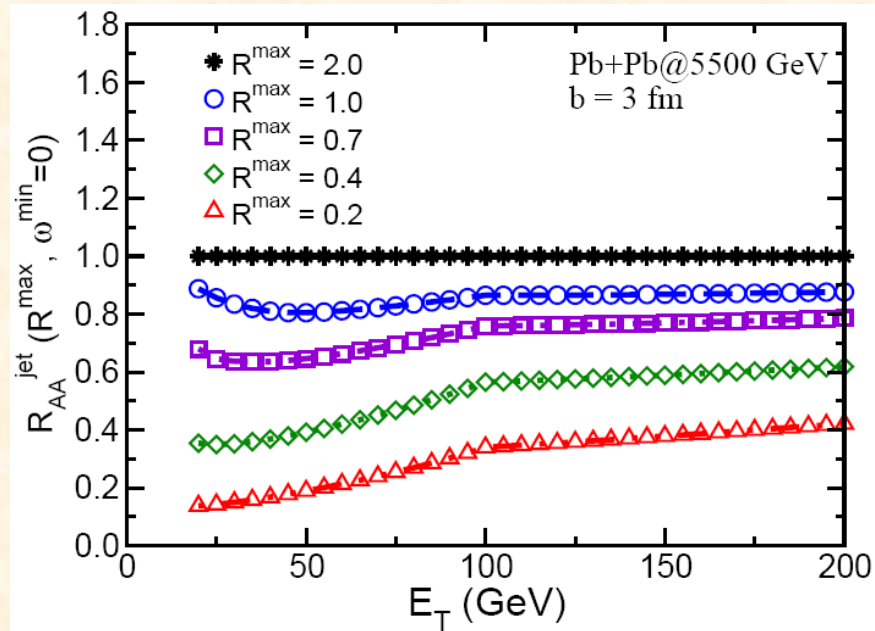
**Define nuclear modification factor for jet cross section:**

$$R_{AA}^{\text{jet}}(E_T; R^{\max}, \omega^{\min}) = \frac{\frac{d\sigma^{AA}(E_T; R^{\max}, \omega^{\min})}{dy d^2 E_T}}{\langle N_{\text{bin}} \rangle \frac{d\sigma^{PP}(E_T; R^{\max}, \omega^{\min})}{dy d^2 E_T}}$$

**Centrality dependence of  $R_{AA}$  for jet cross section is similar to that for single hadron production**



# $R_{AA}$ vs $R^{\max}$ and $\omega^{\min}$



- $R_{AA}$  for jet cross section evolves continuously by varying cone size and acceptance cut.
- Contrast: single result for leading particle
- Limits:  $R_{AA}$  approaches to single hadron suppression with  $R^{\max}$  and large  $\omega^{\min}$

# Tagging with $Z^0$ boson

# Tagged Jets

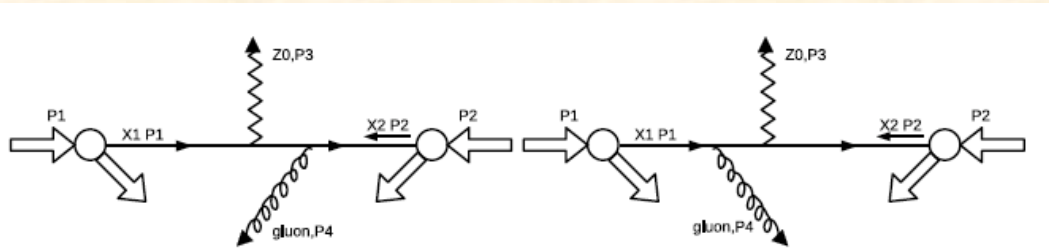


Figure 1: Diagrams contributing to  $Z^0$  + gluon jet production.

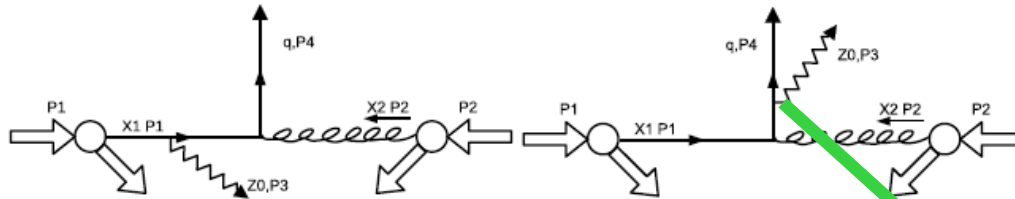


Figure 2: Diagrams contributing to  $Z^0$  + (anti)quark jet production.

$$R_q^2 + L_q^2 = \tau_q^2 - 4 e_q \tau_q \sin^2 \theta_w + 8 e_q^2 \sin^4 \theta_w.$$

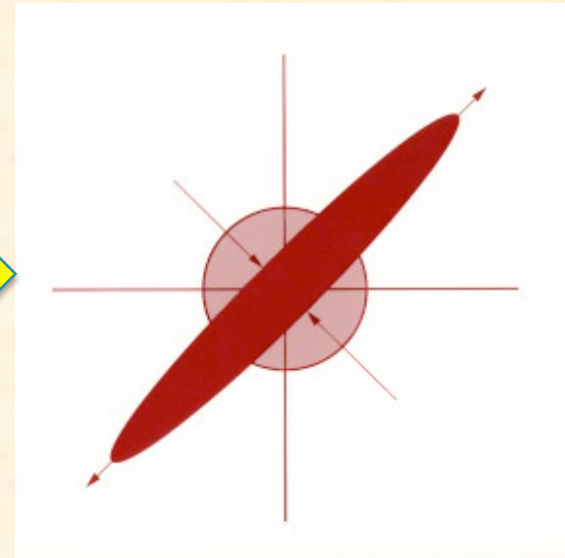
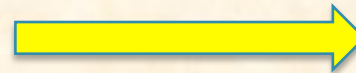
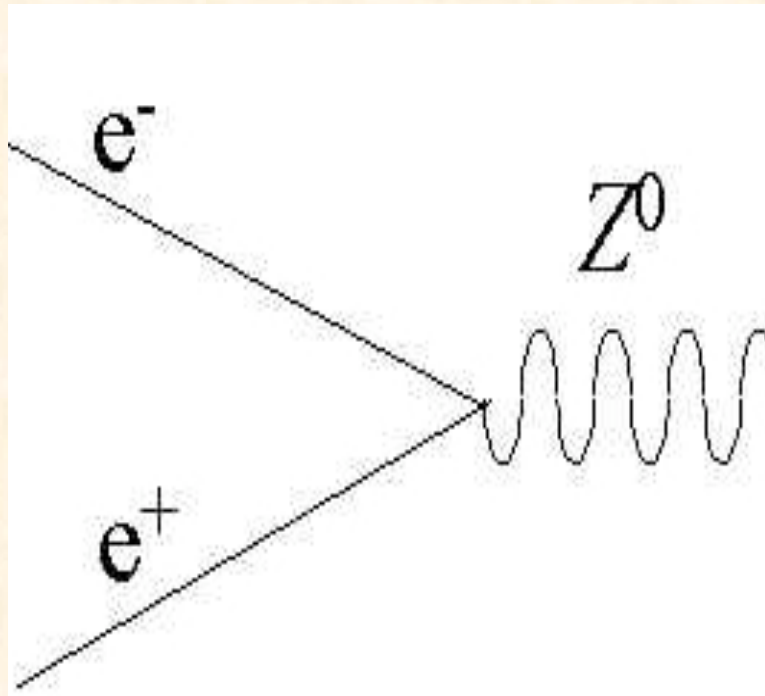
$$\frac{d\sigma}{dy_3 dy_4 d^2 p_T} = \frac{|M|^2 \delta(x_1 - \bar{x}_1) \delta(x_2 - \bar{x}_2)}{(2\pi)^2 4 x_1 x_2 S^2}$$

$$|M_T|^2 = \frac{32\pi}{9\sqrt{2}} \alpha_s G_F m_z^2 Q_{EW} \left( \frac{\hat{t}^2 + \hat{u}^2 + 2\hat{s} m_z^2}{\hat{t}\hat{u}} \right)$$

$$+(\hat{u} \rightarrow -\hat{s}, \hat{s} \rightarrow \hat{u})$$

- Consider both  $Z^0$ +jet and  $\gamma^*$ +jet (small correction)
- $Z^0$ +jet has small yield, but is excellent handle for jet energy loss

# From $Z^0$ to dileptons

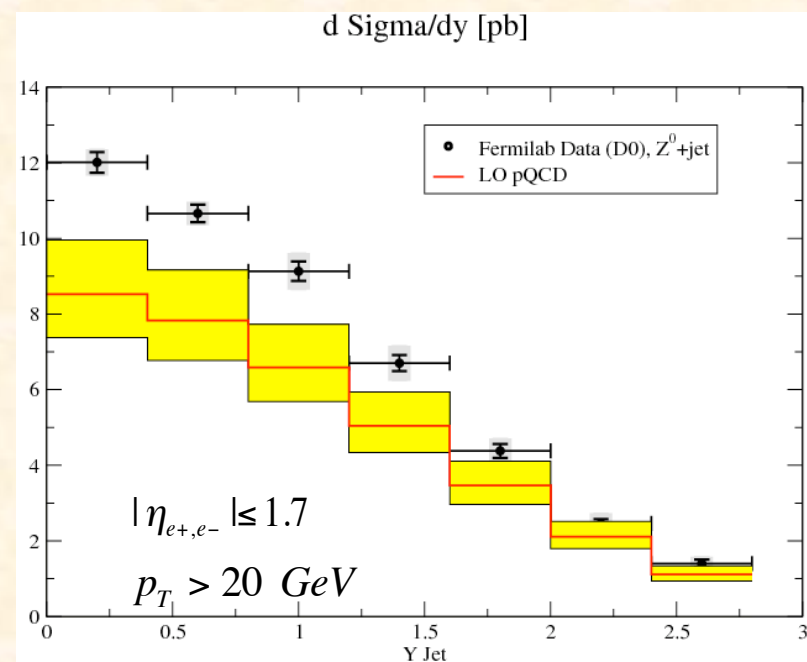
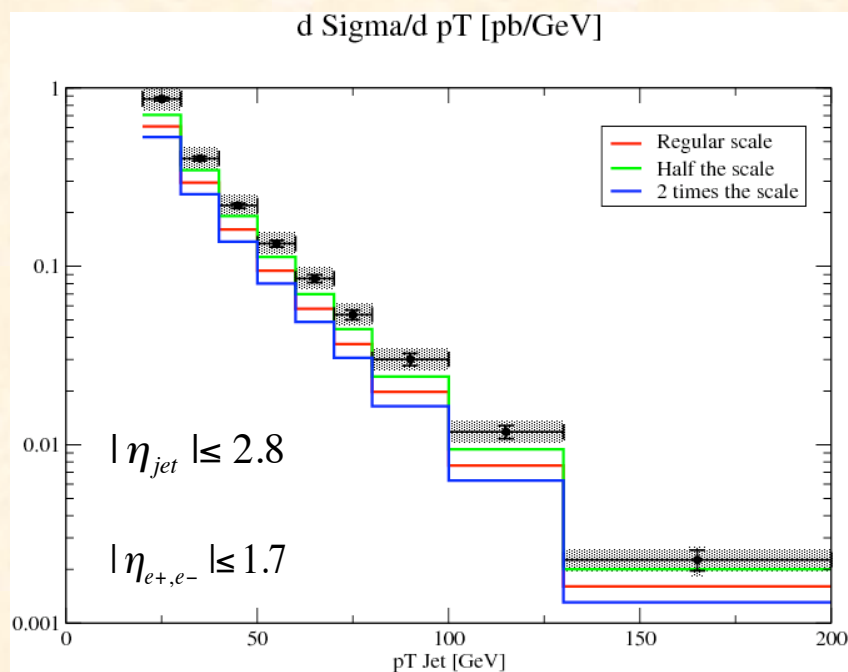


- Experimentally, dileptons are observed. We perform the decay by a Lorentz boost weighted with branching ratio.



# Comparison to Data

- $Z^0$ +jet measurements recently became available



- As expected within 30% - 50% of the data. Shape is reasonably well described, NLO in progress

# At LO, quenched cross section takes simple form, probes $P(\varepsilon)$ , $f$

$$\frac{d\sigma}{dy_3 dy_4 dp_T^3 dp_{TQ}^4} = P\left(\frac{1 - \frac{p_{TQ}^4}{p_T^4}}{1 - f}\right)_{q,g} \frac{|M|^2 \delta(x_1 - \bar{x}_1) \delta(x_2 - \bar{x}_2)}{(2\pi)^2 4 x_1 x_2 S^2 (1 - f)}$$

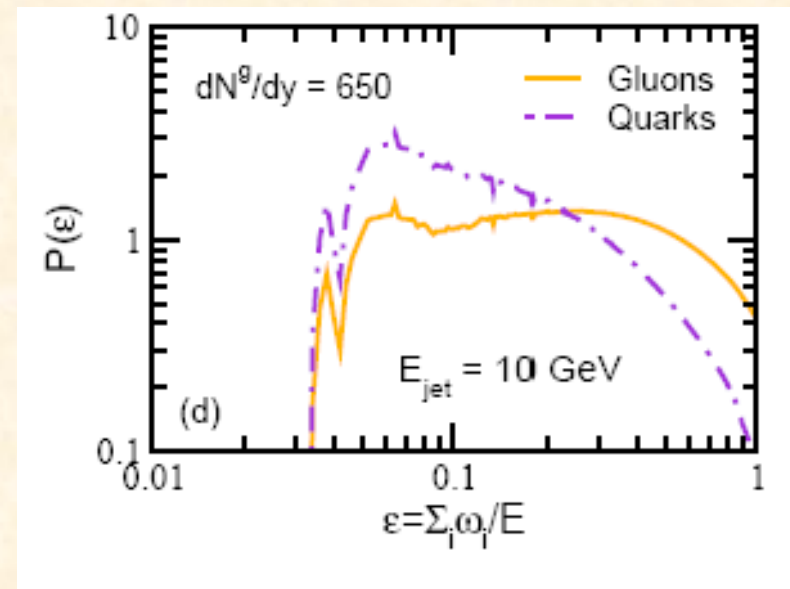
$$\varepsilon = \sum_{i=1}^n \frac{\omega_i}{E}, \quad P(\varepsilon) = \sum_0^\infty P_n(\varepsilon) \quad P_0(\varepsilon) = e^{-\langle N_g \rangle} \delta(\varepsilon)$$

$$P_1(\varepsilon) = \frac{dN}{d\varepsilon}(\varepsilon), \quad P_n(\varepsilon) = \frac{1}{n} \int_0^\varepsilon d\varepsilon' P_{n-1}(\varepsilon - \varepsilon') \frac{dN}{d\varepsilon}(\varepsilon')$$

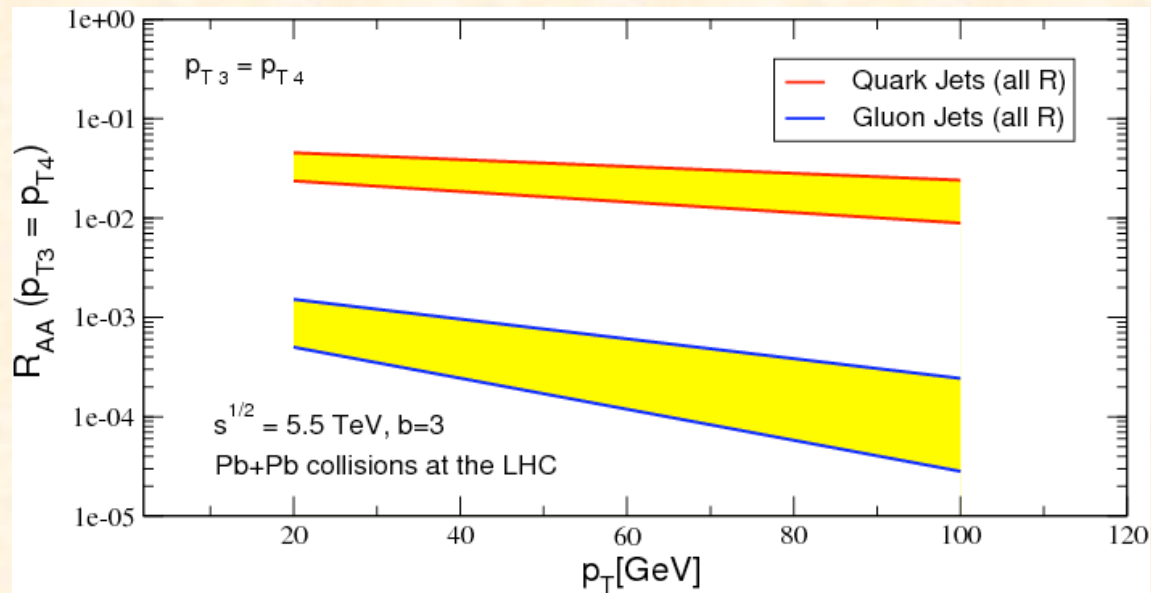
$$\int_0^1 d\varepsilon' P(\varepsilon') = 1, \quad \int_0^1 d\varepsilon' \varepsilon' P(\varepsilon') = \left\langle \frac{\Delta E}{E} \right\rangle$$

GLV, BDMPS (ASW)

## Example of probability density



# Obtaining the number of radiated gluons



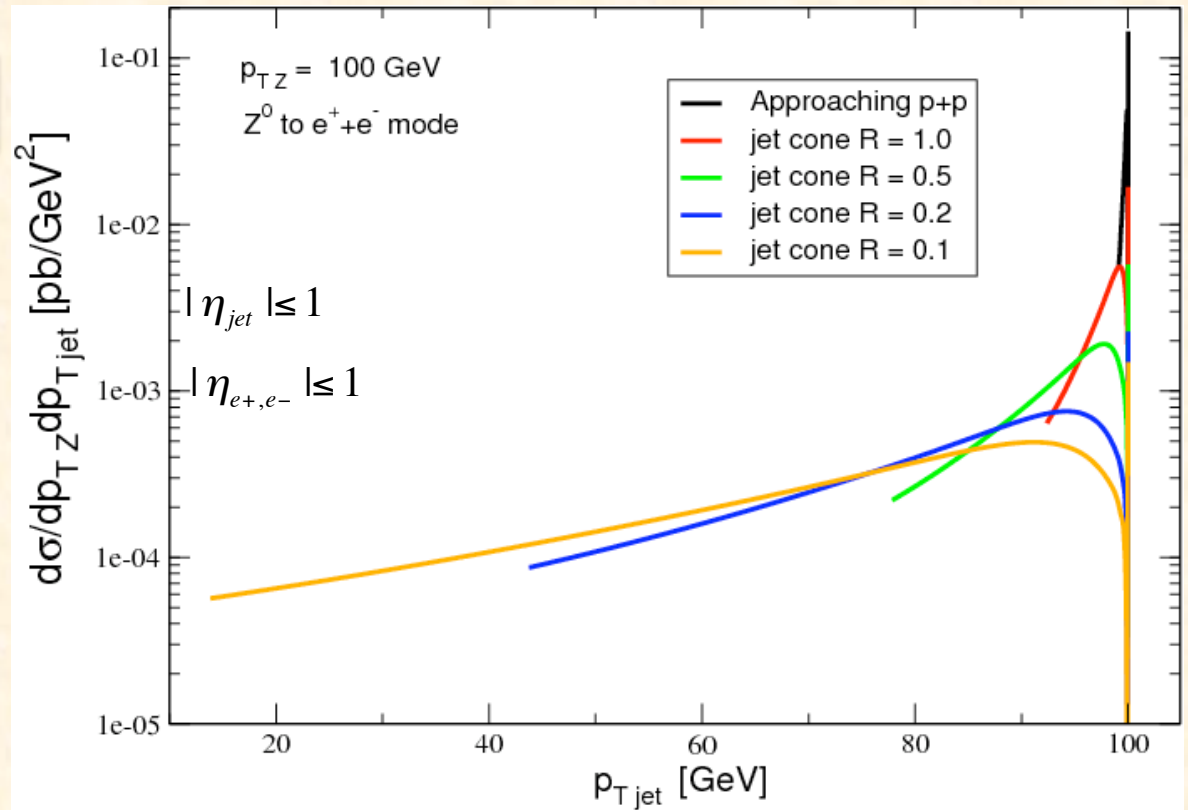
Constrain  $p_{T3} = p_{T4}$

$$\langle N^g \rangle = -\ln(R_{AA})$$

# The form of the quenched cross section

Consider  $p_{T \text{ jet}} < p_{T Z}$

$$\frac{d\sigma^{\text{Quench}}}{dy_Z dy_{\text{jet}} dp_{T Z} dp_{T \text{ jet}}} = \sum_{q,g} \frac{d\sigma^{\text{pp}}}{dy_Z dy_{\text{jet}} dp_{T Z}} \times \frac{1}{p_{T Z} (1 - f_{q,g})} \times P\left(\frac{1 - p_{T \text{ jet}} / p_{Z \text{ jet}}}{1 - f_{q,g}}\right)$$



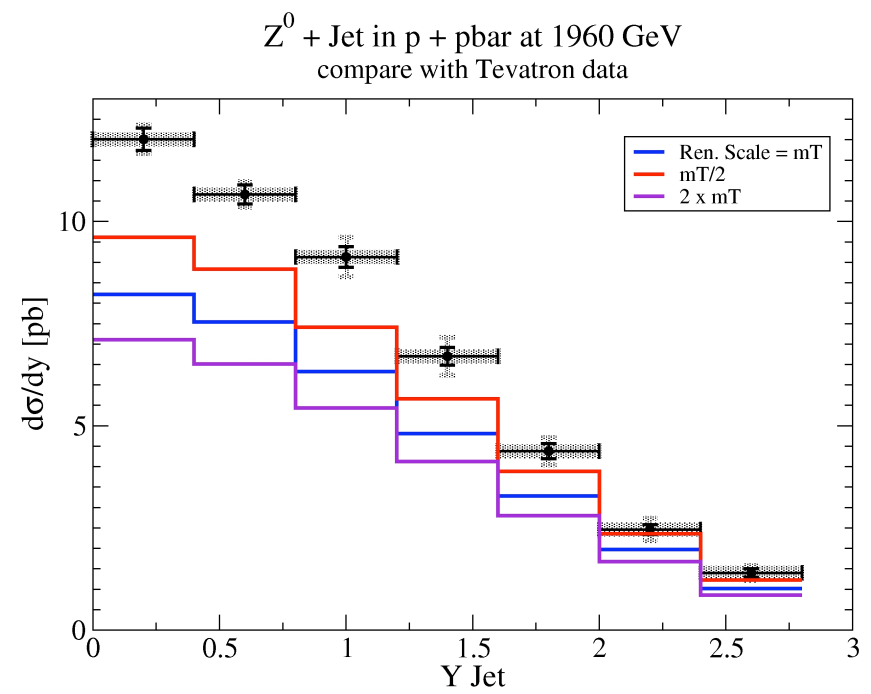
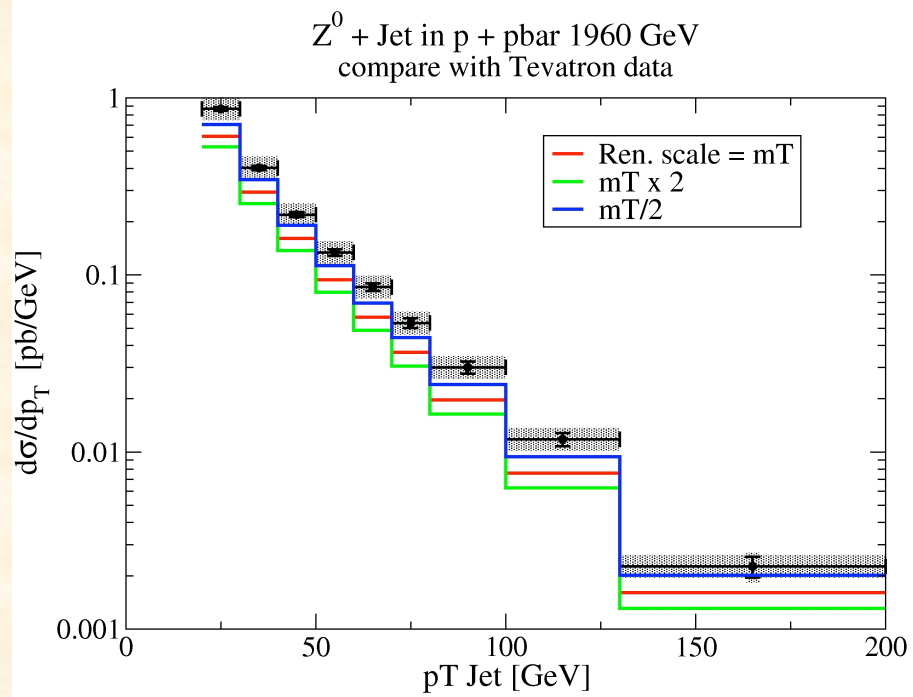
Neufeld, IV, Zhang (2010)

# Summary

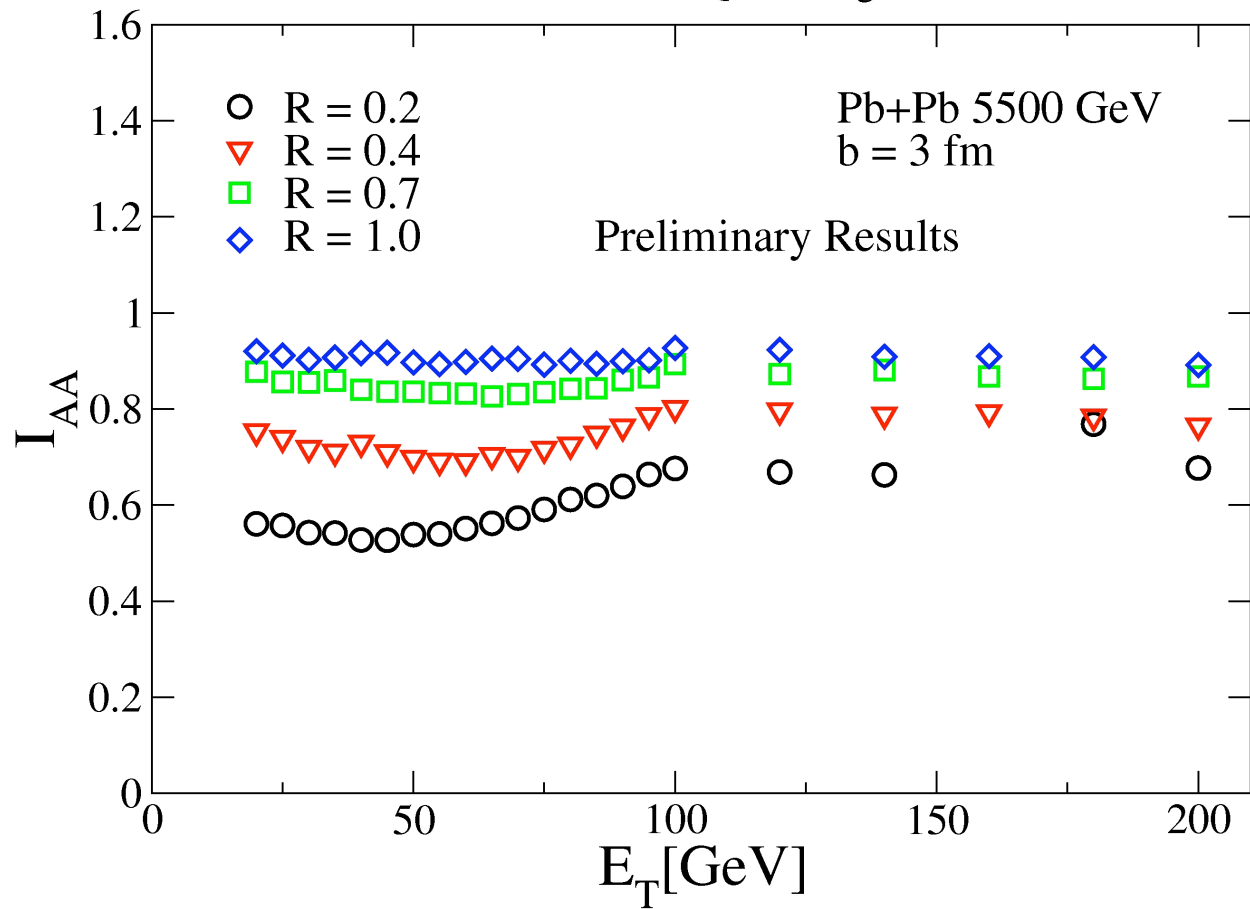
- Jet quenching is well established experimentally, however, leading particle suppression by itself provides incomplete information
- Jet shapes and jet cross sections may be able to distinguish between energy loss formalisms, determine fundamental properties of QGP
- The theory of jet shapes and jet cross sections in nuclear collisions has been developed by VWZ, and applied to inclusive jets at LHC
- Work now shifting to tagged jets, here presented preliminary results on  $Z^0$  tagged jets at LHC energies

# Backup





# $Z^0$ Tagged Jets at LHC with GLV Quenching



# What to use for the source term?

A common choice:

$$J^\nu(x) = \frac{dE}{dt} (1, \vec{u}) \delta(\vec{x} - \vec{u}t) ?$$

- Conserves energy and momentum globally (simply integrate the equation of motion over all space)
- Neglects local excitations, terms which integrate to zero globally

The linearized hydro equations couple to the source term, in turn yielding the particle emission spectrum

$$\delta\epsilon(\vec{k}, \omega) = \frac{ikJ_L(\vec{k}, \omega) + J^0(\vec{k}, \omega)(i\omega - \Gamma_s k^2)}{\omega^2 - c_s^2 k^2 + i\Gamma_s \omega k^2}$$

$$\vec{g}_L(\vec{k}, \omega) = \frac{i\omega \hat{k} J_L(\vec{k}, \omega) + ic_s^2 \vec{k} J^0(\vec{k}, \omega)}{\omega^2 - c_s^2 k^2 + i\Gamma_s \omega k^2}$$

$$\vec{g}_T(\vec{k}, \omega) = \frac{i\vec{J}_T(\vec{k}, \omega)}{\omega + \frac{3}{4}i\Gamma_s k^2}$$



$$\frac{dN}{dy d\phi}(y = 0) = \int_{p_T^i}^{p_T^f} dp_T p_T \int d\Sigma_\mu P^\mu (f(p) - f_{eq}(p))$$