Quantum Physics I PHY471, Fall 1999 Homework set 4 Due Monday, 9/27/1999

Please clearly state your assumptions, number the equations and indicate logical connections between different lines.

1. [2+2 pt] Gaussian wavepackets and expectation values Ohanian, #2.15, p. 55

2. [1+1+1+1 pt] Free particle with a wavefunction

Ohanian, #2.16, p. 55

3. [1+1+1+1+2+2 pt] Free particle with a different wavefunction

Consider the a wavefunction similar to the one in set 2, problem 2,

$$\Psi(x,0) = \begin{cases} A\cos bx \text{ for } |\mathbf{x}| < \frac{p}{2b} \\ 0 \text{ otherwise} \end{cases}$$

- a) Determine the constant *A* such that the wavefunction $\Psi(x,0)$ is normalized.
- b) What is the probability for finding the particle in the interval

$$-\frac{\mathbf{p}}{2b} \le x < 0 ?$$

- c) What is the momentum amplitude for the wavefunction?
- d) For what value of the momentum is the momentum probability maximum?
- e) What is the probability for finding the momentum in an interval dp around $\hbar b$?
- f) Evaluate the uncertainty Δx .
- g) Evaluate the uncertainty Δp .

4. [2 pt] Classical quantities in quantum mechanics: velocity and momentum

Ohanian, #2.23, p. 56