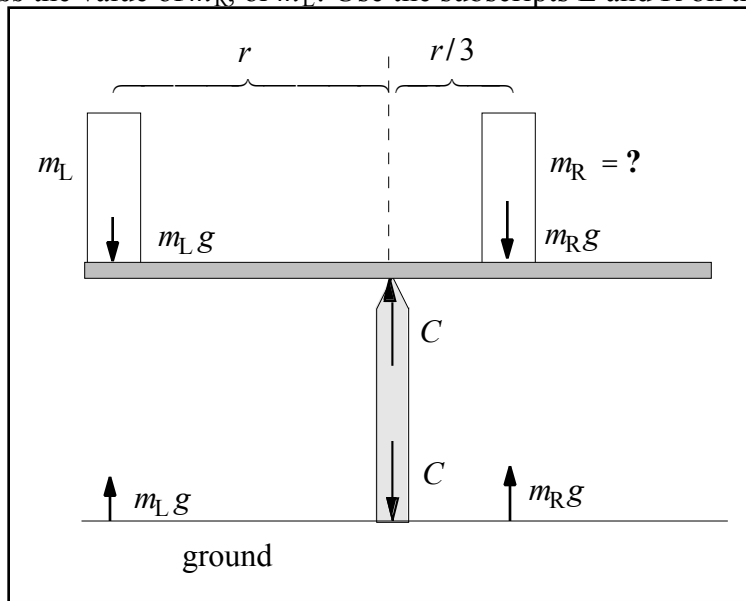


Homework 7

(Do not guess the value of m_R , or m_L ! Use the subscripts L and R on the masses)



1. The weights are $W_L = m_L g$ and $W_R = m_R g$
 2. The compression forces are $C_L = m_L g$ and $C_R = m_R g$ The directions (*are*) the same. The forces acting on the board and on the earth are drawn on the Figure.
 - 3 The force angles are 90°
 4. Magnitude of torques about the pivot point are: $\tau_L = m_L g r$ and, $\tau_R = m_R g r/3$
 5. The torque vectors try to rotate the board in the (*opposite*) directions
 6. Mass m_L generates the torque vector, $\tau_L = -m_L g r$
 7. Mass m_R generates the torque vector, $\tau_R = +m_R g r/3$
 8. Net torque vector, acting on the board, $\tau_{Net} = -m_L g r + m_R g r/3$
 9. The net torque on the board must be, $\tau_{Net} = 0$, if the board is balanced.
 - 10 The right mass, $m_R = 3m_L$

$$-m_L g r + m_R g r/3 = 0$$

$$m_R/3 = m_L$$

$$m_R = 3m_L$$
 11. The net force on the board must be, $F_{Net} = 0$, if it is balanced.
 12. The net force acting on the board, ($C_L = -m_L g$, $C_R = -m_R g = -3m_L g$)
$$F_{Net} = C_L + C_R + C = (-m_L g) + (-3m_L g) + (+C) = 0 \text{ (balanced)}$$
 13. The magnitude $C = 4m_L g$.
- The forces acting on the ground (*do*) balance
14. If the masses are hung from the board, the C's change to T's and nothing else.

Homework 7

15. The net force and net torque must be set equal to zero to determine the forces acting on a *balanced* beam

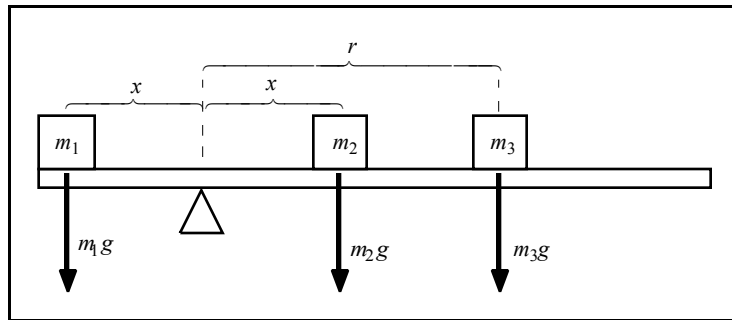


Figure for Problems 16-20: Three masses on a massless board.

16. The *force* vectors applied to the board are shown on the Figure and generate torques:

17 $\tau_1 = -m_1gx$, $\tau_2 = +m_2gx$, and , $\tau_3 = +m_3gr$ (+, clockwise)

18. Net torque vector $\tau_{\text{Net}} = \tau_1 + \tau_2 + \tau_3 = -m_1gx + m_2gx + m_3gr$

19. A balanced board has a net torque vector = 0 = $-m_1gx + m_2gx + m_3gr$

$$m_3gr = (m_1g - m_2g)x$$

$$r = [(m_1 - m_2) / m_3]x$$

20. The location, r , of m_3 that will balance the board is a) $r = [(m_1 - m_2) / m_3]x$

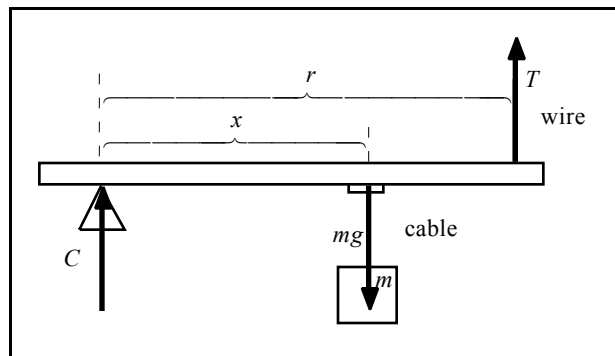


Figure for problems 22-25

21. $r = 10 \text{ m}$, $m = 100 \text{ kg}$, $x = 7 \text{ m}$,

(**C** at the pivot, **F** in the cable (use m), and **T** in the wire) are drawn on the Figure.

22. The torque *vectors* acting on the board are: $\tau_{\text{pivot}} = 0$, $\tau_{\text{cable}} = mgx$, $\tau_{\text{wire}} = -Tr$.

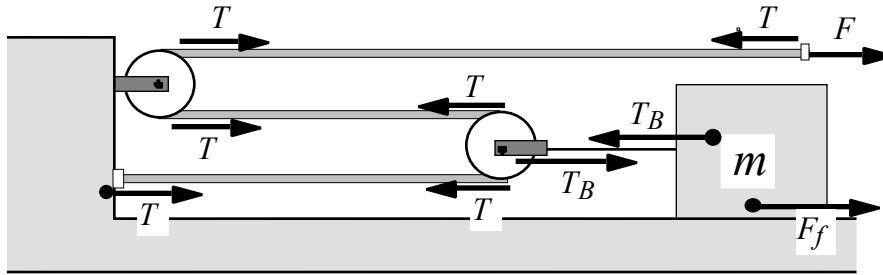
$$\tau_{\text{Net}} = mgx - Tr = 0 \quad \underline{T = mgx/r}$$

23. The tension in the wire is, $T = mgx/r = (100 \text{ kg})(10 \text{ N/kg})(7 \text{ m})/(10 \text{ m}) = \underline{700 \text{ N}}$

$$\mathbf{F}_{\text{Net}} = \mathbf{C} + \mathbf{T} + \mathbf{F} = (+C_{\text{pivot}}) + (+mgx/r) + (-mg) \quad C_{\text{pivot}} = mg(1 - x/r)$$

24. $C_{\text{pivot}} = mg(1 - x/r) = (1000 \text{ N})[1 - (7 \text{ m})/(10 \text{ m})] = (1000 \text{ N})(0.3) = \underline{300 \text{ N}}$

Homework 7



$$\underline{T = F} \quad (\text{balance at the handle})$$

$$T_B = 2T = 2F \quad (\text{balance at the pulley})$$

$$F_f = T_B = 2F \quad (\text{balance at the mass})$$

$$\underline{\mathbf{F}_f = +2F} \quad (\text{same direction as } \mathbf{F})$$

$$F_{wall} = 3T = 3F \quad (\text{same direction as } \mathbf{F})$$

$$\underline{\mathbf{F}_{wall} = +3F}$$

25. The tension in the rope is: a) F
26. The frictional force vector is: e) $\mathbf{F}_f = +2F$
27. The net rope force, \mathbf{F}_R , on the wall is: e) $\mathbf{F}_R = +3F$