

# Lecture 14

Chapter 28  
Circuits

# Chapter 27 Review

- Current,  $i$ , is defined as amount of charge  $q$  passing through plane in time  $t$

$$i = \frac{dq}{dt}$$

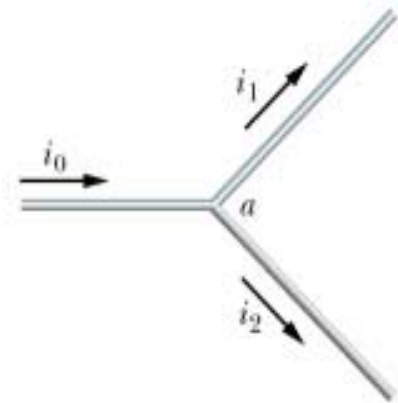
- SI unit ampere, A

$$1A = 1C/s$$

- Charge is conserved

$$i_0 = i_1 + i_2$$

- Current arrow drawn in direction + charge carriers would move



# Chapter 27 Review

- Resistance is defined as
- SI unit is the ohm,  $\Omega$

$$1\Omega = 1V / A$$

$$R = \frac{V}{i}$$

- Resistance of conducting wire of length  $L$ , resistivity  $\rho$ , and cross section  $A$

$$R = \rho \frac{L}{A}$$

- Ohm's Law –  $R$  is independent of magnitude and polarity of  $V$

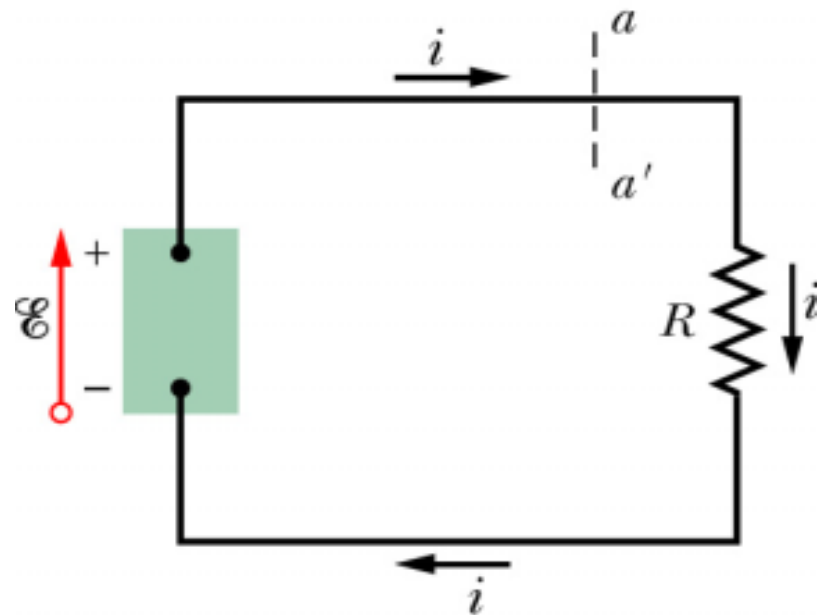
$$V = iR$$

# Circuits (1)

- To produce study flow of charge use an **emf device**
- Does work on charge carriers to maintain a  $V$  between its terminals
- Examples:
  - Battery
  - Electric generator
  - Solar cells

# Circuits (2)

- **emf device** label terminal at higher  $V$  as + and lower  $V$  as –
- Draw emf,  $\mathcal{E}$ , arrow from – to + terminal
- + charge carriers move against  $E$  field in emf device from lower (-) to higher (+)  $V$

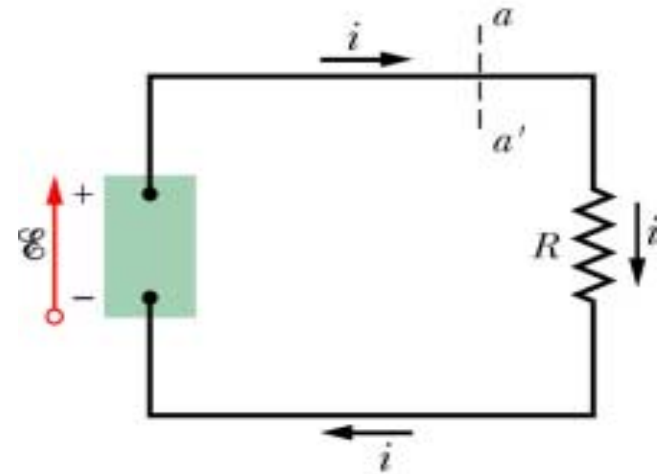


# Circuits (3)

- Must do work to move charges within emf device

$$W = q\Delta V$$

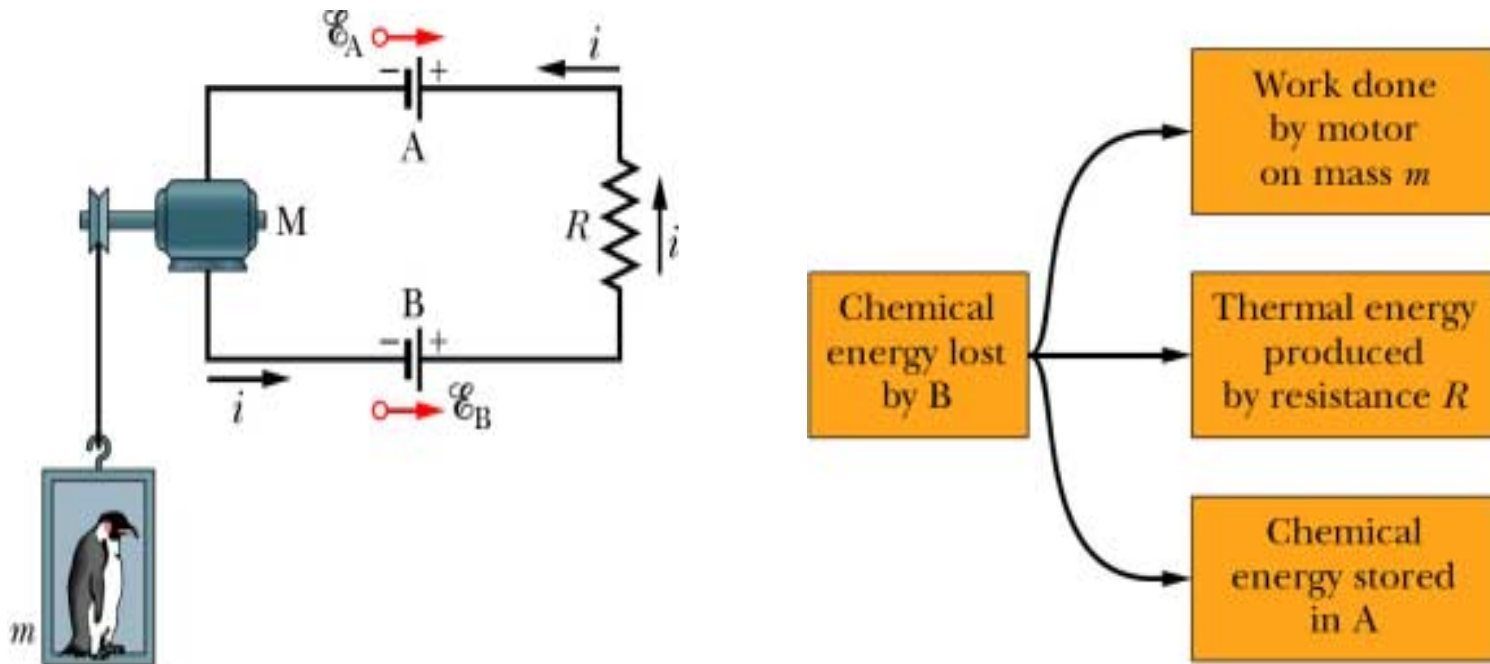
- The emf,  $\mathcal{E}$ , is the work per unit charge a device does to move + charge from low- $V$  terminal to high- $V$  terminal
- Energy source to do work may be chemical, mechanical, solar ...



$$\mathcal{E} = \frac{dW}{dq}$$

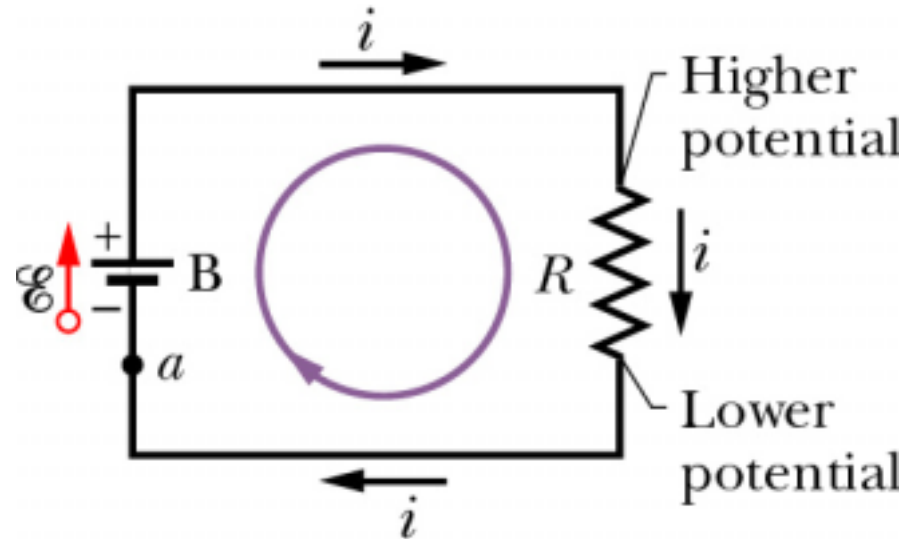
# Circuits (4)

- Emf device transfers energy to charge carriers moving through it
- This energy can be transferred to other devices such as a light bulb or motor



# Circuits (5)

- Calculate the current in single-loop circuit
- Use conservation of energy
- Chemical work done by battery must equal thermal energy dissipated in resistor
  - Assume wires negligible



$$W_{battery} = W_{resistor}$$

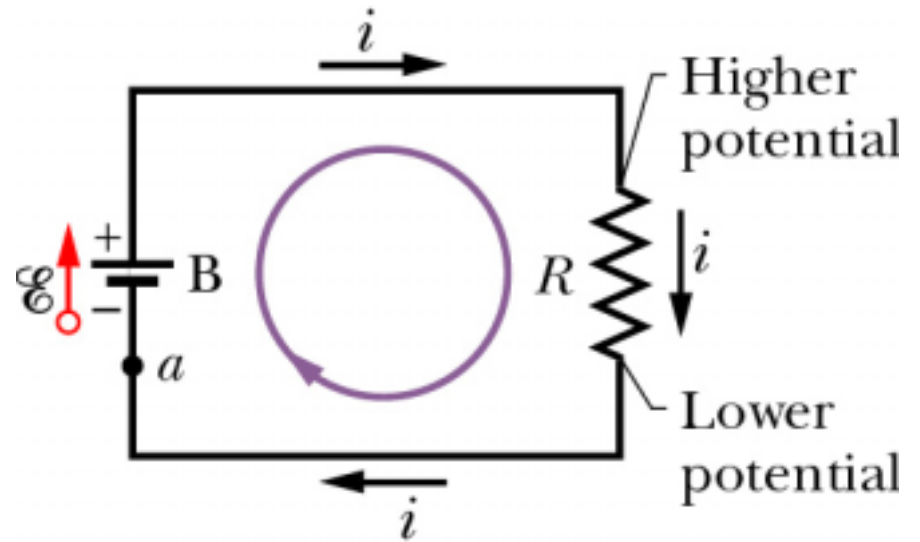


# Circuits (6)

- Start with energy lost in resistor

$$P = \frac{dW}{dt}$$

$$W = Pdt$$



- From chpt. 27 power for a resistor is

$$P = i^2 R$$

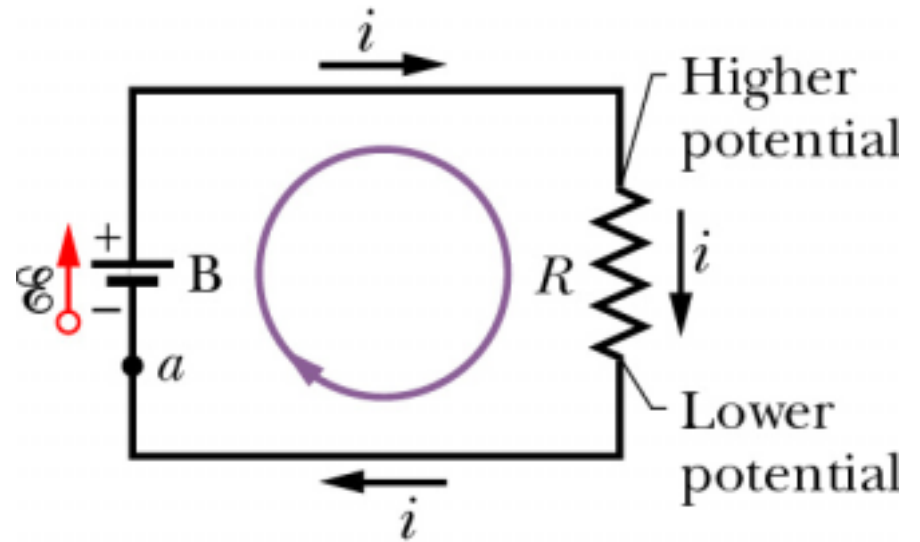
$$W_{resistor} = i^2 R dt$$

# Circuits (7)

- Work done by emf is

$$\mathcal{E} = \frac{dW}{dq}$$

$$W = \mathcal{E} dq$$



- Remember definition of current

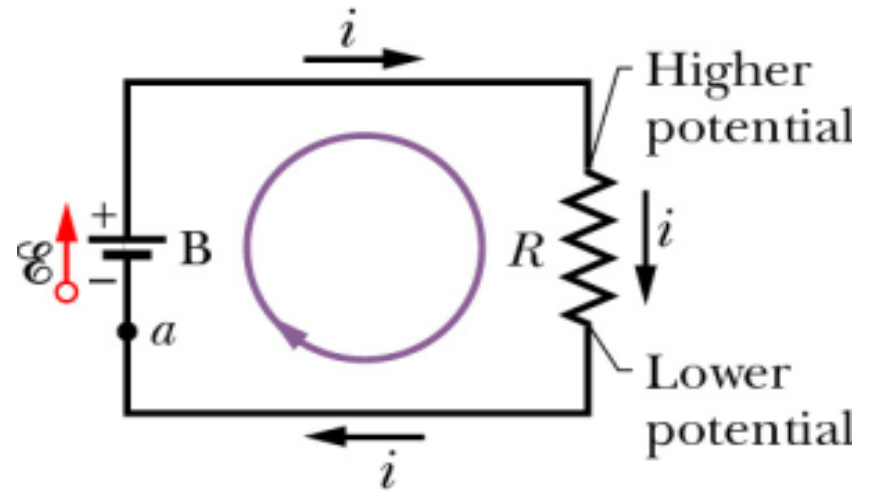
$$i = \frac{dq}{dt}$$

$$W_{battery} = \mathcal{E} i dt$$

# Circuits (8)

- By conservation of energy

$$W_{battery} = W_{resistor}$$



$$W_{resistor} = i^2 R dt$$

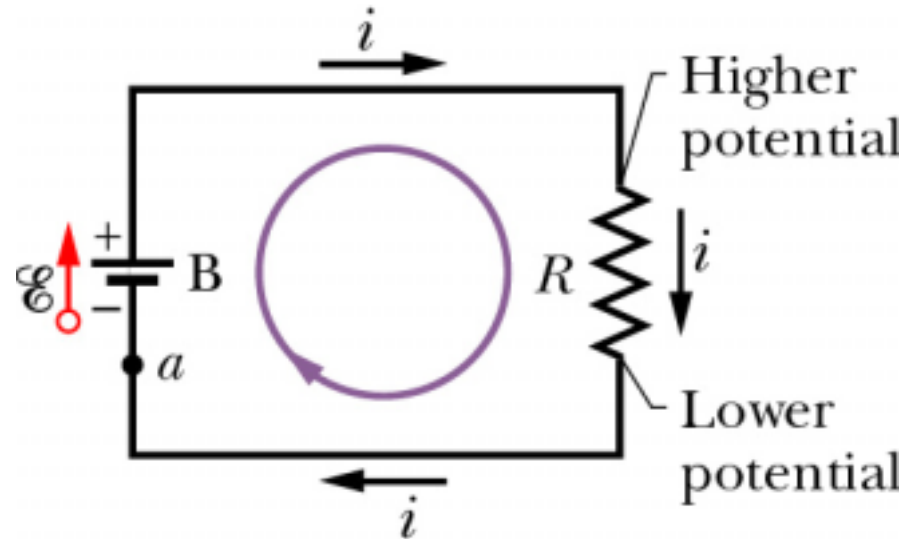
$$W_{battery} = \mathcal{E} i dt$$

- Solving gives

$$\mathcal{E} = iR$$

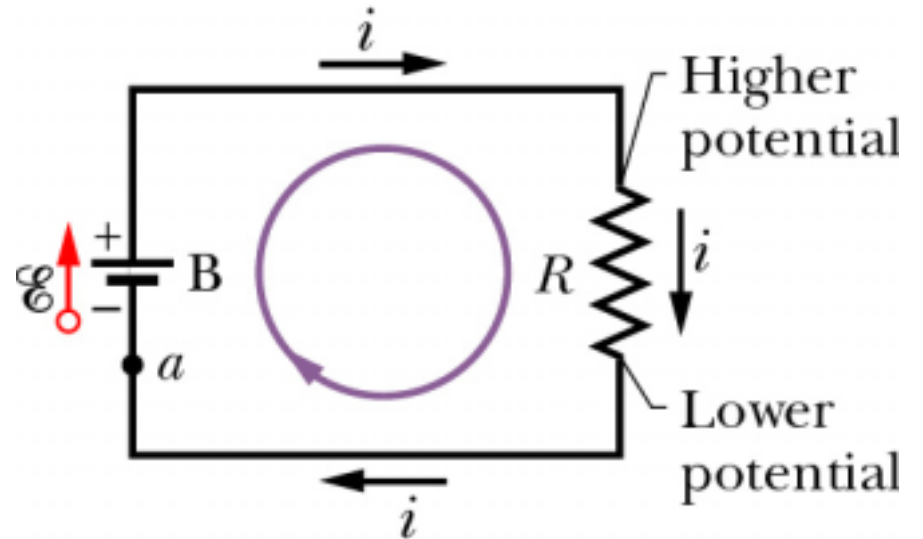
# Circuits (9)

- Calculate the current in single-loop circuit
- Now use potential method
- Travel around circuit in either direction and algebraically add potential differences



# Circuits (10)

- Start at point  $a$  with potential  $V_a$
- Move clockwise around circuit
- Pass through battery moving to higher  $V$ , change in  $V$  is  $+\mathcal{E}$
- Neglect resistance of connecting wires



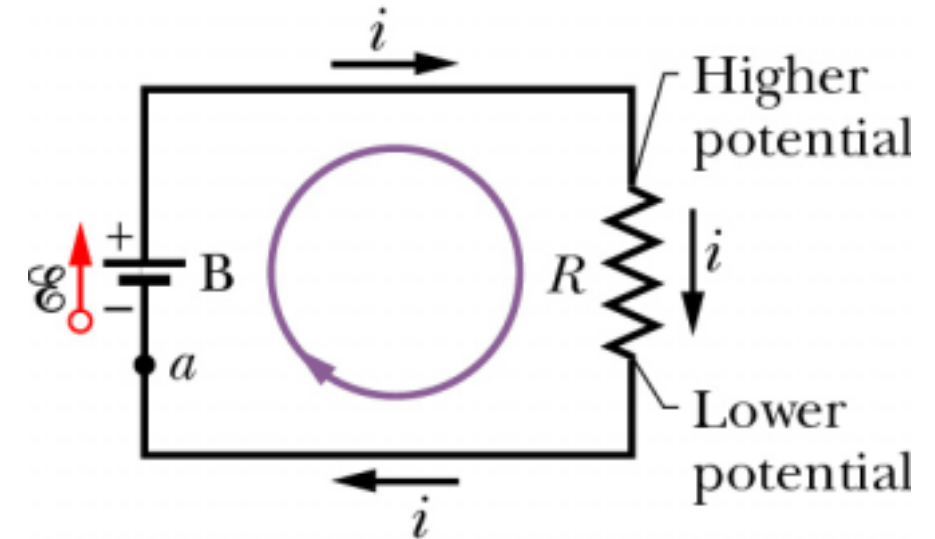
$$V_a + \mathcal{E}$$

# Circuits (11)

- Top of resistor at same  $V$  as battery
- Pass through resistor  $V$  decreases and

$$V = iR$$

- Return to point  $a$  on bottom wire back to potential  $V_a$  so



$$V_a + \mathcal{E} - iR = V_a$$

# Circuits (12)

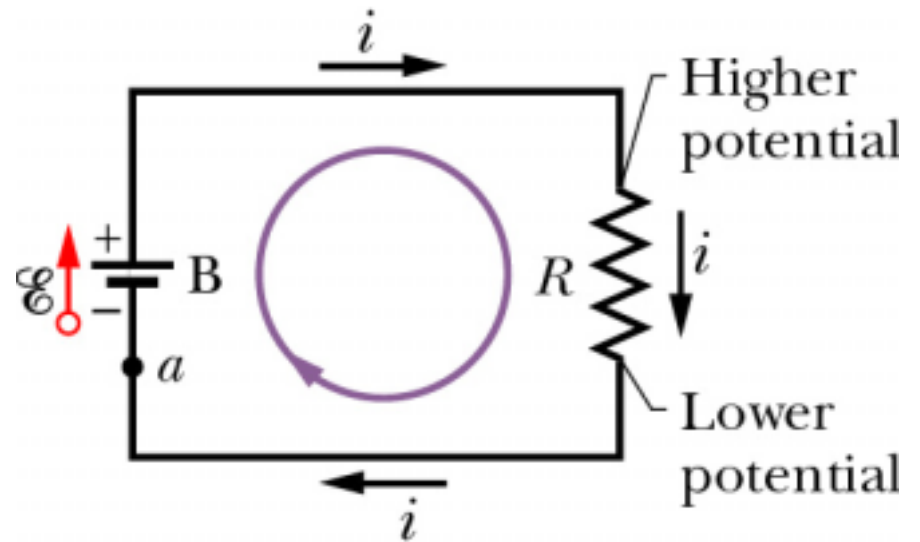
- Get same answer as before

$$\mathcal{E} = iR$$

- Could move around circuit counterclockwise

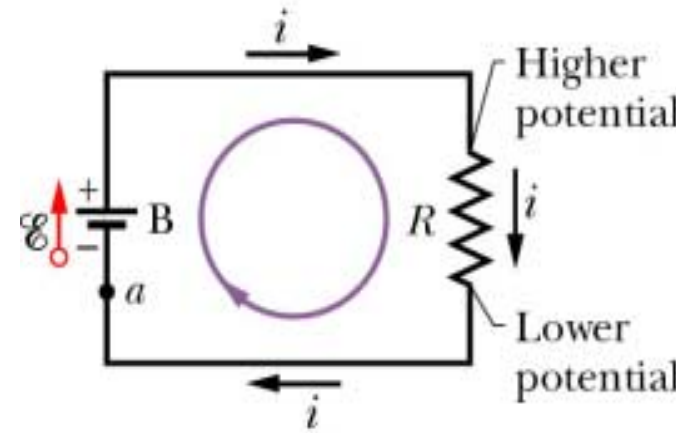
$$V_a - \mathcal{E} + iR = V_a$$

$$\mathcal{E} = iR$$



# Circuits (13)

- **Kirchhoff's loop rule** – in traversing a circuit loop the sum of the changes in  $V$  is zero,  $\Delta V = 0$
- **Resistance rule** – Move through resistor in direction of current  $V = -iR$ , in opposite direction  $V = +iR$
- **Emf rule** – Move through emf device in direction of emf arrow  $V = +E$ , in opposite direction  $V = -E$





# Circuits (14)

- Checkpoint #1 –
- A) What direction should the emf arrow point?

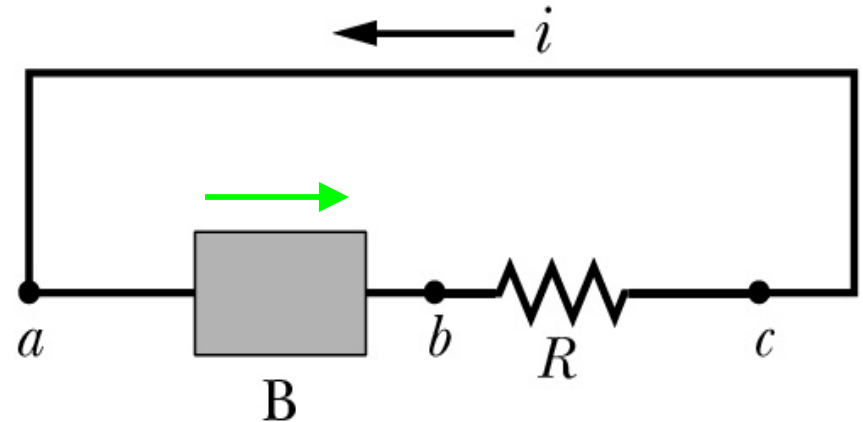
RIGHTWARD

- B) Rank magnitude of current at points a, b, and c.

All same

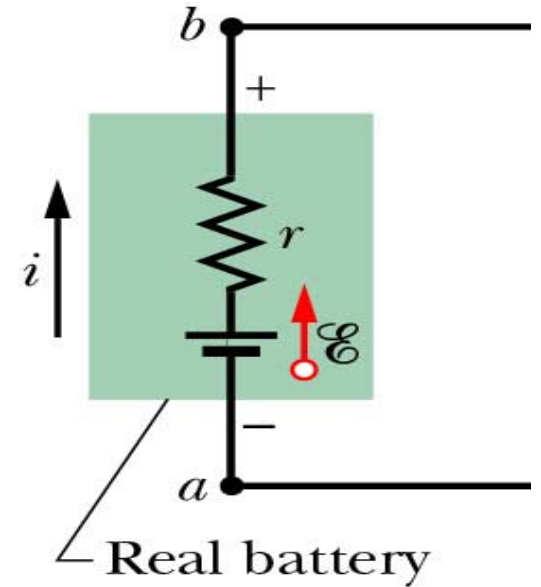
- C) Rank V and U.

B, then A and C tie



# Circuits (15)

- So far assumed **ideal battery** – has no internal resistance
- **Real battery** has internal resistance to movement of charge
- Not in circuit  $V = \mathcal{E}$  of battery
- If current present  $V = \mathcal{E} - iR$ , where  $R$  is the internal resistance of the battery



# Circuits (16)

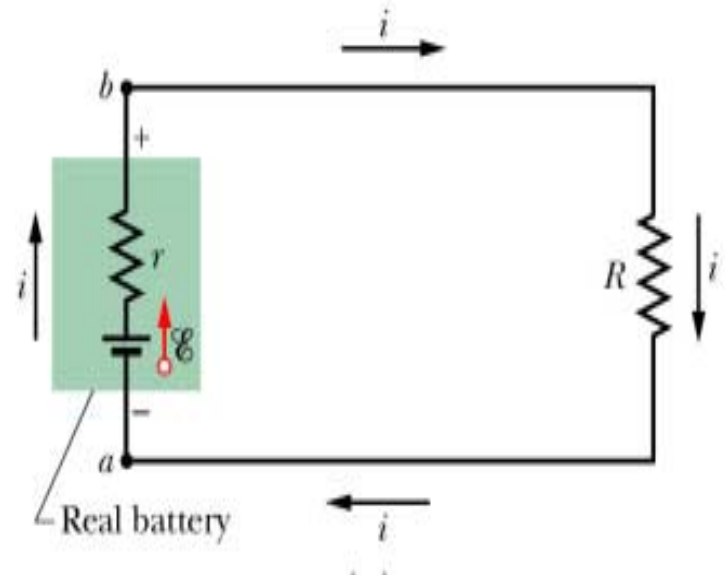
- Put **real** battery in circuit
- Using Kirchhoff's loop rule and starting at point a gives

$$\mathcal{E} - ir - iR = 0$$

$$\mathcal{E} = i(r + R)$$

- For ideal battery,  $r = 0$  and we get same as before

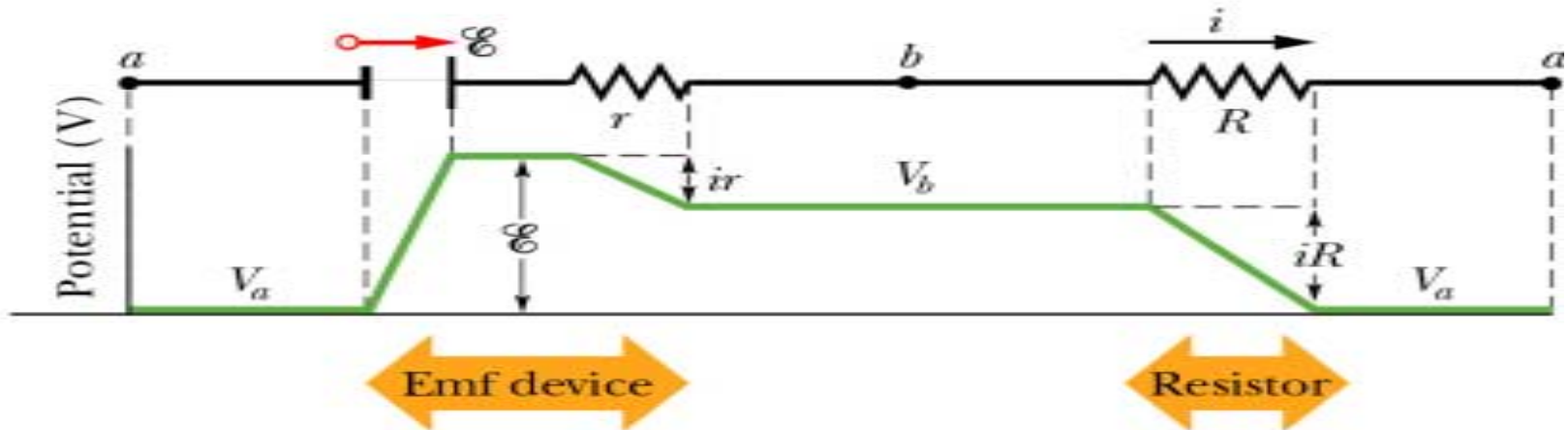
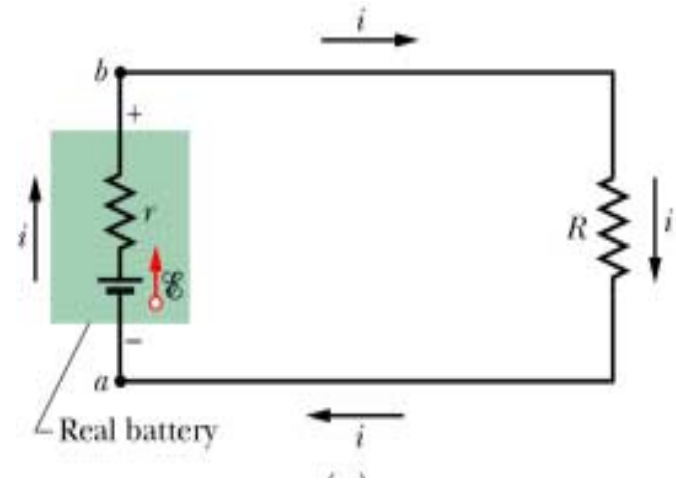
$$\mathcal{E} = iR$$



# Circuits (17)

- Can represent changes in potential graphically

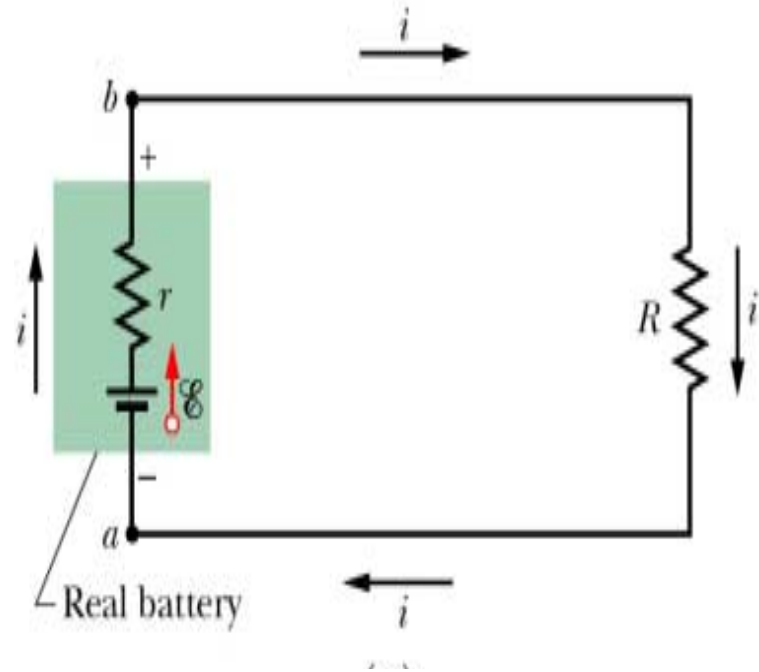
$$\mathcal{E} - ir - iR = 0$$



(b)

# Circuits (18)

- What is the potential difference,  $V$ , between points  $a$  and  $b$ ?
- To find  $V$  between any 2 points in circuit
  - Start at one point and traverse circuit to other following any path
  - Add changes in  $V$  algebraically



# Circuits (19)

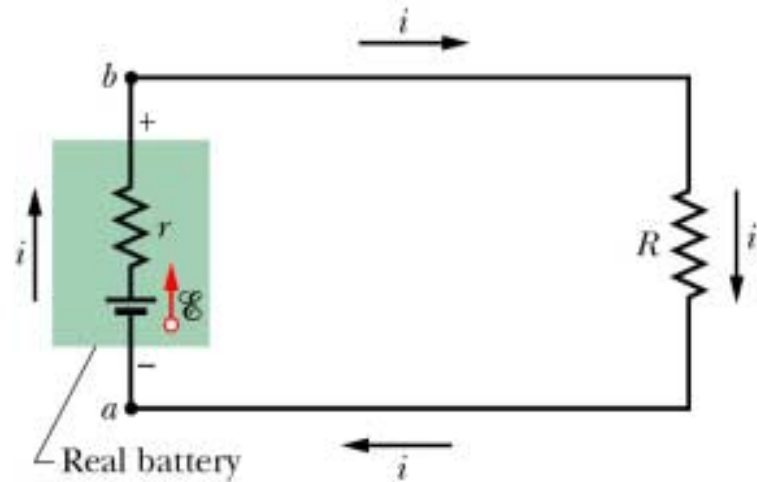
- Moving from b to a clockwise gives

$$V_b - iR = V_a$$

$$V_b - V_a = iR$$

- From loop rule know

$$\mathcal{E} - ir - iR = 0$$

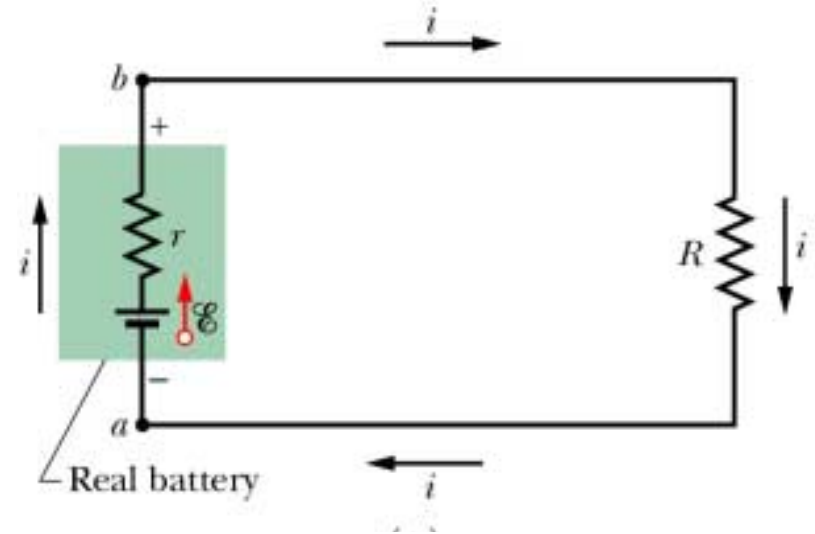


$$i = \frac{\mathcal{E}}{r + R}$$

# Circuits (20)

$$V_b - V_a = iR$$

$$i = \frac{\mathcal{E}}{r + R}$$



- Substituting for  $i$  gives

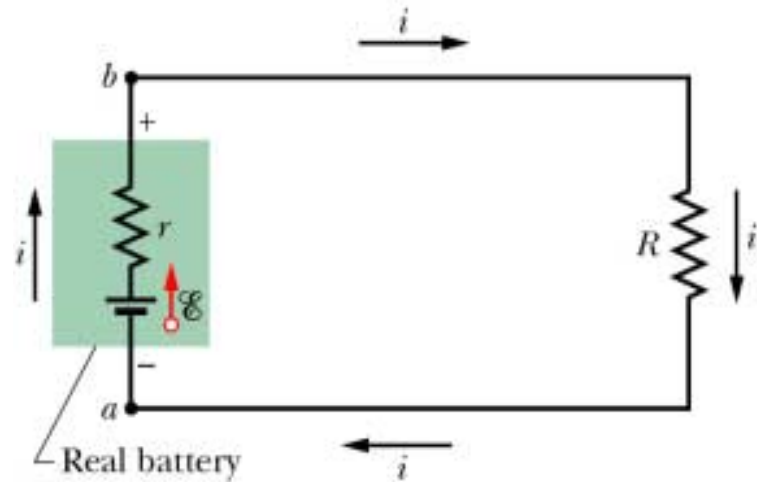
$$V_b - V_a = \mathcal{E} \frac{R}{R + r}$$

# Circuits (21)

- Now move from b to a counterclockwise

$$V_b + ir - \mathcal{E} = V_a$$

$$V_b - V_a = \mathcal{E} - ir$$



- Substituting  $i$  from loop rule

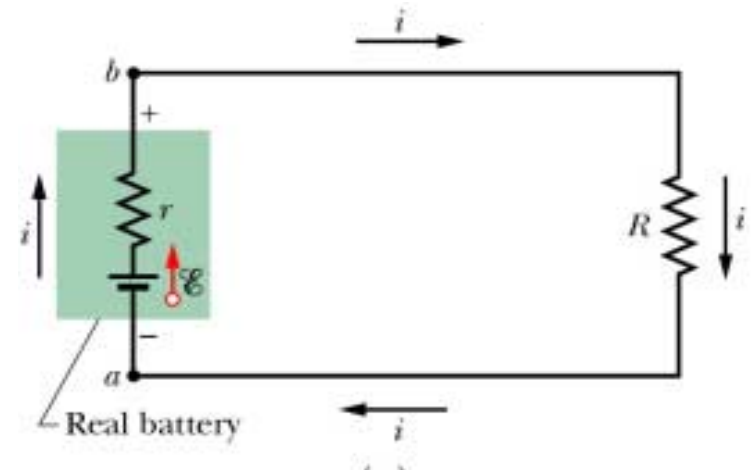
$$i = \frac{\mathcal{E}}{r + R}$$

$$V_b - V_a = \mathcal{E} \frac{R}{R + r}$$



# Circuits (22)

- Suppose  $\mathcal{E} = 12\text{V}$ ,  $R=10\ \Omega$  and  $r=2\ \Omega$
- Potential across battery's terminals is



$$V_b - V_a = \mathcal{E} \frac{R}{R+r} = (12\text{V}) \frac{10\ \Omega}{10\ \Omega + 2\ \Omega} = 10\text{V}$$

- $V$  across terminals only equal to  $\mathcal{E}$  if no internal resistance ( $r=0$ ) or no current ( $i=0$ )

# Circuits (23)

- A real battery transfers energy to
  - Charge carriers through a chemical reaction
  - Thermal energy due to internal resistance (called resistive dissipation)
- Net energy transfer or power from an emf device to charge carriers is
  - Where  $V$  is across terminals

$$P = iV$$

# Circuits (24)

- For real battery just found

$$V_b - V_a = \mathcal{E} - ir$$

- Substituting gives:

$$P = iV = i(\mathcal{E} - ir) = i\mathcal{E} - i^2 r$$

Internal dissipation rate,  $P_r$

$$P_r = i^2 r$$

Power of emf device,  $P_{emf}$

$$P_{emf} = i\mathcal{E}$$