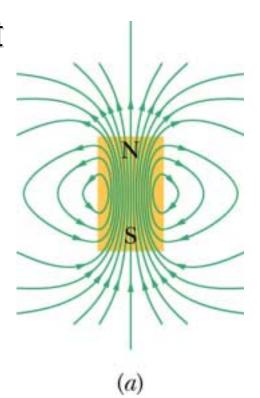
#### October 6th

Magnetic Fields - Chapter 29

 Analogous to electric field, a magnet produces a magnetic field, B

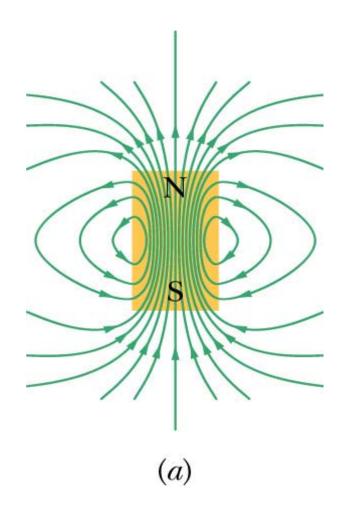
- Set up a B field two ways:
- Moving electrically charged particles
  - Current in a wire
- Intrinsic magnetic field
  - Basic characteristic of elementary particles such as an electron



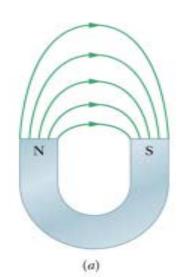
Magnetic field lines

 Direction of tangent to field line gives direction of B at that point

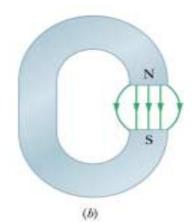
 Denser the lines the stronger the B field



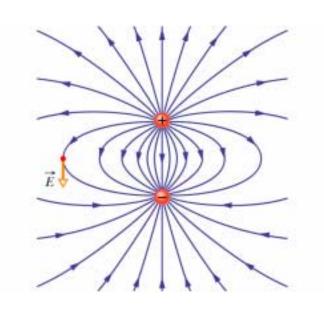
 Magnetic field lines enter one end (south) of magnet and exit the other end (north)

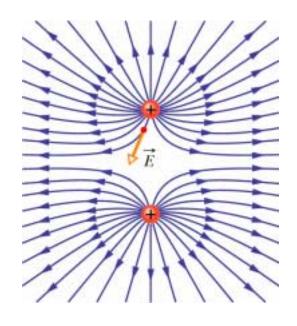


- Opposite magnetic poles attract
- like magnetic poles repel

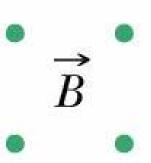


# Like the electric field lines, but there are no "magnetic charges"





#### Magnetic fields

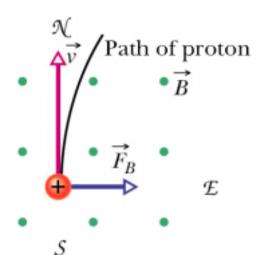


This shows the tips of magnetic field vector lines (green) pointed out of the screen (towards you).

$$\times \overrightarrow{B} \times$$

This shows the tails of magnetic field vector lines (black) pointed into the screen (away from you).

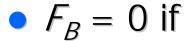
- When charged particle moves through B field, a force acts on the particle
  - $F_B = q\vec{v} \times B$



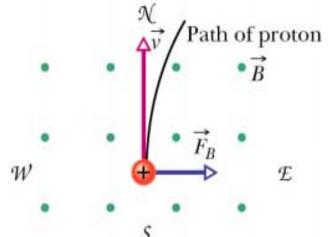
- Magnitude of  $F_B$  is  $F_B = |q| v B \sin \phi$
- where  $\phi$  is the angle between  $\nu$  and B
- SI unit for B is tesla, T

$$1T = 1 \frac{N}{C \cdot m/s} = 1 \frac{N}{A \cdot m}$$

$$\vec{F}_B = q\vec{v} \times \vec{B} = qvB\sin\phi$$

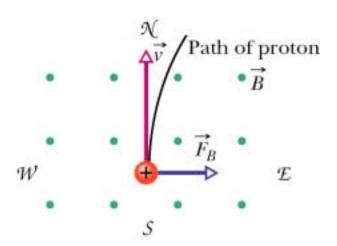


- Charge, q = 0
- Particle is stationary
- $\nu$  and B are parallel ( $\phi$ =0) or anti-parallel ( $\phi$ =180)
- $\bullet$   $F_B$  is maximum if
  - $\nu$  and B are  $\perp$  to each other



$$\vec{F}_B = q\vec{v} \times \vec{B}$$

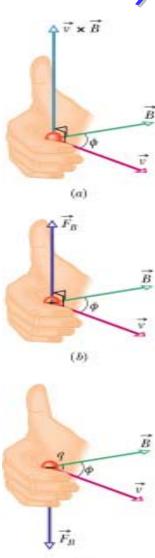
•  $F_B$  acting on charged particle is always  $\bot$  to  $\lor$  and B



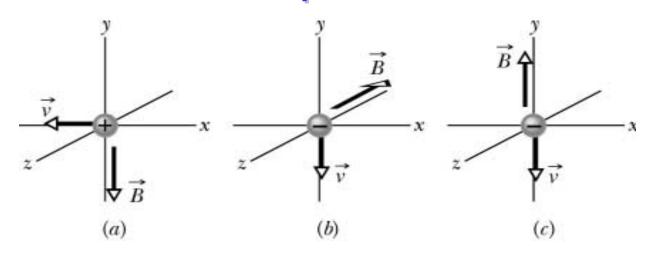
- $F_B$  never has component || to  $\nu$
- $F_B$  cannot change  $\nu$  or K.E. of particle
- $F_B$  can only change direction of  $\nu$

• Right-hand rule – For positive charges - when the fingers sweep  $\nu$  into B through the smaller angle  $\phi$  the thumb will be pointing in the direction of  $F_B$ 

• For negative charges  $F_B$  points in opposite direction



#### Checkpoint #1

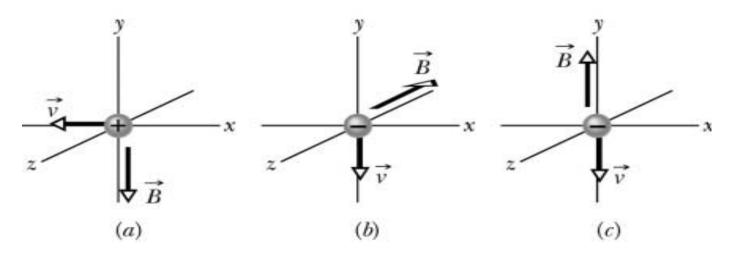


- What is the direction of  $F_B$  on the particle with the  $\nu$  and B shown?
- Use right-hand rule don't forget charge

$$A) + Z$$

$$\vec{F}_{B} = q\vec{v} \times \vec{B}$$

#### Magnetic Fields



- Check yourself using matrix notation
- Write vectors for v and B

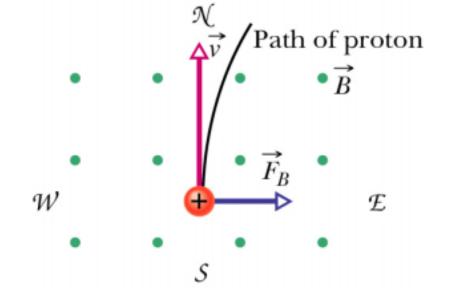
$$\vec{a} \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix} = (a_y b_z - b_y a_z) \hat{i} - (a_x b_z - b_x a_z) \hat{j} + (a_x b_y - b_x a_y) \hat{k}$$

#### Sample Problem 29-1

$$\vec{F}_B = q\vec{v} \times \vec{B}$$

- B = 1.2 mT
- $KE_{proton} = 5.3 \text{ MeV}$
- $m_p = 1.67 \times 10^{-27} \text{ kg}$
- Find F<sub>B</sub> (magnitude and direction)
- Find acceleration

$$KE = \frac{1}{2}mv^2$$
 
$$F = ma$$



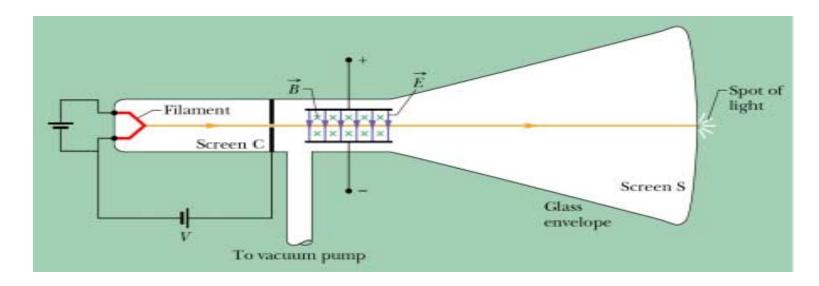
$$F = ma$$

#### Magnetic Fields

 What happens if there is both an E field and a B field?

 Both fields produce a force on a charged particle

 If the two fields are ⊥ to each other call them crossed fields



- Cathode ray tube used in television
- Can deflect a beam of electrons by
  - E field from charged parallel-plates
  - B field from magnet
- Adjust E and B fields to move electron beam across fluorescent screen

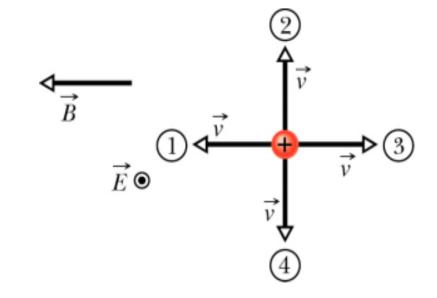
#### Checkpoint #2

- E field out of page, B field to left
- A) Rank 1,2, and 3 by magnitude of net F
  on particle, greatest first
- What direction is  $F_E$  for 1?

#### Out of page

 Is it the same for all directions of v?

YES



#### Checkpoint #2

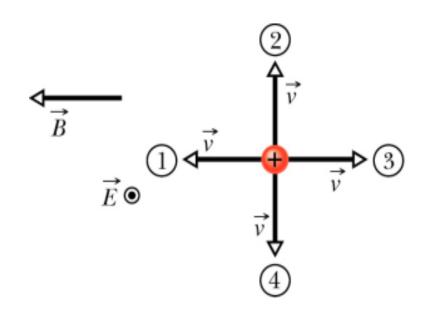
• What is direction of  $F_B$  for 1,2,3 and 4?

1) 
$$F_B = 0$$

2) F<sub>B</sub> out of page

3) 
$$F_{B} = 0$$

4) F<sub>B</sub> into page



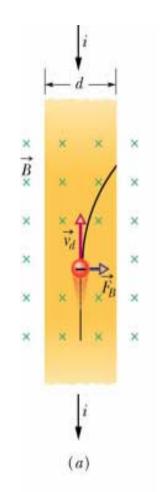
A) Rank magnitude of net F for 1, 2 and 3.

2, then 1 & 3 tie

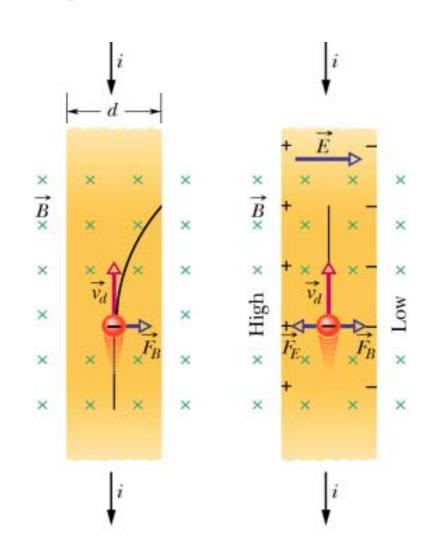
B) Which direction could have net F of zero?

Direction 4

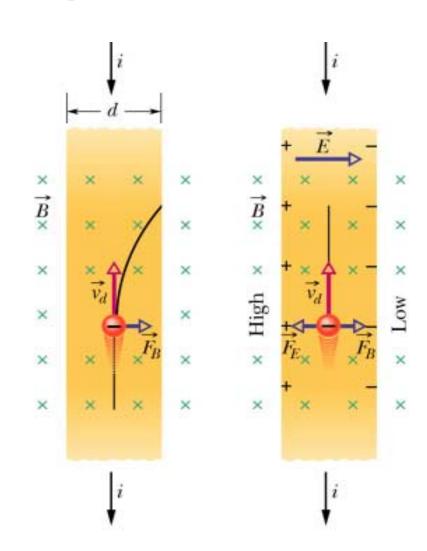
- Electrons moving in a wire. In this case the wire is a rectangular slab with width, d, and thickness, l.
- The total cross sectional area of the wire is A=I d.
- B field points into the screen.



- Electrons moving in a wire (= current) can be deflected by a B field called the Hall effect
- Creates a Hall potential difference, V, across the wire
- Can measure the wire's charge density when at equilibrium  $F_E = F_B$



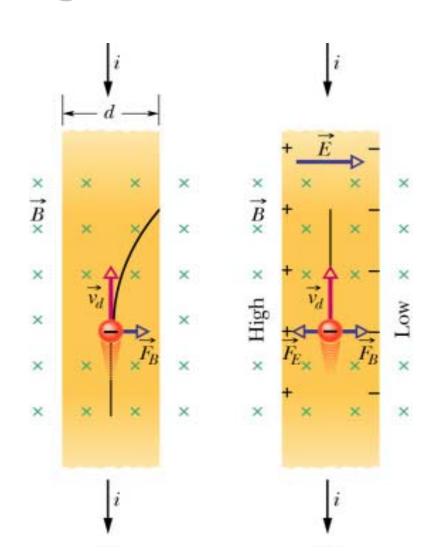
- Electrons have drift velocity, V<sub>d</sub> in direction opposite the current, i
- B field into page causes force,  $F_B$  to right
- Electrons pile up on right hand side of strip
- Leaves + charges on left and produce an E field inside the strip pointing to right



- E field on electron produces a  $F_E$  to the left
- Quickly have equilibrium where  $F_F = F_B$
- E field gives a V across the strip

$$V = Ed$$

 Left side is at a higher potential



 Can measure the number of charge carriers per unit volume, *n*, at equilibrium

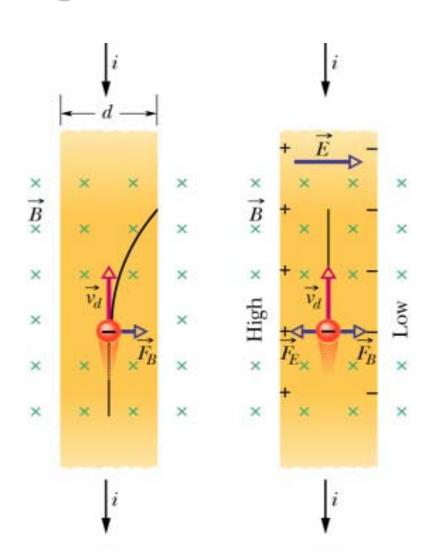
$$F_E = F_B$$

$$F_E = qE$$

$$F_E = qE \quad F_B = |q\vec{v} \times \vec{B}|$$

$$eE = ev_d B \sin(90)$$

$$E = v_d B$$

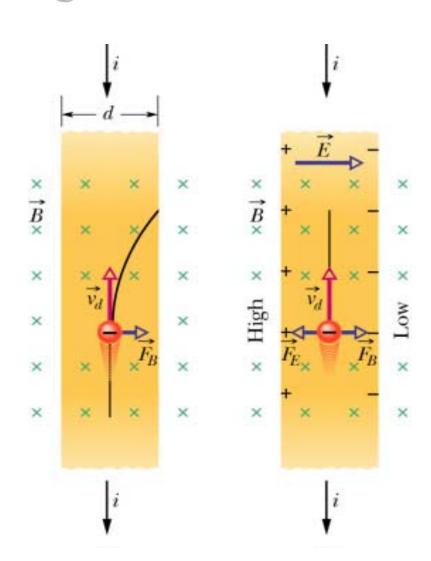


 Remember from Chpt. 27 that drift speed is

$$v_d = \frac{J}{ne} = \frac{i}{neA}$$

$$E = v_d B = \frac{iB}{neA}$$

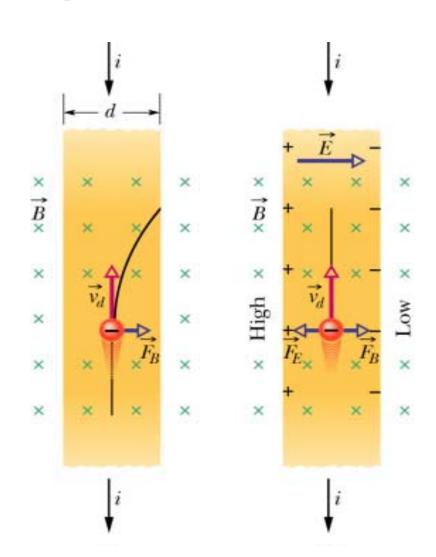
$$n = \frac{iB}{EeA}$$



Replacing E by

$$V = Ed$$

$$n = \frac{iB}{EeA} = \frac{iBd}{VeA}$$



If / is the thickness of the strip

$$l = \frac{A}{d}$$

Finally get

$$n = \frac{iB}{Vle}$$

