# **Review for Midterm-1**

# Midterm-1

- Wednesday Sept. 24th at 6pm
  - Section 1 (the 4:10pm class) exam in BCC N130 (Business College)
  - Section 2 (the 6:00pm class) exam in NR 158 (Natural Resources)
- Allowed one sheet of notes (both sides) and calculator
- Need photo ID
- Send Prof. Tollefson email if you need to take the make-up exam and explain why (tollefson@pa.msu.edu)
  - Make-up exam is at 8am Thursday (meet at 3234 BPS by 7:55am)
- Use the help-room to prepare
- Review in class on Tuesday



## **Electric Force**

 The magnitude of the electrostatic force, F, between 2 charged particles with charges q<sub>1</sub> and q<sub>2</sub>, respectively, and separated by a distance r is defined as

$$F = \frac{k |q_1| ||q_2|}{r^2} \qquad k = \frac{1}{4\pi\varepsilon_0} = 8.99 \times 10^9 N \cdot m^2 / C^2$$

- This is Coulomb's law where *k* is a constant
- The forces on 2 point charges are equal and opposite, pointing to (away from) the other particle for unlike (like) charges

## **Electric Field**

 Electric field, *E*, is the force per unit positive test charge



• For a point charge

$$F = k \frac{|q_0||q|}{r^2} \quad \text{so} \quad E = k \frac{|q|}{r^2}$$

## **Electric Field**

• *E* points towards a negative point charge and away from a positive point charge.

Superposition principle

$$\vec{F} = \vec{F}_1 + \vec{F}_2 + \dots + \vec{F}_n$$

$$\vec{E} = \vec{E}_1 + \vec{E}_2 + \ldots + \vec{E}_n$$

• Given the E field we can find the force on charge q  $\vec{F} = q\vec{E}$ 

If the vector addition gives zero you do not need to calculate each one.

For example, in the figure below, if  $q_1 = q_2$  then  $\vec{E}_1 + \vec{E}_2 = 0$  at the origin and the field comes only from  $q_3$ .



#### Flux

• Calculate flux of uniform *E* through cylinder

$$\Phi = \oint \vec{E} \bullet d\vec{A}$$



3 surfaces - a, b, and c

$$\Phi = \int_{a} \vec{E} \bullet d\vec{A} + \int_{b} \vec{E} \bullet d\vec{A} + \int_{c} \vec{E} \bullet d\vec{A}$$

#### Flux





#### **Gauss' Law**

Gauss' Law

$$\mathcal{E}_0 \Phi = q_{enc}$$

Also write it as

$$\boldsymbol{\varepsilon}_0 \oint \vec{E} \bullet d\vec{A} = \boldsymbol{q}_{enc}$$

 Net charge q<sub>enc</sub> is sum of all enclosed charges and may be +, -, or zero

# Example for Gauss' Law

- Charge  $q_1$  inside
- *E=0* inside conductor
- Thus \$\varphi = 0\$ for Gaussian surface (red line)
- So net charge enclosed must be 0
- Induced charge of
   q<sub>2</sub> = -q<sub>1</sub> lies on inner
   wall of sphere
- Shell is neutral so charge of  $q_3 = -q_2$  on outer wall



## **Charge distributions**

- *E* field from a continuous line or region of charge
- Use calculus and a charge density instead of total charge, Q
- Linear charge density  $\lambda = Q / Length$
- Surface charge density  $\sigma = Q / Area$
- Volume charge density

$$\rho = Q / Volume$$

# Gauss' Law (Fig. 24-15)

• Non-conducting sheet of charge  $\sigma$ 

$$\mathcal{E}_0 \oint \vec{E} \bullet d\vec{A} = q_{enc}$$

$$\mathcal{E}_0(EA + EA) = \sigma A$$

$$E = \frac{\sigma}{2\varepsilon_0}$$





#### **Electric Potential**

• Electric potential energy U for a constant E and work done by the field

$$\Delta U = U_f - U_i = -W$$

$$\begin{array}{c}
\overrightarrow{E} \\
\overrightarrow{F} \\
\overrightarrow{f}
\end{array}$$

$$\Delta U = -Fd = -qEd$$

• Electric potential for a constant *E* 

$$\Delta V = \frac{\Delta U}{q} = -Ed$$

# Electric Potential (Fig. 25-5)

• Work done by field

$$W = q_0 \int_i^f \vec{E} \bullet d\vec{s}$$

Path Field line 
$$q_0$$
  
 $q_0$   
 $d\vec{s}$   $f$ 

Used to find

$$\Delta V = V_f - V_i = -\frac{W}{q_0} = -\int_i^f \vec{E} \bullet d\vec{s}$$

 Potential decreases if path is in the direction of the electric field



• 1) Suppose we generate an electric field of

$$\vec{E} = 200.0 \ (V / m) \ \hat{i}$$

 What is the change in the electric potential, measured in Volts, associated with a moving a charge of 1.4 C from (0,0) m to (2,2) m?

$$\Delta V = -\int_{i}^{f} \vec{E} \bullet d\vec{s}$$

• A) -400, B) -280, C) 600, D) -800, E) 1000



2) Suppose we generate an electric field of

$$\vec{E} = 1.0 \ (V / m) \ \hat{i} + 2.0 \ (V / m) \ \hat{j}$$

What is the work done (in J) by an external agent (W\*) to move a charge of 6.0 C from (0,0) m to (2,2) m?

$$W^* = -W = -q_0 \int_i^f \vec{E} \bullet d\vec{s}$$

• A) -6, B) 6, C) -36, D) 70, E) -24

## **Electric Potential**

#### Summary for a point change

$$F = k \frac{|q||q_0|}{r^2}$$

$$E = k \frac{q}{r^2}$$

$$V = k \frac{q}{r}$$



# Electric Potential (Fig. 25-3)

- Dashed lines are the edge of equipotential surfaces where all points are at the same potential.
- Equipotential surfaces are always ⊥ to electric field lines and to *E*.
- In this example V decreases by constant intervals from the positive charge to the negative charge



## **Electric Potential**

 Use superposition principle to find the potential due to n point charges

$$V = \sum_{i=1}^{n} V_{i} = k \sum_{i=1}^{n} \frac{q_{i}}{r_{i}}$$

- This is an algebraic sum, not a vector sum
- Include the sign of the charge

## **Electric Potential (Mathematica)**



#### **Electric Field from Potential**

• Take *s* axis to be *x*, *y*, or *z* axes

$$E_x = -\frac{\partial V}{\partial x}, \quad E_y = -\frac{\partial V}{\partial y}, \quad E_z = -\frac{\partial V}{\partial z}$$

• If *E* is uniform and *s* is  $\perp$  to equipotential surface

$$E = -\frac{\Delta V}{\Delta s}$$

## **Potential Energy**

 Total potential energy for a collection of charges is the scalar sum of individual potential energies - work required to assemble the charges

$$U = U_{12} + U_{13} + U_{14} + U_{23} + U_{24} + U_{34}$$



where

$$U_{12} = k \frac{q_1 q_2}{d}$$

etc

## Capacitance

- Calculate *C* of a capacitor from its geometry using steps:
- 1) Assume charge, q, on the capacitor
- 2) Find *E* between using *q* and Gauss' law

$$\varepsilon_0 \oint \vec{E} \bullet d\vec{A} = q_{enc}$$

• 3) Find *V* from *E* using

$$\Delta V = -\int_{i}^{f} \vec{E} \bullet d\vec{s}$$

• 4) Get C using

$$C = \frac{q}{V}$$

# Capacitance (Fig. 26-5)



- Only depends on area A of plates and separation d
- *C* increases if we increase *A* or decrease *d*

## **Energy in a Capacitor**

• Work required from 0 to total charge q is

$$W = \frac{1}{C} \int_0^q q' \, dq' = \frac{q^2}{2C}$$

Potential energy = work

$$U = \frac{q^2}{2C}$$

• Or, use 
$$q = CV$$

$$U = \frac{1}{2}CV^2$$

## Capacitance

- Capacitors in parallel
  - *V* across each is equal
  - Total q is sum
- Capacitors in series
  - q is equal on each
  - Total V is sum





#### Capacitance

- Place a dielectric in capacitor its capacitance increases by numerical factor.
- Called dielectric constant, *k*

$$C_{dielectric} = \kappa C_{air}$$