

September 2nd

Electric Fields – Chapter 23

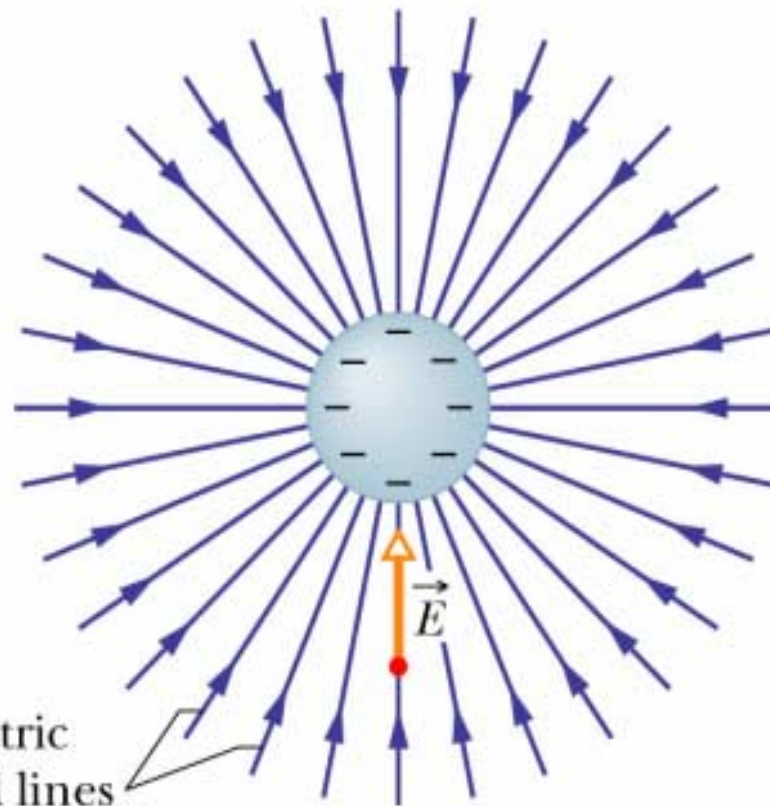
Electric Field

- How does a charge, q_1 , exert a force on another charge, q_2 , when the charges don't touch?
- The charge, q_1 , sets up an **electric field** in its surrounding space
- This electric field has both magnitude and direction which determine the magnitude and direction of the force acting on q_2



Positive
test charge

(a)

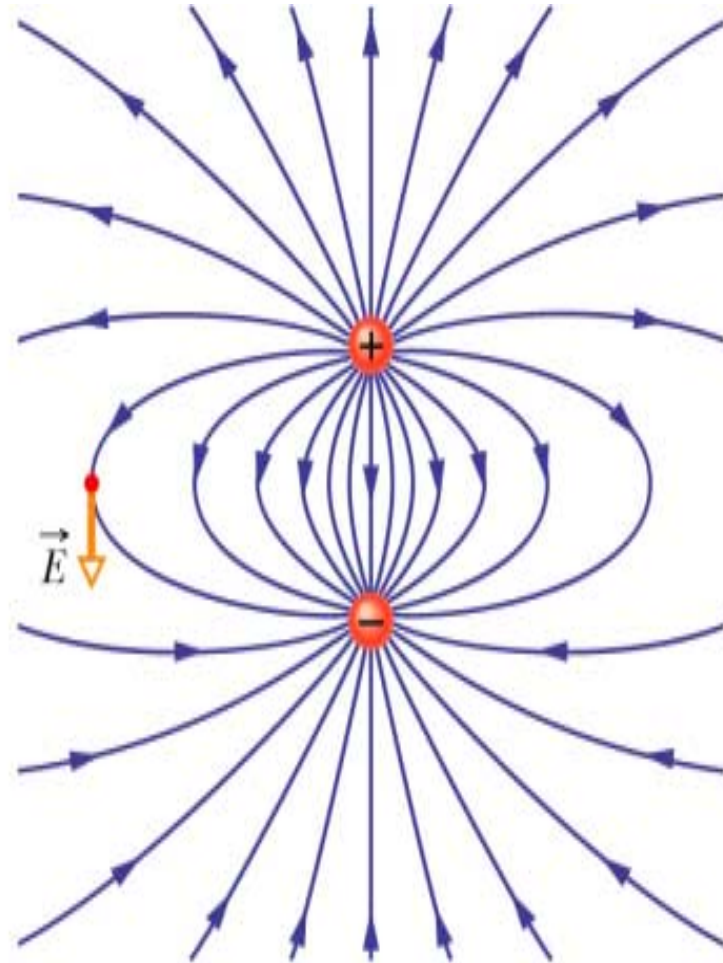


Electric
field lines

(b)

Electric Field

- **Electric field lines:**
 - Point away from positive and towards negative
 - Tangent to the field line is the direction of the E field at that point
 - # lines is proportional to magnitude of the charge



Electric Field

- Electric field lines:
 - Close to a point charge are radial in direction
 - Do not intersect in a charge-free region
 - Begin and end on charges (charge may be at "infinity")
 - Do not begin or end in a charge-free region

Electric Field

- Electric field, E , is the force per unit positive test charge

$$E = \frac{F}{q_0}$$

- For a point charge

$$F = k \frac{|q_0||q|}{r^2}$$

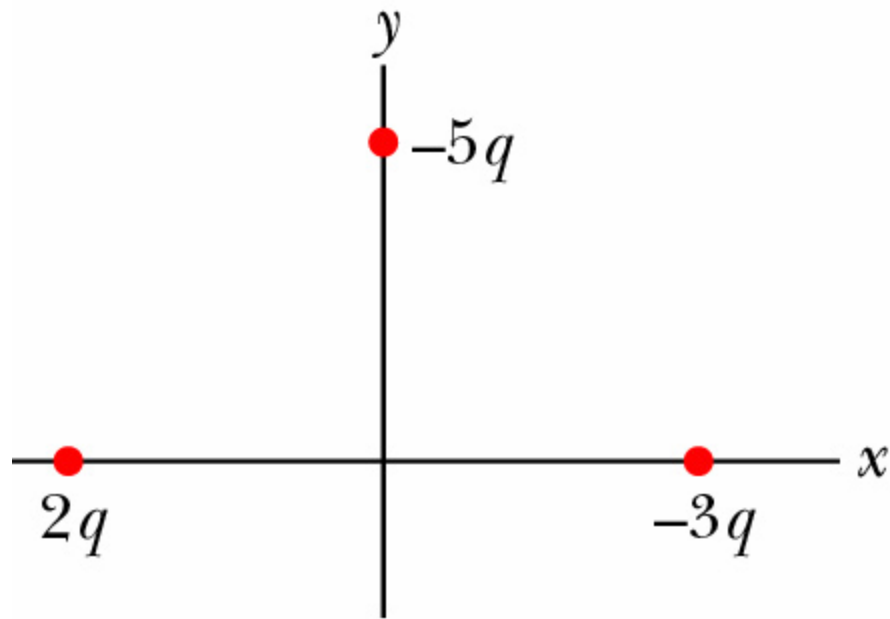
so

$$E = k \frac{|q|}{r^2}$$

Electric Field

- Direction of E = direction of F (for positive charge)
- E points towards a negative point charge and away from a positive point charge
- Superposition of electric fields

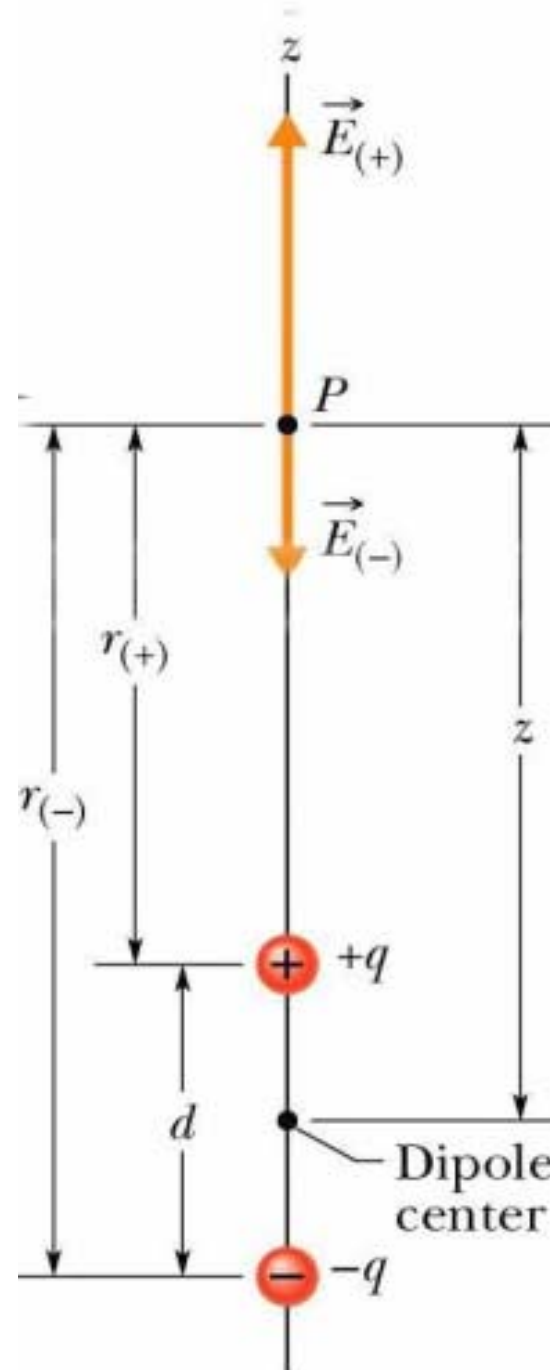
$$\vec{E} = \vec{E}_1 + \vec{E}_2 + \dots + \vec{E}_n$$



(a)

Electric Dipole

- Electric dipole – two equal magnitude, opposite charged particles separated by distance d
- What's the electric field at point P due to the dipole?



- E is on z-axis so

$$E = E_z = E_+ - E_-$$

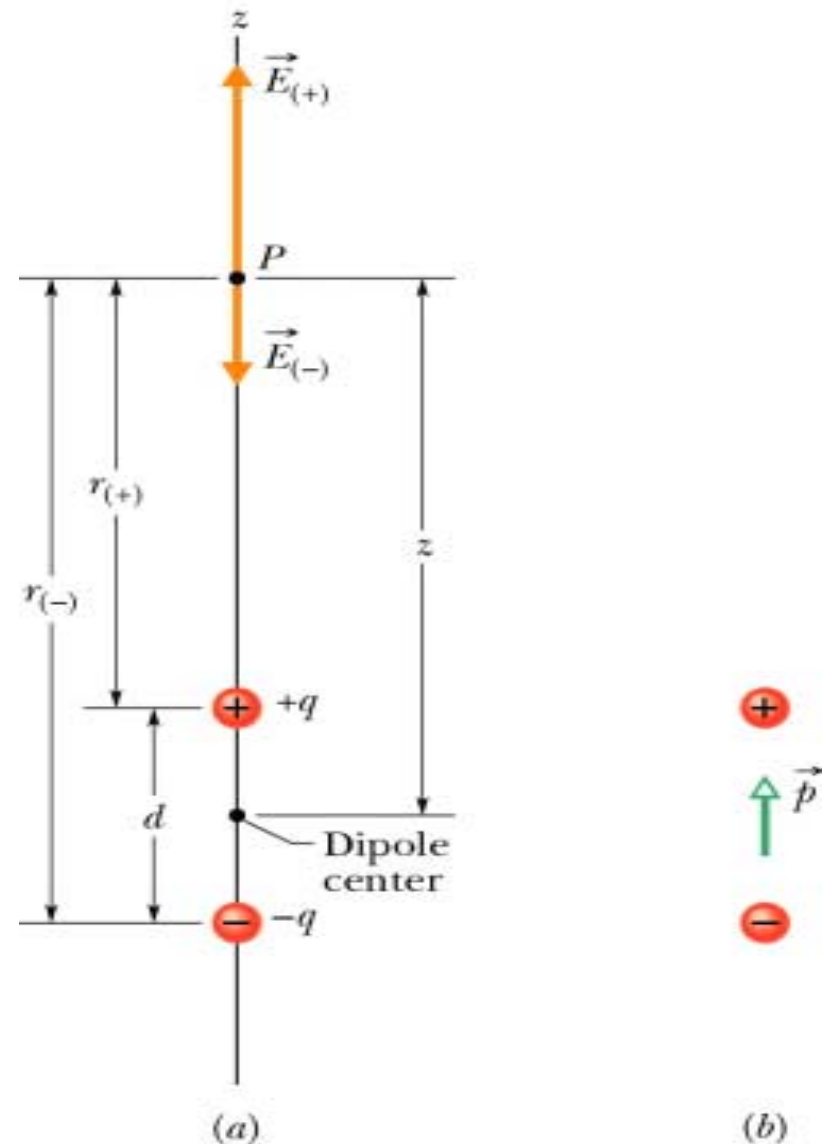
- giving

$$E = k \frac{q}{r_+^2} - k \frac{q}{r_-^2}$$

- where

$$r_+ = z - \frac{d}{2}$$

$$r_- = z + \frac{d}{2}$$



- Substituting and rearranging gives

$$E = \frac{kq}{z^2} \left[\left(1 - \frac{d}{2z} \right)^{-2} - \left(1 + \frac{d}{2z} \right)^{-2} \right]$$

- Assuming $z \gg d$ then expand using binomial theorem ignoring higher order terms $d/z \ll 1$

$$E = \frac{kq}{z^2} \left[\left(1 + \frac{d}{z} + \dots \right) - \left(1 - \frac{d}{z} + \dots \right) \right]$$

Electric Dipole

- Approximate E field for a dipole is

$$E = \frac{2 k q d}{z^3}$$

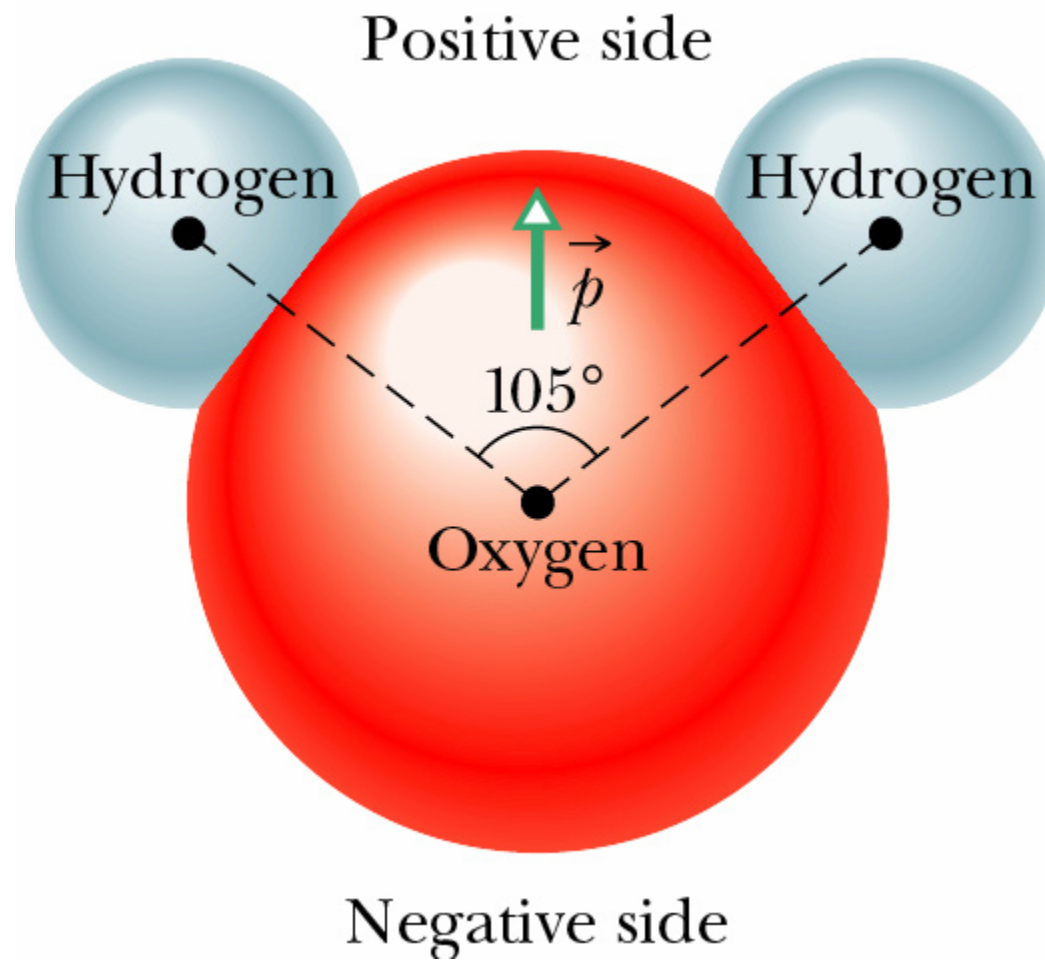
- Define electric dipole moment, p as,

$$\vec{p} = q \vec{d}$$

- The direction of p and d is from the negative to positive

- E field along dipole axis at large distances ($z \gg d$) is

$$E = \frac{2 k p}{z^3}$$



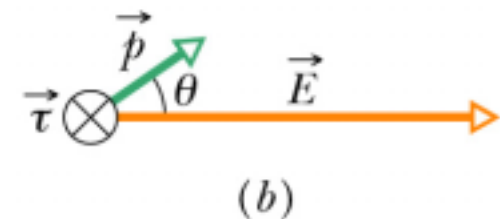
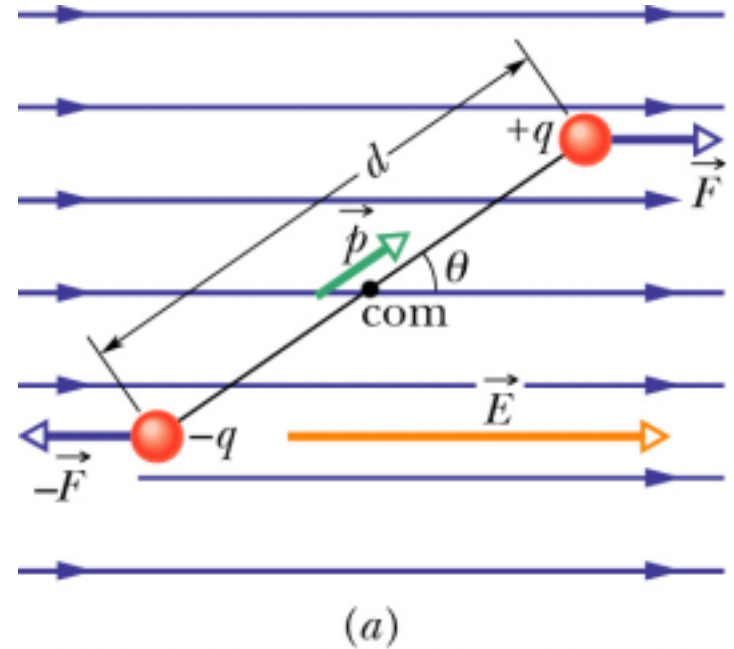
Electric Field

- If a charge q is placed in an electric field, then there is a force given by:

$$\vec{F} = q \vec{E}$$

Electric Dipole

- What happens when a dipole is put in an electric field? (com = center of mass)
- Net force, from uniform E , is zero
- **But** force on charged ends produces a net torque about its center of mass



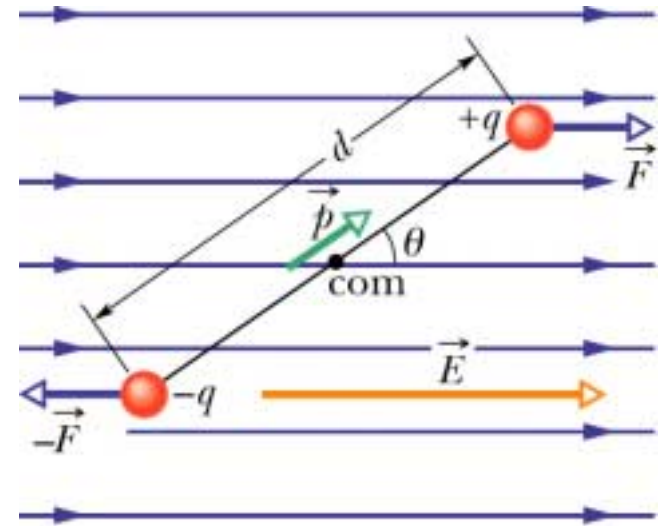
Electric Dipole

- Definition of torque

$$\vec{\tau} = \vec{r} \times \vec{F} = rF \sin \phi$$

- For dipole rewrite it as

$$\begin{aligned} \tau &= xF \sin \theta + (d - x)F \sin \theta \\ &= d F \sin \theta = (qd) (F/q) \sin \theta \end{aligned}$$



(a)

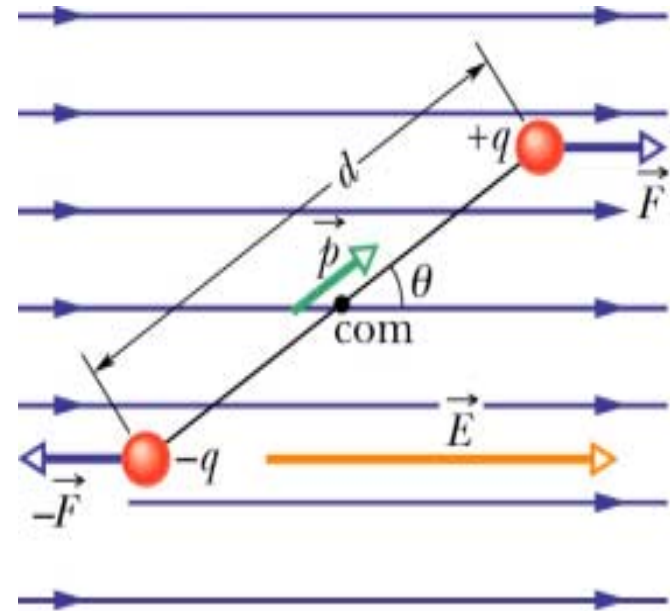


(b)

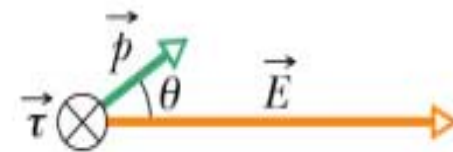
$$\text{Thus: } \vec{\tau} = \vec{p} \times \vec{E}$$

Electric Dipole

- Torque acting on a dipole tends to rotate \vec{p} into the direction of \vec{E}
- Associate potential energy, U , with the orientation of an electric dipole in an \vec{E} field
- Dipole has least U when \vec{p} is lined up with \vec{E}



(a)



(b)

Electric Dipole

- Remember

$$U = -W = -\int_{90}^{\theta} \tau d\theta = \int_{90}^{\theta} pE \sin \theta d\theta$$

- Potential energy of a dipole

$$U = -pE \cos \theta = -\vec{p} \cdot \vec{E}$$

- U is least (greatest) when p and E are in same (opposite) directions

Checkpoint #5

- Rank a) magnitude of torque and b) U , greatest to least

$$\vec{\tau} = \vec{p} \times \vec{E} = pE \sin \theta$$

- a) Magnitudes are same

$$U = -\vec{p} \cdot \vec{E} = -pE \cos \theta$$

- U greatest at $\theta=180$
- 1 & 3 tie, then 2 & 4

