

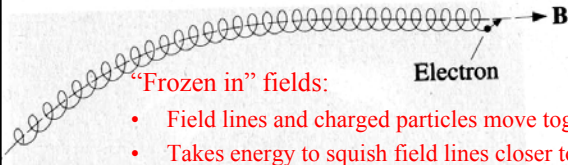
Plasma = a fluid of free charged particles

Maxwell's eqn's:

Gauss's law for electricity	$\epsilon_0 \oint \mathbf{E} \cdot d\mathbf{S} = q$
Gauss's law for magnetism	$\oint \mathbf{B} \cdot d\mathbf{S} = 0$
Ampère's law (as extended by Maxwell)	$\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 \epsilon_0 \frac{d\Phi_E}{dt} + \mu_0 i$
Faraday's law of induction	$\oint \mathbf{E} \cdot d\mathbf{l} = - \frac{d\Phi_B}{dt}$

+ Newton's laws \rightarrow Magnetohydrodynamics (MHD)

$$\begin{aligned} \frac{d\rho}{dt} + \rho \nabla \cdot \mathbf{V} &= 0, \\ \rho \frac{d\mathbf{V}}{dt} + \nabla p - \mathbf{j} \times \mathfrak{B} &= \mathbf{0}, \\ \mathbf{E} + \mathbf{V} \times \mathbf{B} &= \mathbf{0}, \\ \frac{d}{dt} \left(\frac{p}{\rho^\Gamma} \right) &= 0, \end{aligned}$$



"Frozen in" fields:

- Field lines and charged particles move together.
- Takes energy to squish field lines closer together
- Takes energy to stretch field lines.



Charged particles in magnetic field feel Lorentz force:

$$\mathbf{F} = q \mathbf{v} \times \mathbf{B},$$

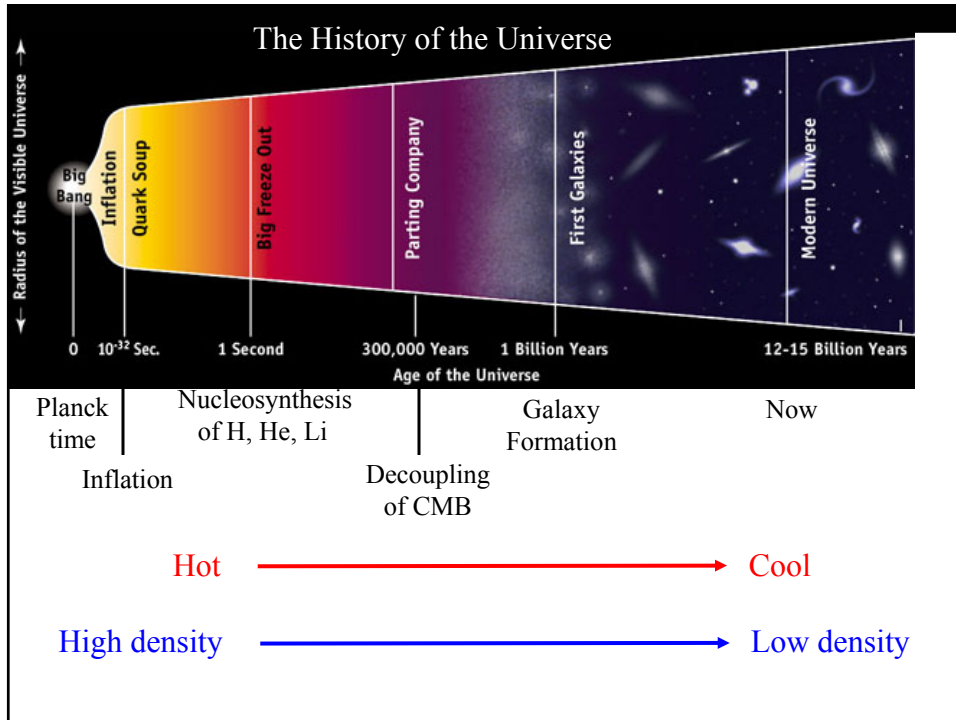


The Sun's magnetic field

Magnetic Field Lines

Figure 26.24 An accretion disk and its magnetic field orbiting a rotating black hole.

<http://farside.ph.utexas.edu/teaching/plasma/lectures/node60.html>



Interactions

Four forces in Nature

1 Gravity

Newton

3 Weak Interaction

Beta (radioactive) decay
Muon decay

Time scales: $10^{-12} \sim 10^3$ sec

2 Electromagnetism

Faraday

4 Strong Interaction

Hold nuclei together
Particle collision

Time scales: 10^{-23} sec

(These slides compliments of Prof. Yuan)

Leptons

- Don't feel the strong force
- Integer or Zero charge
- Flavours:

e^-	"electron" (0.511 MeV)	(1897)	In atoms
μ^-	"Muon" (206 m_e)	(1937)	First seen in Cosmic Ray
τ^-	"Tau" (17 m_μ)	(1975)	Seen at SLAC (Stanford Linear Accelerator Center)
ν_e	"electron neutrino" Pauli's explanation of Beta Decay (1930)	(1956)	<div style="border: 1px solid black; background-color: yellow; padding: 5px;"> <p>Mass</p> <p>$\nu_e < 3 \text{ eV}$</p> <p>$\nu_\mu < 0.19 \text{ MeV}$</p> <p>$\nu_\tau < 18.2 \text{ MeV}$</p> </div>
ν_μ	"Muon neutrino"	(1962)	
ν_τ	"Tau neutrino"	(2000)	

Quarks

- Feel the strong force
- Fractionally charged

$$Q = \begin{cases} 2/3 \\ -1/3 \end{cases} \times \text{Proton charge}$$

- Constituents of neutron and proton
(udd) (uud)

$\begin{pmatrix} u \\ d \end{pmatrix}$ "up"
"down"

- Flavours:

u "up"
d "down"
s "strange"
c "charmed"
b "bottom"
t "top"

Baryon

A strongly interacting particle that is composed of quarks and has a spin that is an integer multiple of \hbar (e.g., a quark, neutron, or proton).

The Standard Model of Particle Physics

❖ Matter fields (make up all visible matter in the universe)

▪ Fermions (Spin 1/2)

Lepton (No Strong Interaction)

$$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix}_L \quad \begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix}_L \quad \begin{pmatrix} \nu_\tau \\ \tau^- \end{pmatrix}_L$$

$$e^-_R \quad \mu^-_R \quad \tau^-_R$$

Quarks (q)

$$\begin{pmatrix} u \\ d \end{pmatrix}_L \quad \begin{pmatrix} u \\ d \end{pmatrix}_L \quad \begin{pmatrix} u \\ d \end{pmatrix}_L \quad \begin{pmatrix} c \\ s \end{pmatrix}_L \quad \begin{pmatrix} c \\ s \end{pmatrix}_L \quad \begin{pmatrix} c \\ s \end{pmatrix}_L \quad \begin{pmatrix} t \\ b \end{pmatrix}_L \quad \begin{pmatrix} t \\ b \end{pmatrix}_L \quad \begin{pmatrix} t \\ b \end{pmatrix}_L$$

$$u_R \quad u_R \quad u_R \quad c_R \quad c_R \quad c_R \quad t_R \quad t_R \quad t_R$$

$$d_R \quad d_R \quad d_R \quad s_R \quad s_R \quad s_R \quad b_R \quad b_R \quad b_R$$

} 3 families

▪ Scalar (Spin 0)

Higgs Boson (Not yet found!)

(From Higgs Mechanism — Spontaneous Symmetry Breaking)

The Standard Model of Particle Physics

❖ Interactions (mediated by interchanging Gauge Bosons, spin-1 force carrier)

1) Electromagnetic Interaction (QED)

Photon (massless)

2) Strong Interaction (QCD)

Gluon (massless) (1979)

3) Weak Interaction

W^+ , W^- and Z Gauge Bosons (1983)

$$\left(\begin{array}{l} \text{massive } M_W = 80.4 \text{ GeV} \\ M_Z = 91.187 \text{ GeV} \end{array} \quad 1 \text{ GeV} = 10^9 \text{ eV} \right)$$

In SM, the Mass of W-boson, either W^\pm or Z , arises from the Higgs Mechanism

(Without it, Gauge Bosons have to be massless from gauge principle.)

“Freezing out” of the four forces:

