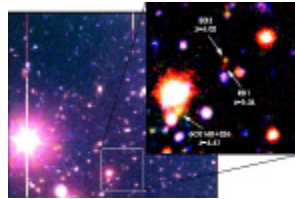


When Radiation Ruled—31 Oct

- Mass of radiation was more than mass of matter at early times
 - Stars & galaxies cannot form because of pressure of radiation.
 - Like trying to make a ball of light collapse.
- Recombination: when matter became free.



Galaxy 0140+326 RD1 at $z=5.35$ or $a=1/6.35$
<http://antwrp.gsfc.nasa.gov/apod/ap980324.html>

How mass density of radiation changes

- Mass of radiation = $4 \times 10^{-32} \text{kg}$
 - Same mass as 1/50,000 hydrogen atom
 - Mass density of matter changes as
 - $\rho = \rho_{\text{now}} a^{-3}$
 - One power for each dimension
 - Photons have mass
 - $E = m c^2$
 - Energy of a photon is proportional to temperature
1. (2 pts.) The radiation in the 2-L bottle used to occupy a smaller volume. When universe half the present size, how much volume did the radiation in the 2-L bottle fill? The mass density at that time was ___ that of the present mass density.



Then



Matter: $2 \times 10^{-27} \text{kg}$
 Rad: $4 \times 10^{-32} \text{kg}$

How mass density of radiation changes

- Mass of radiation = $4 \times 10^{-32} \text{kg}$
 - Same mass as 1/50,000 hydrogen atom
- 1. (2 pts.) The radiation in the 2-L bottle used to occupy a smaller volume. When universe half the present size, how much volume did the radiation in the 2-L bottle fill? The mass density at that time was ___ that of the present mass density.
- Mass of a photon decreases as universe expands
 - $E = m c^2$.
 - $\text{Mass} \propto E \propto T \propto 1/\lambda$ (Wien)
- Mass density of radiation changes as
 - $\rho = \rho_{\text{now}} a^{-4}$
 - One power for each dimension and one power for mass



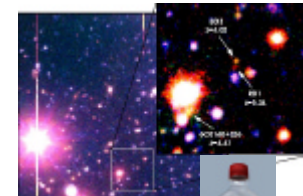
Then



Matter: $2 \times 10^{-27} \text{kg}$
 Rad: $4 \times 10^{-32} \text{kg}$

Mass density of matter & radiation

- In a 2-L bottle
 - Mass of radiation = $4 \times 10^{-32} \text{kg}$
 - Same mass as 1/50,000 hydrogen atom
 - Mass of matter = $2 \times 10^{-27} \text{kg}$
 - Same mass as 1 hydrogen atom
- Mass density changes as
 - $\rho = \rho_{\text{now}} a^{-3}$ for matter
 - $\rho = \rho_{\text{now}} a^{-4}$ for radiation
- When the light that we see left Galaxy 0140+326 RD1, its wavelength was 1215 Å (121.5nm). We see its wavelength to be 7710Å. λ has expanded by a factor of 6.35 since the time the light left that galaxy. $a=1/6.35$ when light left galaxy.
- 2. (2 pts.) How much greater was the mass of the matter in 2LB when LLG? How much greater was the mass of radiation...?



Matter: $2 \times 10^{-27} \text{kg}$
 Rad: $4 \times 10^{-32} \text{kg}$

Mass density of matter & radiation

- In a 2-L bottle
 - Mass of radiation = 4×10^{-32} kg
 - Same mass as 1/50,000 hydrogen atom
 - Mass of matter = 2×10^{-27} kg
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 - $\rho = \rho_{\text{now}} a^{-3}$ for matter
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- When the light that we see left Galaxy 0140+32 RD1, its wavelength was 1215 Å (121.5nm). W its wavelength to be 7710Å. U has expanded by factor of 6.35 since the time the light left that galaxy. $a=1/6.35$ when light left galaxy.
- 2. (2 pts.) How much greater was the mass of the matter in 2LB when LLG? How much greater was the mass of radiation...?
- Radiation dominated matter when U was young
 - $M_{\text{matter}} = 6.35^3 = 260$
 - $M_{\text{rad}} = 6.35^4 = 260 * 6.35 = 1600$
 - At $a=1/6.35$, radiation gains by a factor of 6.35.
 - When $a=1/50,000$, mass of radiation matched mass of matter.



Matter: 2×10^{-27} kg
Rad: 4×10^{-32} kg

Pressure of radiation

- Can a star or galaxy form? Battle: Pressure vs. gravity
 - If gravity wins, star or galaxy forms.
 - If pressure wins, no star, no galaxy.
- Pressure on a balloon comes from gas particles hitting balloon and transferring momentum.
 - Interpret $PV=nRT$ as $P=n/V RT$ = number density \times mass \times speed²
 - $P = \text{mass density} \times \text{speed}^2$.
- Pressure of radiation dominates when mass density of matter & radiation are close.
 - For matter (H atoms) at 3000K, $v=6$ km/s.
 - For radiation $v=300,000$ km/s.
 - Pressure of radiation is bigger by $(300,000/6)^2 = 2.5 \times 10^9$.
- How can star form?
 - When matter no longer interacts with radiation
 - $p + e \rightarrow$ hydrogen atom

When stars and galaxies form

- Pressure of radiation is bigger by 2.5×10^9 .
- How can star form?
- When matter was ionized
 - Gravity pulls matter together; ionized electrons hit radiation and get pushed back apart.
- After recombination (at $a=1/1200$.)
 - $p + e \rightarrow$ hydrogen atom
- 3. Modify the statement "Gravity pulls matter together; ionized electrons hit radiation and get pushed back apart." so that it applies to the universe after recombination.

When stars and galaxies form

- Pressure of radiation is bigger by 2.5×10^9 .
- How can star form?
- When matter was ionized
 - Gravity pulls matter together; ionized electrons hit radiation and get pushed back apart.
- After recombination (at $a=1/1200$.)
 - $p + e \rightarrow$ hydrogen atom
- After recombination: Gravity pulls matter together; without ionized electrons to hit, radiation does not exert pressure on matter. Pressure drops by a factor of 10^{11} .
- Gravity wins and pulls more. Stars and galaxies form.