

## Weighing the Universe—18 Apr

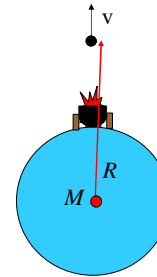
- Fill out SIRS; then get 3 bonus clicker points an angel.
  - 18-29 April
- Dear Students:
 

As Director of Integrative Studies- Science, your opinions of ISP and ISB are very important to me. Comments from previous students have made a difference and yours may also. Therefore, I hope you'll take a few minutes and go to <http://www.gsu.edu/~sibley> and fill in the SIRS questionnaire. I look at the results for every class, and I read every comment.

If you would rather write me directly, please email me at [sibley@gsu.edu](mailto:sibley@gsu.edu). I'll write back. Thank you, and good luck on your finals.

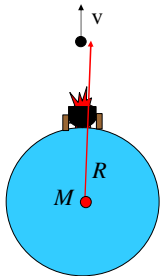
Dr. Duncan Sibley, Director  
Center for Integrative Studies in General Science
- Weighing the earth with a cannonball
  - What is the fate of the cannonball? Will it fall back to earth?
  - What is the mass of the earth? Is there mass that we cannot see?
- Weighing the universe
  - What is the fate of the universe? Will it expand forever or fall back on itself?
  - What is the universe made of? Is there mass that we cannot see?
- Key parameter: PE/KE

## A Cannon Ball



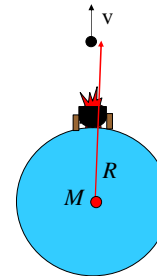
- Cannonball is shot out of cannon at speed  $v$ . Cannonball has mass=1kg.
  - Kinetic energy is  $\frac{1}{2} v^2$ .
- Gravity pulls on cannonball to slow the motion.
  - Potential energy of gravity is
    - $G M / R$
    - $M$  is entire mass enclosed by sphere of radius  $R$ !
    - Mass outside of  $R$  does not count if spherically symmetric.
    - Distance is  $R$  between cannonball and center of sphere!

## A Cannon Ball



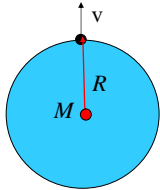
- Cannonball is shot out of cannon at speed  $v$ . Cannonball has mass=1kg.
  - Kinetic energy is  $KE = \frac{1}{2} v^2$ .
- Gravity pulls on cannonball to slow the motion.
  - Potential energy of gravity is
    - $PE = G M / R$
- Cannonball will escape if
  - $KE \geq PE$
  - Shot faster than gravity can hold
- Define “Density parameter”
  - $\Omega = PE/KE = 2 G M / (R v^2)$

## A Cannon Ball



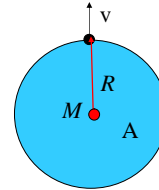
- Kinetic energy is  $KE = \frac{1}{2} v^2$ .
- Potential energy of gravity is
  - $PE = G M / R$
- Cannonball will escape if
  - $KE \geq PE$
  - Shot faster than what gravity can hold
- Define “Density parameter”
  - $\Omega = PE/KE = 2 G M / (R v^2)$
- 1. A cannonball is shot with  $\Omega=0.7$ . Will the cannonball escape? Same question for  $\Omega=1.1$ .

### A Galaxy



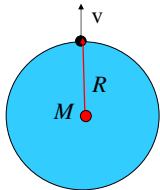
- Hoag's object is moving from us at speed  $v$ . Galaxy has mass=1kg.
  - Kinetic energy is  $\frac{1}{2} v^2$ .
- Gravity pulls on galaxy to slow the motion.
  - Potential energy of gravity is
    - $G M / R$
    - $M$  is entire mass enclosed by sphere of radius  $R$ !
    - Mass outside of  $R$  does not count if spherically symmetric.
    - Distance is  $R$  between cannonball and center of sphere!

### A Galaxy



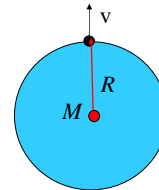
- Hoag's object is moving from us at speed  $v$ . Galaxy has mass=1kg.
  - Kinetic energy is  $\frac{1}{2} v^2$ .
- Gravity pulls on galaxy to slow the motion.
  - Potential energy of gravity is
    - $G M / R$
- 2. Galaxies are distributed uniformly in space. Do galaxies at A affect motion of H's object? Same question for galaxies at B.
  - a. NN
  - b. NY
  - c. YN
  - d. NN

### A Galaxy



- Hoag's object is moving b/c big bang. Use Hubble's Law  $v = H R$ 
  - Kinetic energy is  $\frac{1}{2} v^2 = \frac{1}{2} H^2 R^2$ .
- Potential energy of gravity is
  - $G M / R$
- Define "Density parameter"
  - $\Omega = PE/KE = 2 G M / (R v^2)$
  - $\Omega = PE/KE = 2 G M / (R^3 H^2)$
- Mass/volume is mass density  $\rho$ 
  - $\Omega = PE/KE = 8\pi G \rho / H^2$
- Does not depend on particular galaxy

### A Galaxy



- Density parameter
  - $\Omega = PE/KE = 8\pi G \rho / H^2$
- 3.  $\Omega=0.7$ . Will the universe expand forever? Same question for  $\Omega=1$ .
  - a. YY
  - b. YN
  - c. NY
  - d. NN