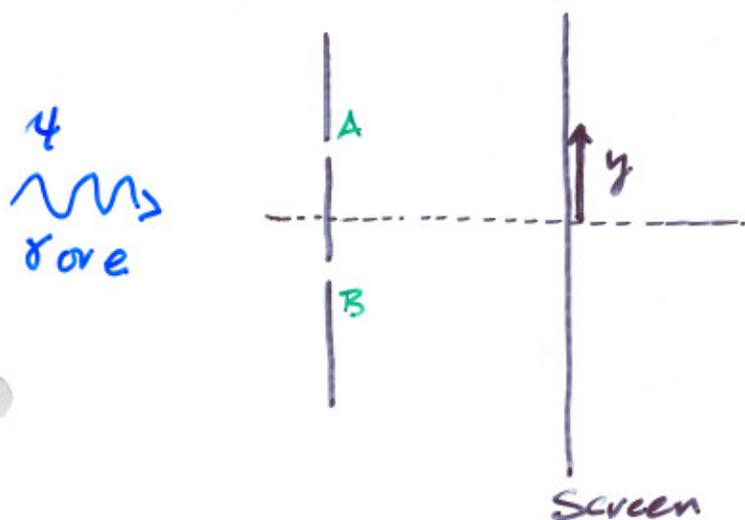


# NO CHAPTER... A BIT ON THE CONCEPTUAL ISSUES IN QUANTUM MECH.

## WHAT ARE "CLASSICAL" COMMITMENTS?

- OBJECTS EXIST IN SPACE & TIME
  - can be localized, can be counted
  - evolution takes place in space & time
- CAUSALITY
  - every event has a cause
- DETERMINATION
  - every later <sup>state</sup> ~~event~~ is uniquely determined by an earlier state
- CONTINUITY
  - all process exhibit an initial and final state in space and time
  - they ~~also~~ inhabit each instant in space and time between those states

The 2 slit returns...



Quantum mechanics predicts - with precision -  
the probability of finding an electron at  $y$   
- only the probability  $\rightarrow$  BUT... get only whole wave

$$\psi = \psi_A + \psi_B$$

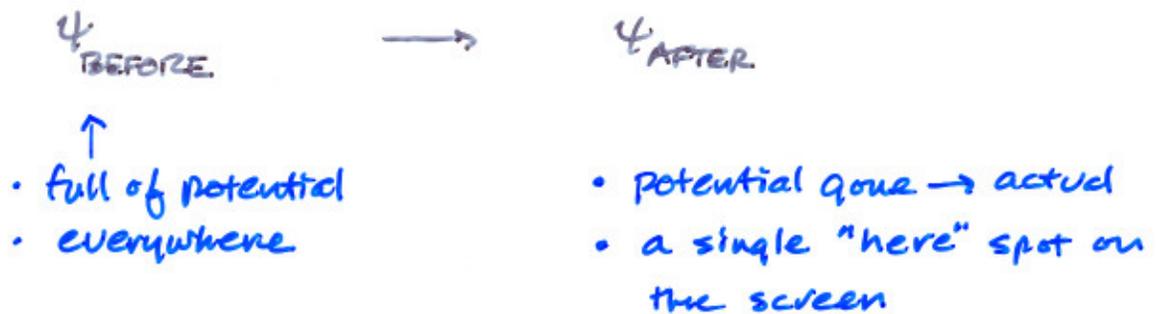
the wavefunction contains  
the potential of passing  
through A and/or B.

$$|\psi|^2 dy = (|\psi_A|^2 + |\psi_B|^2 + 2\psi_A\psi_B) dy$$

interference creates the  
fringes

Try to identify the slit -- ask a question about localization (a particle-like question) -- the interference (the wave-like character) goes away.

What causes the indeterminant  $\Psi$  to become the real, classical THING of a whole electron or photon on the screen?



"Copenhagen" answers: A MEASUREMENT.

a measurement is ... an observation.

→ the "observer" seems to play a role in making reality.

Said another way---

What is the state of the electron/photon before the measurement (before being observed)?

"Copenhagen" answers: not a meaningful scientific question.

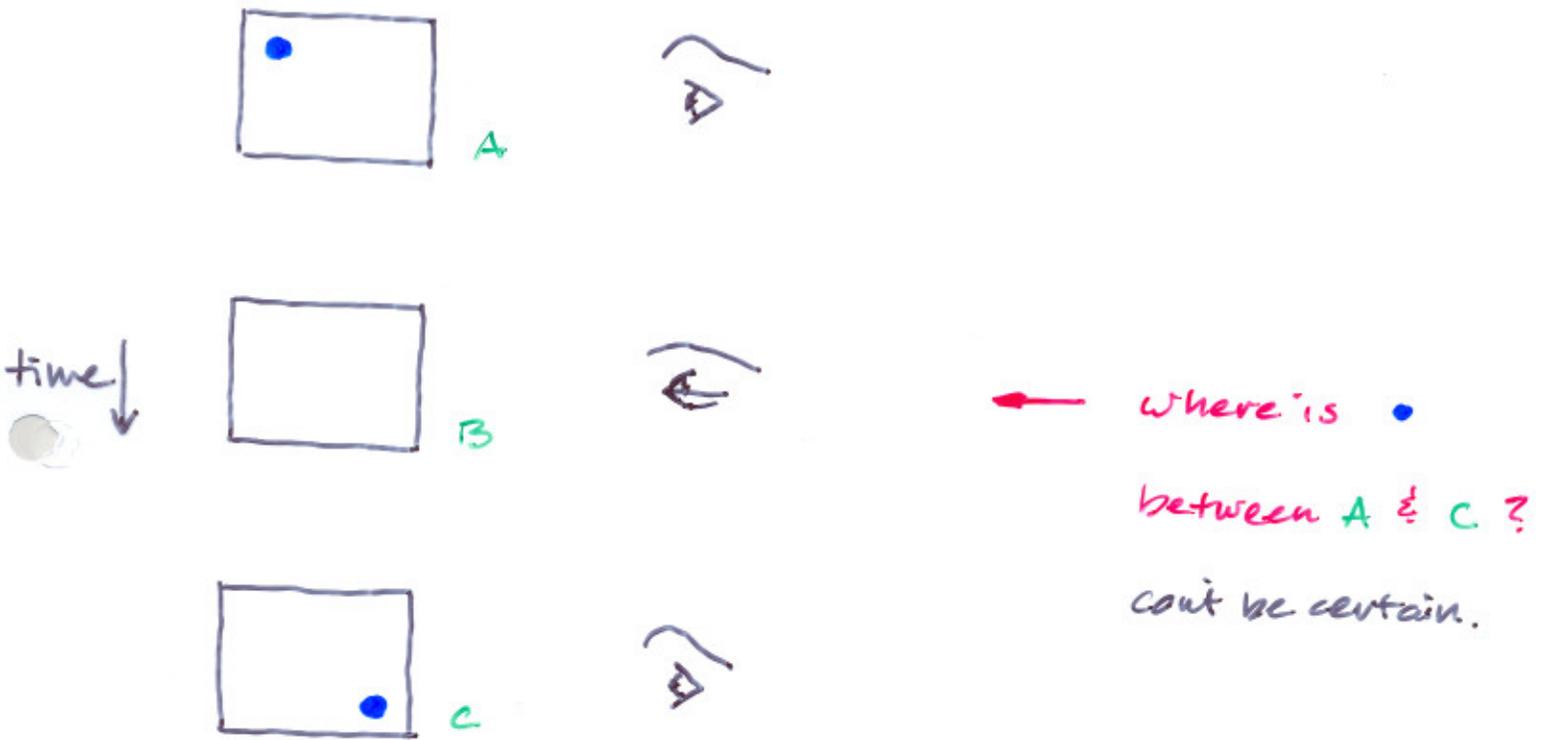
Wanna know? Make a measurement.

The Schrödinger equation precisely predicts the behavior of  $\psi$

But Born taught us that the connection to the world is  $|\psi|^2$  ... a probability.

What you see is what you get.

but what you get can only come from what you see.



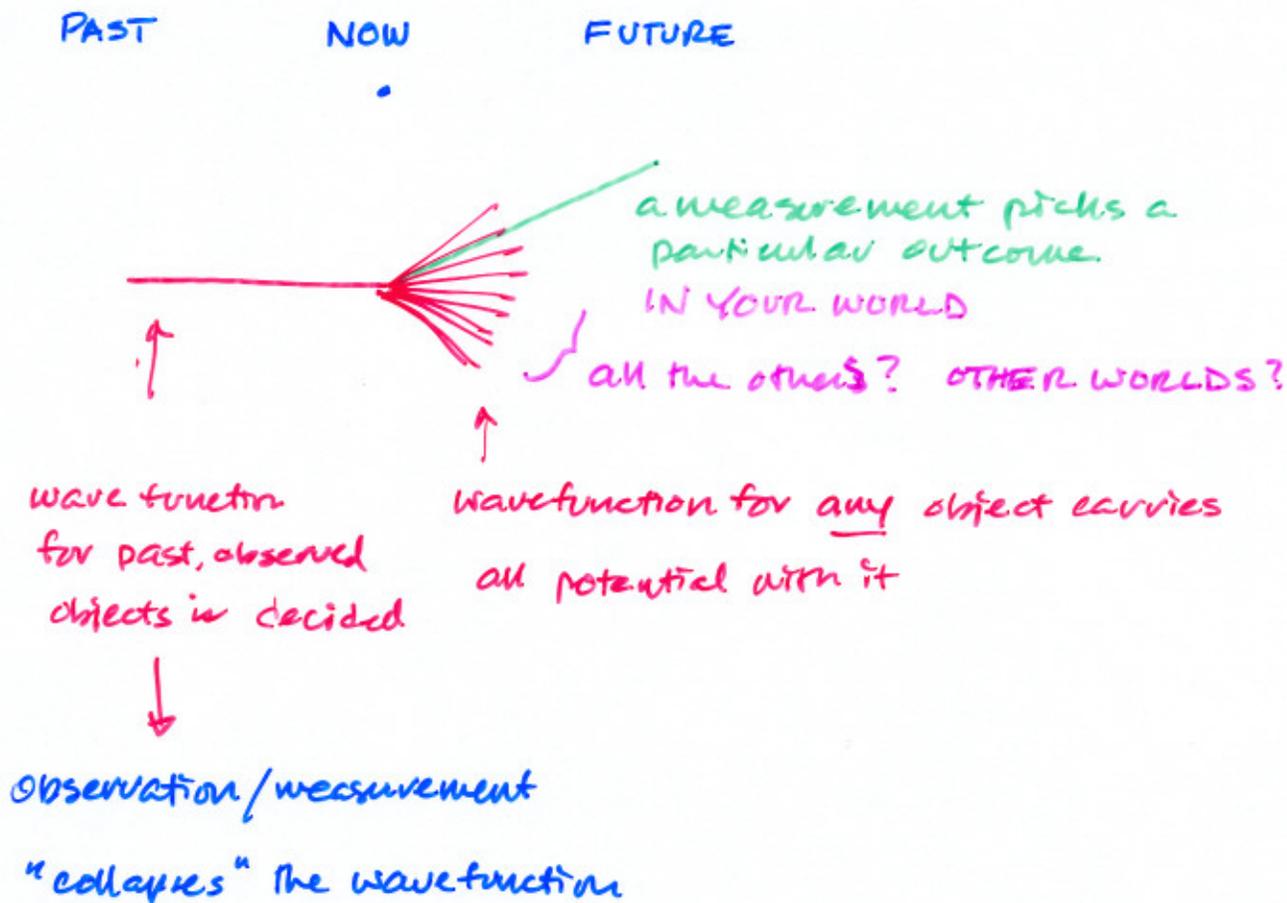
In some sense, Bishop Berkeley has returned.

Tied to the Uncertainty Principle...

"Copenhagen" insists: objects possessing both a specific position and specific speed cannot be said to exist

→ don't exist? That's for you to decide!

# A STRANGE "ARROW OF TIME"



The "Many Worlds Interpretation" of QM

→ totally consistent with everything  
no "measurement problem"

The price? A weird view of  $\infty$  worlds popping up everywhere, everytime.

This famously disgusted Einstein and Schrödinger

opposed to

Bohr, Heisenberg, Born.

Schrödinger facetiously famously proposed the cat paradox  
in 1935.



The Schrödinger Cat.

- half-life of 60 min
- creates an electrical connection which releases a hammer
- breaking a vial of poison

after 60 minutes, is the cat alive or dead?

→ 50-50 chance that this is so.

- Copenhagen Interpretation?

cannot ask.

- Von Neumann

consciousness only causes  $\psi$  to collapse

- Many Worlds Interpretation

cat both alive and dead

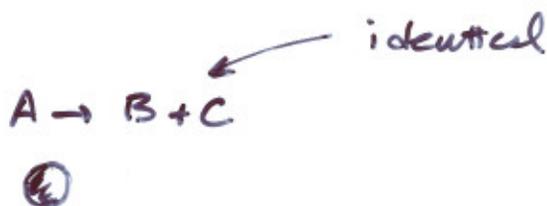
- Einstein and Bohm

missing information, or another, hidden variable

in QM... when found, would make a

well-behaved prediction.

1935 also, Einstein, Rosen, Podolsky postulated  
an experiment designed to destroy the  
Copenhagen interpretation



"EPR Paradox"

O can make a measurement on C.

- okay, measure the momentum precisely.

⇒ the position of C becomes completely  
undetermined.

BUT ALSO Copenhagen says that this  
makes the position of B completely  
unknown.

→ hidden variables applied BY experiment.

Einstein wrong.

## Modern interpretation



"entanglement"

→ Bottom line—

- most adhere to Copenhagen interpretation
- none believe in Hidden Variables
- some willing to acknowledge the MW interpretation

# CHAPTER 9 STATISTICAL PHYSICS

an experiment... a bit of plastic & a bit of chalk.

hold your breath...

Kinetic Theory & Boltzmann's Approach  
Remember, for an ideal gas we found

$$\langle K \rangle = \frac{3}{2} kT$$

- now let molecules have a variety of velocities and  $E$ 's  
→ continuum.

$n(\vec{v}) d\vec{v}$  = number of molecules per unit volume  
having velocity between  $\vec{v}$  and  $\vec{v} + d\vec{v}$   
 $n(\vec{v})$  is the number density per unit volume

$$\# \text{ molecules per unit volume} = n = \int n(\vec{v}) d\vec{v}$$

or - can work in probabilities -

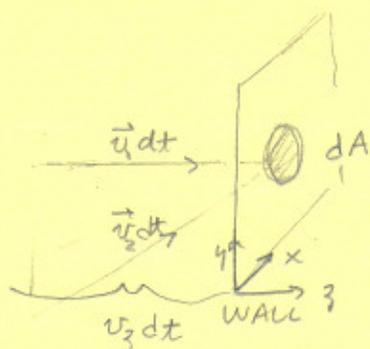
$$f(\vec{v}) d^3\vec{v} = \frac{n(\vec{v}) d^3\vec{v}}{n} \quad \text{probability of finding a molecule with } \vec{v} \text{ to } \vec{v} + d\vec{v}$$

$$f(\vec{v}) d^3\vec{v} = f(\vec{v}) dv_x dv_y dv_z$$

$f(\vec{v})$  is the probability density function.

$$f(\vec{v}) = \frac{n(\vec{v})}{n}$$

Remember, averages:  $\langle v^2 \rangle = \int v^2 f(\vec{v}) d^3\vec{v}$



each can contribute to pressure on  $dA$  during  $dt$  by transferring  $P_z$  during that time.

the momentum transfer due to molecules with  $\vec{v}$  between  $\vec{v}$  and  $\vec{v} + d\vec{v}$  is

$$(2mv_z) [n(\vec{v}) d^3\vec{v}] (dA v_z dt)$$

$$= 2m dA dt v_z^2 n(\vec{v}) d^3\vec{v}$$

The total  $\Delta p$  transferred

$$\Delta p = 2m dA dt \int_{+v_z}^{\text{all } \vec{v}} v_z^2 n(\vec{v}) d^3\vec{v}$$

$$\text{Pressure} = \frac{\Delta p}{dt dA} = P = 2m \int v_z^2 n(\vec{v}) d^3\vec{v}$$

no preferred direction  $\Rightarrow n(\vec{v}) = n(v)$   $v$ -speed.

$$v_z > 0 \Rightarrow \text{all speed} \times \frac{1}{2}$$

$$P = \frac{2m}{2} \int_{\text{all}} \left( \frac{v_z^2 + v_y^2 + v_x^2}{3} \right) n(v) d^3\vec{v} = \frac{2m}{3} \int v^2 n(v) d^3\vec{v}$$

$$P = \frac{1}{3} m n \int d^3 \vec{v} \underbrace{v^2}_{\langle v^2 \rangle} f(v)$$

$$= \frac{2}{3} n \cdot n \int d^3 \frac{1}{2} m v^2 f(v)$$

$$P = \frac{2}{3} n \langle K \rangle \Rightarrow \langle K \rangle = \frac{3}{2} kT = \frac{1}{2} m \langle v^2 \rangle$$

need  $f(v)$  to go further.

$f$  only depends on the speed.

So probabilities are independent for  $v_x$ ,  $v_y$  or  $v_z$

$$\begin{aligned} f(v_x, v_y, v_z) &= h(v_x) h(v_y) h(v_z) \\ &= f(v_x^2 + v_y^2 + v_z^2) \end{aligned}$$

what kind of function works? Take log.

$$\begin{aligned} \ln h(v_x^2) + \ln h(v_y^2) + \ln h(v_z^2) \\ = \ln f(v_x^2 + v_y^2 + v_z^2) \end{aligned}$$

which implies

$$h(v_i^2) = \text{constant} + e^{-Bv_i^2}$$

so

$$f(v) = C e^{-B(v_x^2 + v_y^2 + v_z^2)} = C e^{-Bv^2}$$