Adiabatic Expansion ($\Delta Q = 0$)

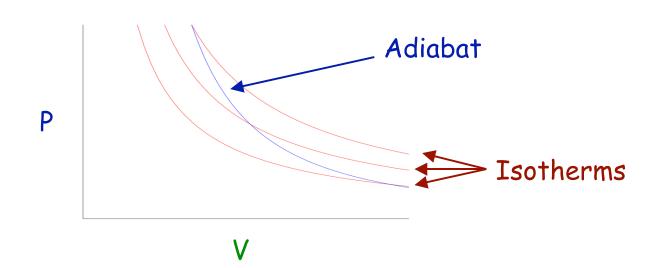
Occurs if:

- change is made sufficiently quickly
- and/or with good thermal isolation.

Governing formula:

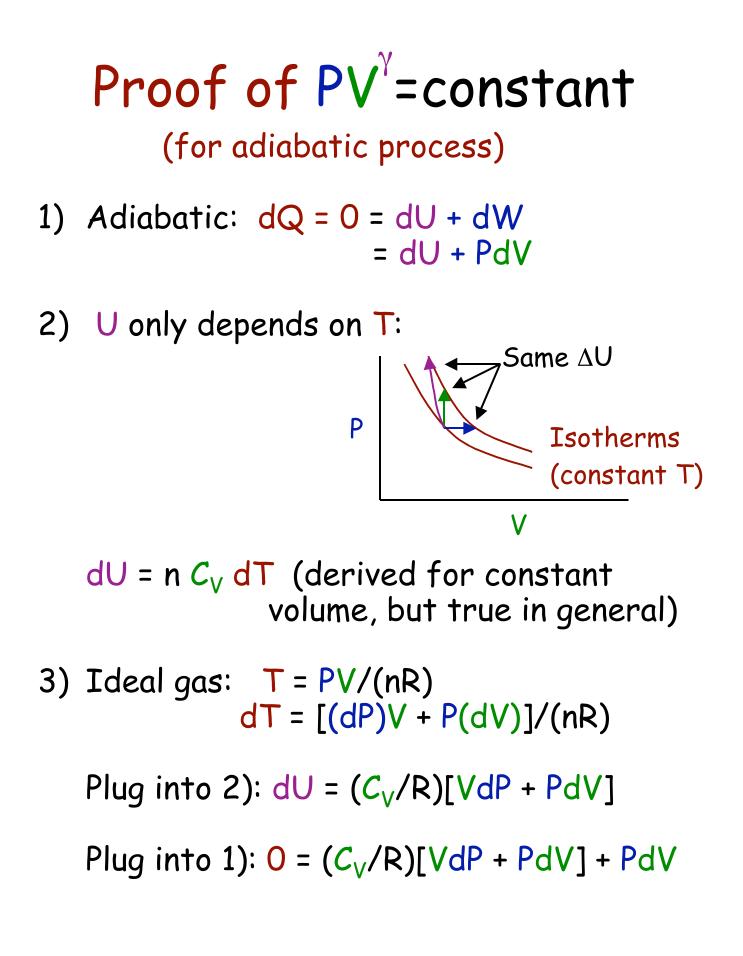
$$PV^{\gamma}$$
 = constant

where $\gamma = C_P / C_V$



Because PV/T is constant (ideal gas):

 $V^{\gamma-1}T$ = constant (for adiabatic)



Rearrange:

 $(dP/P) = - (C_V + R)/C_V (dV/V)$ = - $\gamma (dV/V)$

where $\gamma = (C_V + R)/C_V = C_P/C_V$

Integrate both sides:

 $ln(P) = -\gamma ln(V) + constant$

or

 $ln(PV^{\gamma}) = constant$

or

 PV^{γ} = constant

QED

Irreversible Processes

Examples:

- Block sliding on table comes to rest due to friction: KE converted to heat.
- Heat flows from hot object to cold object.
- Air flows into an evacuated chamber.

Reverse process allowed by energy conservation, yet it does not occur.

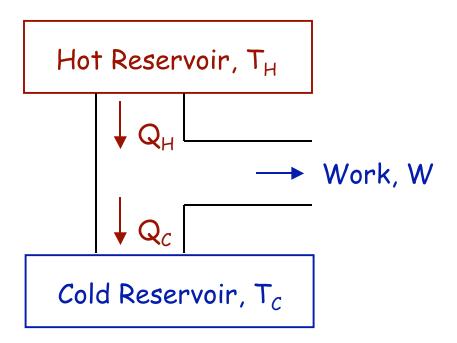


Why?

2nd Law of Thermodynamics (entropy)

<u>Heat Engines</u>

Heat engine: a <u>cyclic</u> device designed to convert heat into work.



2nd Law of TD (Kelvin form):

It is impossible for a cyclic process to remove thermal energy from a system at a single temperature and convert it to mechanical work without changing the system or surroundings in some other way. For a cyclic engine $\Delta U = 0$,

So work done is equal to heat in minus heat out:

 $W = Q_H - Q_C$

Define the Efficiency of the engine:

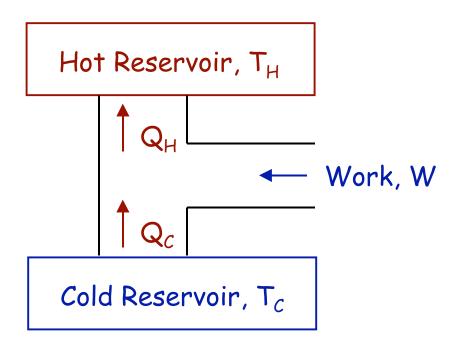
 $\varepsilon = W/Q_H = (Q_H - Q_C)/Q_H = 1 - Q_C/Q_H$

Corollary of the 2nd Law of TD:

It is impossible to make a heat engine whose efficiency is 100%.

Refrigerators

Refrigerator: a cyclic device which uses work to transfer heat from a cold reservoir to hot reservoir.



2nd Law of TD (Clausius form):

It is impossible for a cyclic process to have no other effect than to transfer thermal energy from a cold object to a hot object. A measure of refrigerator performance is the ratio:

 $K = Q_c / W$

"Coefficient of performance" (The larger the better.)

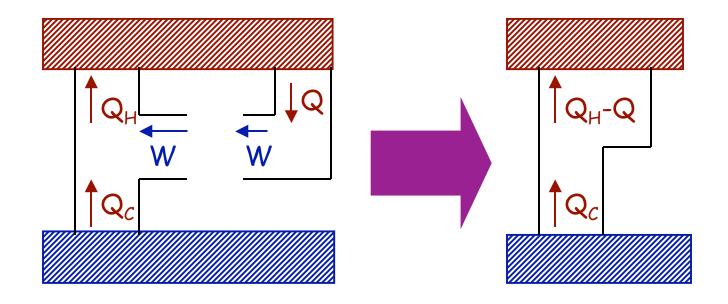
Corollary of the 2nd Law of TD:

It is impossible for the coefficient of performance to be infinite.

<u>Equivalence of Kelvin and</u> <u>Clausius</u> Statements

For example:

You could combine an ordinary refrigerator with a <u>perfect</u> engine (impossible)...



to obtain a <u>perfect</u> refrigerator (also impossible).

The Carnot Engine

2nd Law of TD says:

100% efficient Heat Engine is impossible.

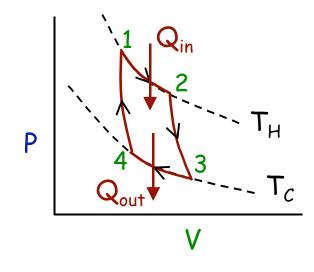
What is the maximum possible efficiency?

No engine working between 2 heat reservoirs can be more efficient than an <u>ideal</u> engine acting in a Carnot cycle. (Sadi Carnot, 1824)

Properties of the Carnot cycle:

- 1. It is reversible: no friction or other dissipative forces.
- 2. Heat conduction only occurs isothermally at the temperatures of the two reservoirs.

Derivation of Carnot Efficiency

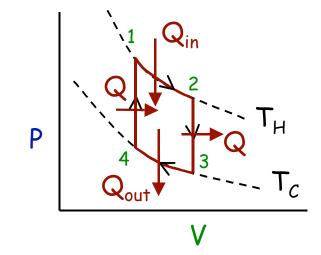


- 1-2: Isothermal (Q_{in} at T_H)
- 2-3: Adiabatic expansion
- 3-4: Isothermal (Q_{out} at T_C)
- 4-1: Adiabatic compression

$$\varepsilon = 1 - T_C / T_H$$

The Stirling Engine

Invented by Robert Stirling in 1816. Its operating cycle is:



The two temperature-changing steps are performed at constant volume; A heat transfer occurs at these steps also.

Entropy

Consider a reversible process for an ideal gas:

 $dQ = dU + dW = n C_V dT + P dV$

 $= n C_V dT + n R T (dV/V)$

We cannot write a general integral of this, because dW (and therefore dQ) depends on the functional form of T(V) (i.e. the path). However, if we divide by T:

 $dQ/T = n C_V (dT/T) + n R (dV/V)$

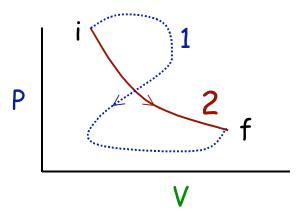
is integrable independent of path.

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This suggests a new state function,

<u>Entropy</u>, defined by:

\Delta S = S_f - S_i = \int_i^f \frac{dQ}{T}
(Valid for any system)
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In general, the process may be too complicated to do the integral (particularly if irreversible process):



However, because entropy is a state function, we can choose any convenient path between i and f to integrate.

For an ideal gas:

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\Delta S = n C_V \ln(T_f/T_i) + n R \ln(V_f/V_i)
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This only depends on the initial state (V_i, T_i) and final state (V_f, T_f) , but not the path.

<u>Isothermal Expansion</u>: $T_f = T_i, V_f > V_i$

The amount of heat which leaves the reservoir and enters the gas is

 $Q = n R T ln(V_f/V_i).$

The entropy change of the gas is

 $\Delta S_{gas} = + Q/T = n R \ln(V_f/V_i).$

The entropy change of the reservoir is

 $\Delta S_{reservoir} = -Q/T.$

The net entropy change is

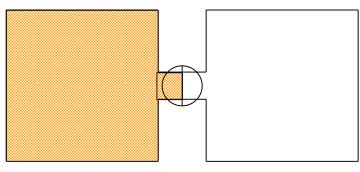
 $\Delta S_{universe} = \Delta S_{gas} + \Delta S_{reservoir} = 0.$

This illustrates a general result:

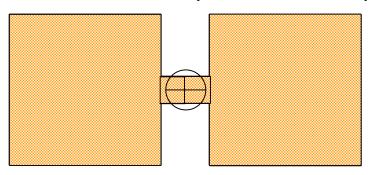
In a reversible process, the entropy change of the universe (system + surroundings) is zero.

Adiabatic Free Expansion of an Ideal Gas

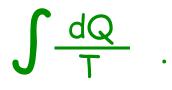
Two containers connected by stopcock. They are thermally insulated so no heat can flow in or out.



<u>Initial</u>: One container is evacuated. Gas is in volume V_i at temperature T_i



<u>Final</u>: Stopcock opened, gas rushes into second chamber. Gas does no work (nothing to push against) and there is no heat transfer. So internal energy does not change. Final volume $V_f > V_i$ at temperature $T_f = T_i$. Because there is no heat transfer, you might think $\Delta S = 0$. WRONG! This is an irreversible process. We can't integrate



But entropy is a state function, and we do know the initial and final conditions for the Free Expansion. They are exactly the same as for an Isothermal Expansion. So

$\Delta S_{gas} = n R \ln(V_f/V_i).$

just as for an isothermal expansion. However, since it is thermally isolated from its surroundings,

 $\Delta S_{surround} = 0$ and $\Delta S_{universe} = \Delta S_{gas} + \Delta S_{surround} = n R \ln(V_f/V_i)$ > 0.

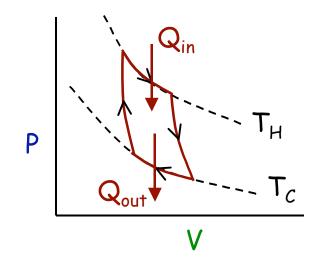
In an irreversible process, the entropy of the universe increases.

Entropy and Heat Engines

For a reversible cycle:



This implies that dQ cannot be strictly positive. There must also be heat released in the cycle.



Carnot cycle: $(Q_{in}/T_H) + (-Q_{out}/T_C) = 0.$

 2^{nd} Law of TD (Entropy form): $\Delta S_{universe} \ge 0.$ (greater-than sign for irreversible processes, and equals sign for reversible processes)