

## Summary of Chapter 20 – Induced Voltage and Inductance

Please read Chapter 20 carefully, and make sure that you understand the summary points below.

- ▶ The magnetic flux,  $\Phi$ , through a planar surface is defined as

$$\Phi = BA \cos \theta$$

where  $B$  is the strength of the uniform magnetic field,  $A$  is the cross-sectional area of the surface, and  $\theta$  is the angle between  $\mathbf{B}$  and the direction perpendicular to the plane.

- ▶ **Faraday's law of induction** states that the instantaneous emf induced in a circuit equals the rate of change of magnetic flux through the circuit:

$$\text{emf} = -\frac{\Delta\Phi}{\Delta t}$$

where  $\Phi$  is the flux through the surface enclosed by the circuit.

- ▶ **Lenz's law** states that the polarity of the induced emf is such that it produces a current whose magnetic field opposes the change in magnetic flux through the circuit.

- ▶ If a conducting bar of length  $C$  moves through a magnetic field with a speed,  $v$ , so that  $\mathbf{B}$  is perpendicular to the bar, the emf induced in the bar, often called a motional emf, is

$$\text{emf} = BLv$$

- ▶ When a coil of wire with  $N$  turns, each of area  $A$ , rotates with constant angular speed  $\omega$  in a uniform magnetic field  $\mathbf{B}$ , the emf induced in the coil is

$$\text{emf} = NAB\omega \sin \omega t$$

- ▶ When the current in a coil changes with time, an emf is induced in the coil according to Faraday's law. This self-induced emf is defined by the expression

$$\text{emf} = -L \frac{\Delta I}{\Delta t}$$

where  $L$  is the inductance of the coil. The SI unit for inductance is the henry;  $1 \text{ H} = 1 \text{ Vs/A}$ .

- ▶ The inductance of a coil can be found from the expression

$$L = \frac{N\Phi}{I}$$

where  $N$  is the number of turns on the coil,  $I$  is the current in the coil, and  $\Phi$  is the magnetic flux through the coil produced by that current.

- ▶ **RL circuit.** If a resistor and inductor are connected in series to a battery and a switch is closed at  $t = 0$ , the current in the circuit does not rise instantly to its maximum value. After one time constant,  $\tau = L/R$ , the current in the circuit is 63% of its final value,  $\text{emf}/R$ .

- ▶ The **energy stored** in the magnetic field of an inductor carrying current  $I$  is

$$U_L = \frac{1}{2} LI^2$$