
PHY492: Nuclear & Particle Physics

Part II

Lecture 19

QCD




Deep inelastic lepton scattering
Time evolution of Neutrino species

QCD basics

- Quarks in three colors

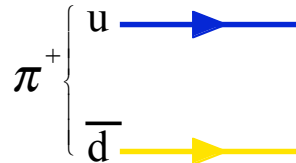
- red 
- green 
- blue 

- Antiquarks in three anticolors

- anti-red 
- anti-green 
- anti-blue 

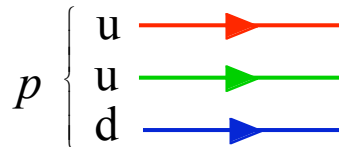
- Mesons

- quark-antiquark pair
- color-anticolor



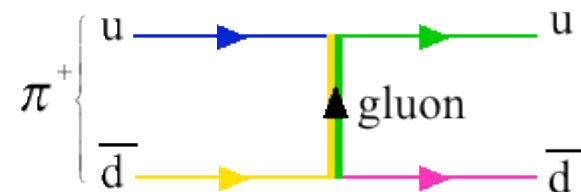
- Baryons

- 3 quarks
- 3 different colors



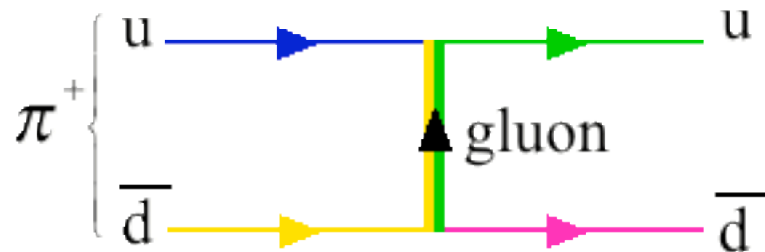
- Strong (color) force between quarks is due to **gluon** exchange

- gluon has no electric charge or flavor
- gluon carries a color-anticolor pair
- exchange changes **only** quark colors
- in mesons gluon changes both colors



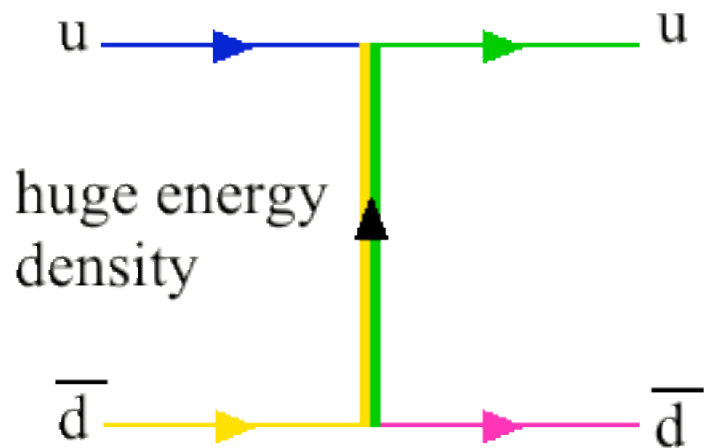
QCD force

- Pi meson



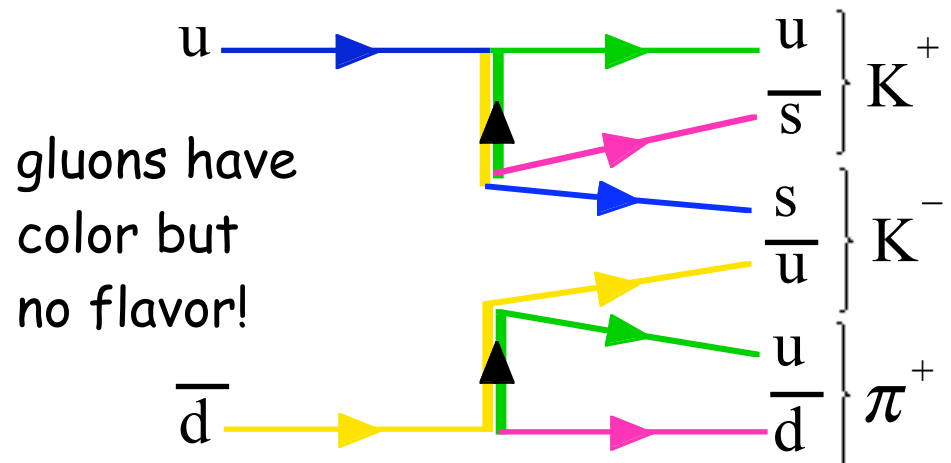
- Attempt to free the quarks

- force grows with separation
 - huge field energy density
- INSTEAD



- Gluon \rightarrow quark-antiquark pair

- tail end splits to a $s \bar{s}$
- head end to $u \bar{u}$
- gluons conserve flavor
- must split to $q \bar{q}$ (same flavor)



Quarks and gluons point-like within hadrons

- Parton (Feynman's term) model of hadrons remains with us, replacing partons with quarks and gluons.
- Electron scattering on hydrogen and deuterium targets.

$$\nu = E - E'$$

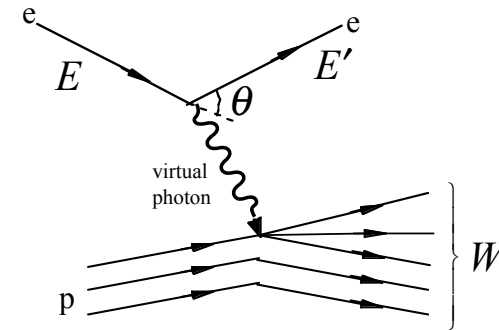
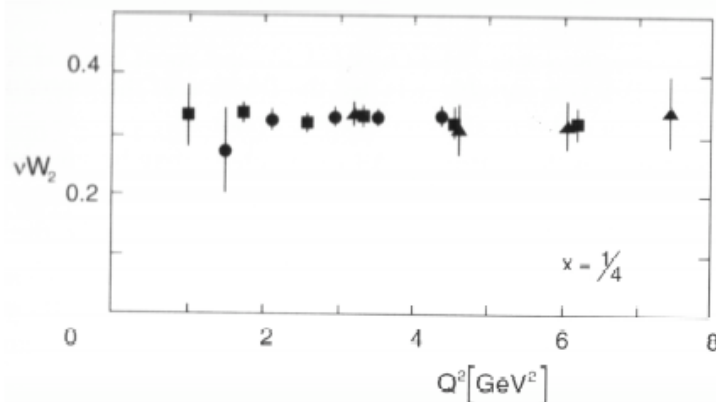
$$Q^2 = 4EE' \sin^2(\theta/2)$$

- Bjorken scaling variable:

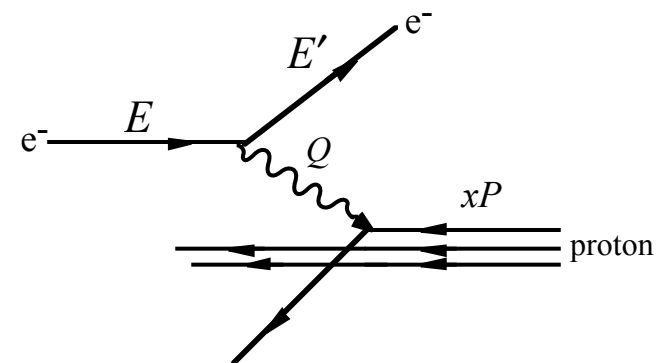
$$0 < x < 1$$

$$x = \frac{Q^2}{2m_p \nu}$$

- If there are partons, cross sections at fixed x independent of Q^2



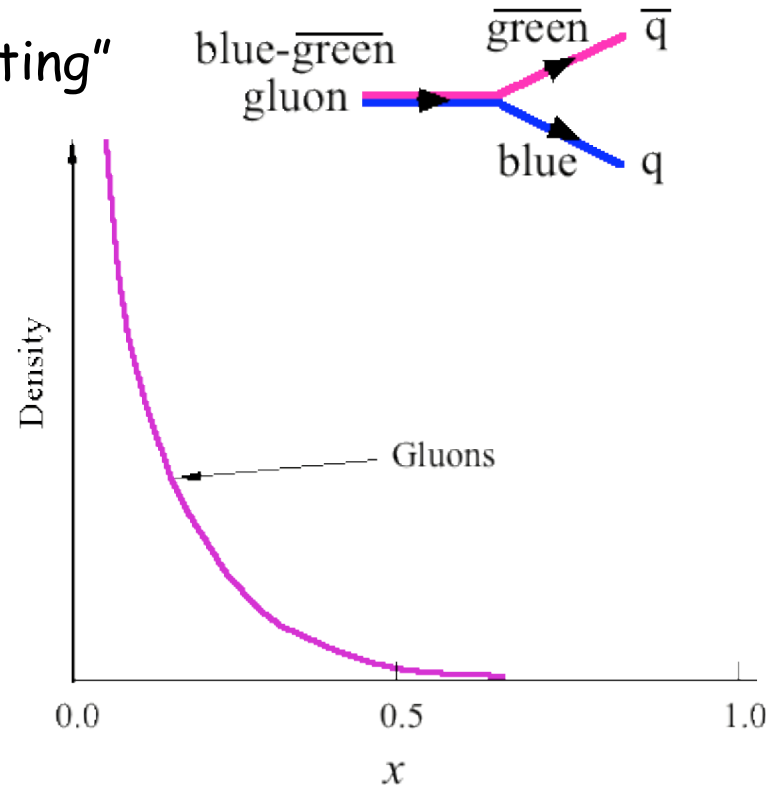
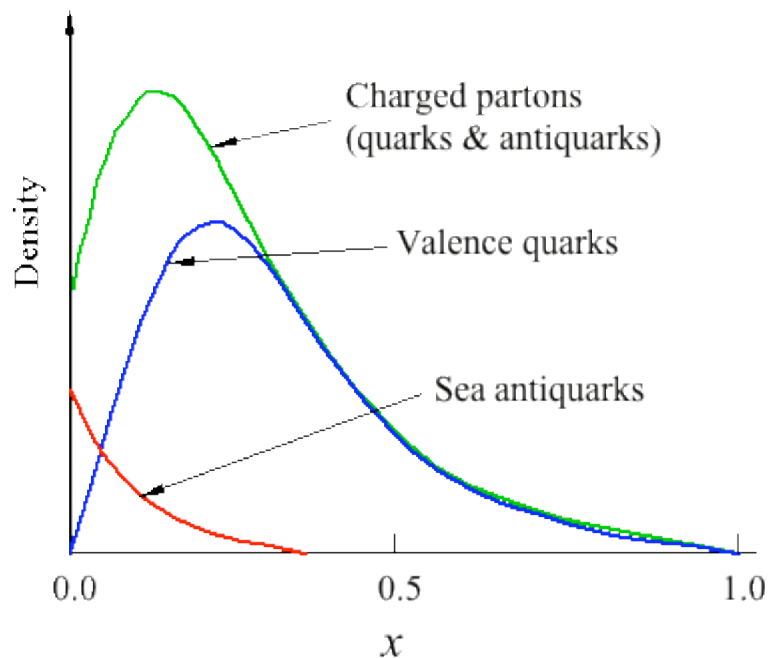
Viewed from infinite momentum frame



Parton distribution functions in the proton

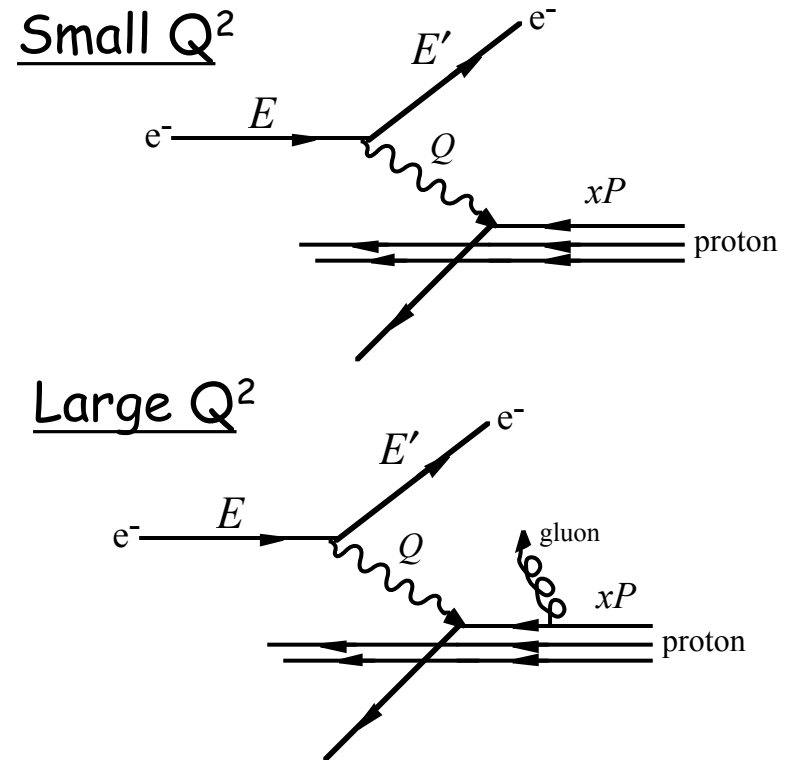
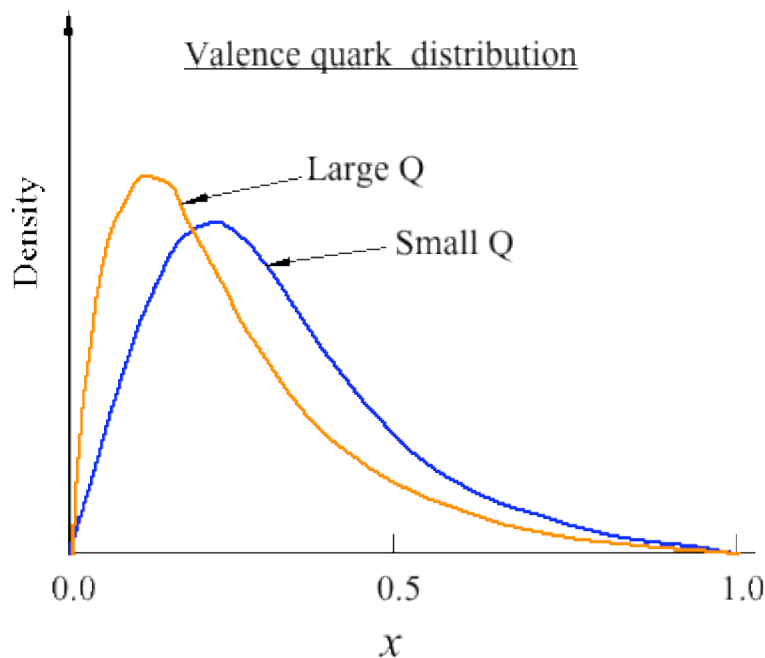
"Valence" "Sea"

- Proton "parton" content is $u u d + (q \bar{q} \text{ pairs}) + \text{gluons}$
- At $Q \sim 5 \text{ GeV}/c$, proton is 50% quarks and 50% gluons
- Sea quarks are from gluon "splitting"



Scaling violations

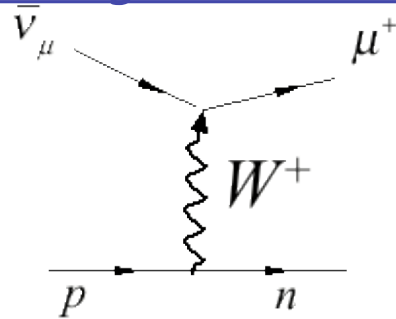
- Full QCD calculations predict deviations from scaling at large Q^2
 - Large Q^2 means a "hard virtual photon"
 - Large Q^2 kicks quark out before it can "catch" radiated gluons.
 - Observed gluon fraction increases for large Q^2 .



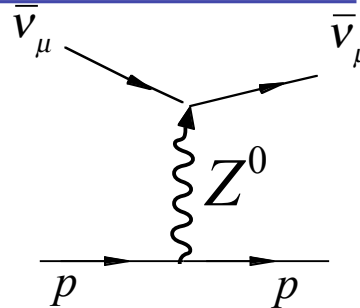
Weak neutral currents

- In addition to W^+, W^- bosons, there is a neutral version, Z boson.
- As seen earlier, there is a cancellation of weak neutral currents in weak decays due to the symmetry of the CKM matrix
- The absence of weak neutral currents lead some to believe they were absent. Neutrino scattering experiments proved them wrong.

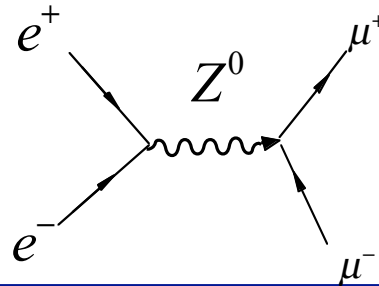
Charged current



Neutral current



- CERN sps collider finished it off by producing them in hadronic collisions. However, the prettiest production is in e^+e^- collisions.



Neutrino mass

- Many attempts to see if neutrinos have mass
 - Tritium beta decay end-point
 - electron neutrino mass $< 3 \text{ eV}/c^2$
 - Meson decays
 - muon neutrino mass $< 200 \text{ keV}/c^2$
 - tau neutrino mass $< 18 \text{ MeV}/c^2$
 - Cosmological limits
 - lots of assumptions about big bang
 - nuclear-synthesis, more assumptions
 - (number density) \times (mass) in universe constraint
 - neutrino masses $< 1 \text{ eV}$
- Theoretical bias for non-zero neutrino mass
 - Why are all neutrinos left-handed?
 - What happened to all the right hand neutrinos?
 - "See-Saw" mechanism
 - right hand neutrinos forced to be VERY MASSIVE
 - and left hand neutrinos to be very light (but not zero).

Propagation of neutrino mass states

- Remember, Schrodinger wave equation solutions ?
- Remember, time dependent Schrodinger wave equation solutions ?

$$e^{-i(\omega t - kx)}; \quad \omega = \frac{E}{\hbar}; \quad k = \frac{p}{\hbar}$$

$$\psi(x, t) = \psi(x, 0) e^{-\frac{i}{\hbar}(Et - px)}; \quad \text{let } x = L, \quad t = L / c$$

$$\psi(L) = \psi(0) e^{-\frac{i}{\hbar c}(E - pc)L}$$

$$\psi(L) = \psi(0) e^{-\frac{i}{\hbar c} \frac{m^2 c^4}{2E} L}$$

$$pc = E \sqrt{1 - \frac{m^2 c^4}{E^2}} \approx E - \frac{m^2 c^4}{2E}, \quad E \gg mc^2$$

$$E - pc \approx \frac{m^2 c^4}{2E}$$

- Phase factor $e^{-\frac{i}{\hbar c} \frac{m^2 c^4}{2E} L}$ depends on distance L from production, particle energy, and mass **squared !!**