

Greek Astronomy / Motions of the sky

- Erathosthenes' measurement of the Earth
- Hipparchus' measurement of distance to the moon
- Motions of the sky that we have seen with our naked eyes. A model to explain the motions.

- Homework 1
 - Due Mon, Sept 14. (Delayed one class.)
 - Missouri Club on Fri, Sept 11. Show me ...
 - You may work with your Ast207 buddies, but you must write your own homework. (No copies.)

Erathosthenes ~200 BC

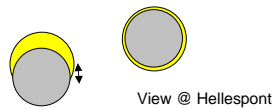
- A correspondent in Syene reports that at noon on the summer solstice, the sun illuminates the bottom of a well. In Alexandria (where Erathosthenes lived), a stick makes a 7° shadow.
- It takes a camel 50 days to travel from Syene to Alexandria. A camel can travel 100 stadia/day.
 1. The distance between Alexandria & Syene is 500 km?
 2. Draw a picture to show the relationship between the sun, the well, the stick, and the two locations. "A clear picture is 90% of clear thinking."
- Picture shows Alexandria & Syene are 7° apart in latitude.
- The circumference is 360° around Earth
 - 500km
 $\times 360^\circ / 7^\circ = 25,000\text{km}$
- Actual circumference is 40,000km.

Hipparchus measures the moon's distance ~200BC

- At the Hellespont, the solar eclipse of 189BC was total. (Sparta defeated Athens there in 405 BC.)
- In Alexandria, the moon covered $\frac{3}{4}$ of the sun. Alexandria is 1000km from the Hellespont.
- The diameter of the sun is $\frac{1}{2}$ degree. In Alexandria, the angle between the sun and moon is $\frac{1}{4} * \frac{1}{2} = \frac{1}{8}$ degree.
- "A clear picture is 90% of clear thinking."
- Draw a picture to show the relationship between the sun, the moon, the two locations, and the angle between the sun and moon in Alexandria.



<http://www.livius.org>

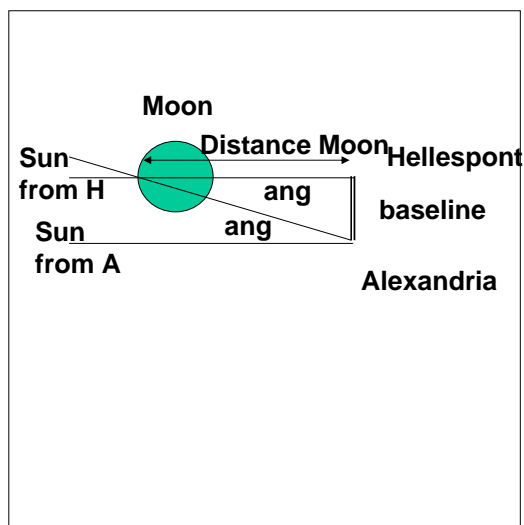


View in Alexandria.
Moon is offset by $\frac{1}{4}$ diameter of sun

http://mkatz.web.wesleyan.edu/medea_lecture/hellespont.gif

- Parts of triangle
 - Angle is due to parallax: moon in foreground shifts with respect to sun in the background.
 - One leg of triangle is the baseline.
 - Other leg is distance to moon.
- Small-angle approximation
 - Angle = Baseline/Distance
 - Angle must be in radians
 - 180° in π rad
 - $57^\circ/\text{rad}$
- Find distance
 - Distance = Baseline/Angle

What triangle did Hipparchus use?



- Small-angle approximation

Angle = Baseline/Distance

- Angle must be in radians
 - 180° in π rad
 - 57° /rad

1. From Alexandria to the Hellespont, the angle between the sun and moon shifts by $1/8^\circ$. What is the shift in radians? Explain how to do this without remembering a formula.

- A. $1/8$ rad
- B. $57/8 = 6$ rad
- C. $1/8/57=1/440$ rad

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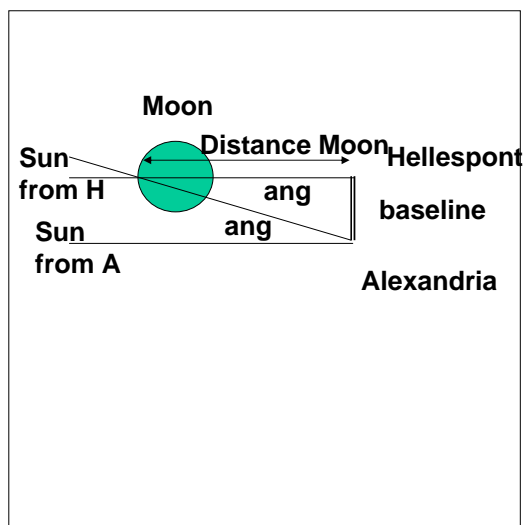
- Find distance

Distance = Baseline/Angle

angle = $1/440$ rad

$D = 1000\text{km} \cdot 440 = 440,000\text{km}$

What triangle did Hipparchus use?



Changes in the Sky

- Name two motions of objects in the sky or changes in the sky that you have observed.

Changes in the Sky

- The sun sets south of west in winter.
- Winter days are short.
- Stars move east to west over a night.
- The constellations change over the months.
- The sun (and moon and stars) rises & sets.
- The sun is higher in the sky in summer than winter.
- Planets move with respect to the stars.
- Comets appear irregularly.