

Kepler's Laws



Kepler at 39, Sternwarte Kremsmünster
<http://members.nextra.at/stewar/>

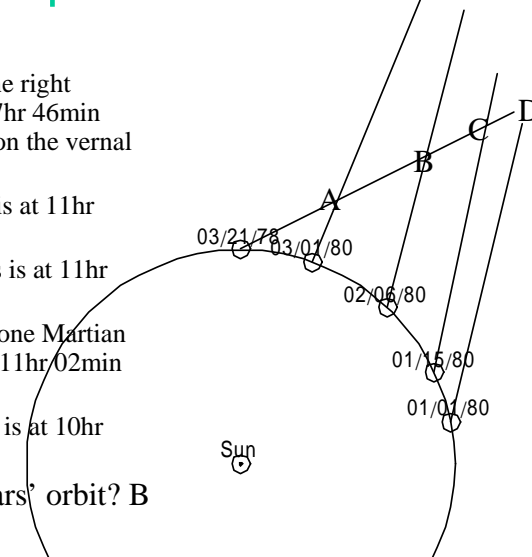
- Hwk1: max is 28
 - If you want a question regraded, write a note on the front & give me the paper.
- Figure added to Homework 2
 - See link on syllabus
- Read pages in Galileo's *Starry Messenger* for Mon
 - See link on syllabus
 - How & when did Galileo know that he had discovered moons of Jupiter?
- The discovery of the laws of motion, the first science.
 - *De Revolutionibus Orbium Coelestium*, Copernicus, 1543
 - *Astronomia Nova*, Kepler, 1609
 - *Philosophiae Naturalis Principia Mathematica*, Newton, 1687
- How Kepler figured out the path of Mars from Tycho's observations.
- Kepler's three laws.

Copernicus	1473–1543
Columbus sails	1492
Tycho Brahe	1546–1601
Shakespeare	1564–1616
Johannes Kepler	1571–1630
Jamestown	1607
King James Bible	1611
Harvard College	1636
Isaac Newton	1642–1727

Determining one point on Mars' orbit

- Observations
 - On 21 March 1978, the right ascension of Mars is 7hr 46min (116.5° from the sun on the vernal equinox).
 - On 1 Jan 1980, Mars is at 11hr 06min (166.5°).
 - On 15 Jan 1980, Mars is at 11hr 12min (168.0°).
 - On 6 February 1980 (one Martian year later), Mars is at 11hr 02min (165.5°).
 - On 1 Mar 1980, Mars is at 10hr 30min (157.5°).

1. Which point is on Mars' orbit? B



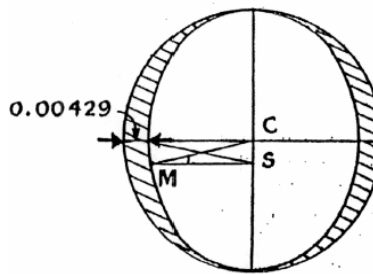
Kepler Solves Mars Orbit

- Kepler's *Astronomia Nova*, 1609, in *Sleepwalkers*, by A. Koestler.
- Kepler describes the orbit: "The conclusion is simply that the planet's path is not a circle—it curves inward on both sides and outward again at opposite ends. Such a curve is called an oval. The orbit is not a circle, but an oval figure." —Ch. 44
- "What happened to me confirms the old proverb: a bitch in a hurry produces blind pups... But simply I could not think of any other means of imposing an oval path on the planets. When these ideas fell upon me, I had already celebrated my new triumph over Mars without being disturbed by the question whether the figures tally or not." —Ch. 45



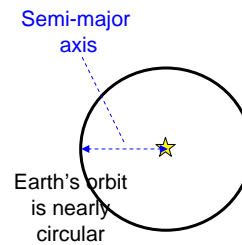
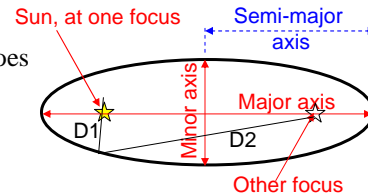
Kepler discovers Kepler's First Law of Planetary Motion

- "... I was wondering why and how a sickle of just that thickness (0.00429) came into being. While this thought was driving me around, while I was considering again and again... that my apparent triumph over Mars has been in vain, I stumbled entirely by chance on the secant of the angle $5^{\circ} 18'$, which is the measure of the greatest optical elongation. When I realized that this secant equals 1.00429, I felt as if I had been awakened from a sleep..." —Ch. 45 (a year's work later)



Kepler's First Law of Planetary Motion 1605

- The path of a planet is an ellipse.
 - Ellipse is figure for which $D1+D2$ does not change
 - The sun is at one focus.
 - Eccentricity = (dist between foci)/(major axis)
- Modern extension
 - The path of an object controlled by the sun's gravity is an ellipse, parabola, or hyperbola.
 - The sun is at one focus.



Kepler's Second Law 1602

- The line joining the planet and the sun sweeps out equal areas in equal amounts of time
 - Planet moves slowly when it is far from sun
 - Planet moves rapidly when close to sun

Kepler2ndLaw

Third Law 1618

- The size and periods of the planetary orbits are related by
$$P^2 = a^3$$
 - where P is the period in years and
 - a is the half of the major axis in astronomical units
- 1. A 10th object (planet?) was found beyond the orbit of Pluto. ___ has the shorter period.
 - A. Pluto
 - B. 10th object
 - C. Not enough information to answer

3rd Law

<http://web.cuug.ab.ca/~kmcclary/fastSolar.html>

Questions concerning Kepler's Laws

- K1: A planet's path is an ellipse with the sun at one focus.
- K2: A planet "sweeps" out the same area in an equal amount of time.
- K3: The planets' periods P and semi-major axes a are related by
$$P^2 = a^3$$
- A planet, which has an almost circular orbit, and a comet, which has a highly elliptical orbit, have the same periods. Draw their orbits on a single picture.
 1. Grading: sun's position
 2. Grading: lengths of major axes.

Questions concerning Kepler's Laws

- A planet's path is an ellipse with the sun at one focus.
 - A planet "sweeps" out the same area in an equal amount of time.
 - The planets' periods P and semi-major axes a are related by $P^2 = a^3$
- A planet, which has an almost circular orbit, and a comet, which has a highly elliptical orbit, have the same periods. Draw their orbits on a single picture.
 1. Grading: sun's position
 - A. Centered for comet
 - B. Offset for comet
 2. Grading: lengths of major axes.
 - A. Same for both
 - B. Different