

Fusion Powers the Sun—12 Oct

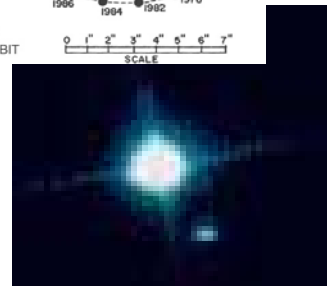
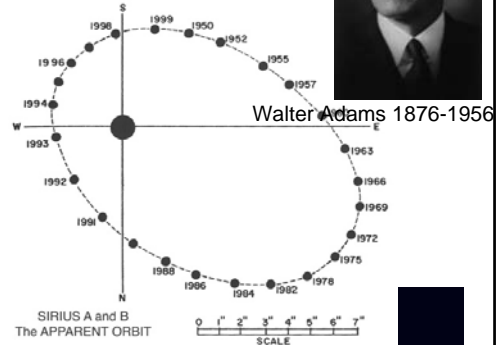
- Finish Walter Adams & white dwarfs
- Big questions
 - What powers the sun?
 - Where does carbon come from?
 - How long does the sun live?
 - What happens to the sun when it dies?
- Lifetime of the sun
 - Chemical reactions
 - Gravitational energy
 - Nuclear fusion
- Fusion
 - $4\text{H} \rightarrow ^4\text{He}$



- Course grade is on angel.
 - Weights: Hwk 25%, Clicker 9%, Test 1 64%
 - Set so that the relative weights of hwk, clicker, & tests are the same as at the end of the term.
 - Lowest hwk & lowest 2 clickers are dropped.
 - 85% of the final course grade is in the future.
- Test 2 is Wed, Oct 21.
 - Covers material though Adams' discovery of white dwarfs (today).
 - One cheat sheet.
- Hwk 5 is due at start of class on Mon, Oct 19. No late papers.

Sirius A and Sirius B (from 9/11)

- We are Walter Adams of the Mt. Wilson Observatory in 1914. We are studying the double star Sirius A and B. (Sirius A & B orbit each other.)
- Sirius B is much fainter than Sirius A.



http://chandra.harvard.edu/photo/2000/0065/0065_optical.jpg



1. Sirius B may be faint for two reasons. It may be small or it may be
 - A. farther away
 - B. closer
 - C. cooler
 - D. hotter



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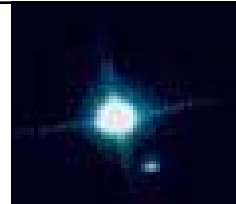


1. Sirius B may be faint for two reasons. It may be small or it may be
 - A. farther away
 - B. closer
 - C. cooler
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- Adams found that Sirius A and B have about the same color. Therefore Sirius B is smaller.



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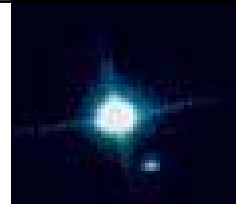
Sirius A and Sirius B



- Adams found that Sirius A and B have about the same color. Therefore Sirius B is smaller.
 - $L=R^2T^4$
 - How much smaller is Sirius B?
 - Apparent mag of Sirius A is -1.5
 - Apparent mag of Sirius B is 8.7
1. The mag of Sirius B is approximately ___ steps of 2.5 fainter than that of Sirius A.
 - A. 4
 - B. 5
 - C. 6
 - D. 10
 2. The flux of Sirius B is approximately ___ fainter.
 - A. a factor 10
 - B. a factor of 100
 - C. a factor of 1000
 - D. a factor of 10,000.

http://chandra.harvard.edu/photo/2000/0065/0065_optical.jpg

Sirius A and Sirius B



- Adams found that Sirius A and B have about the same color. Therefore Sirius B is smaller.
 - $L=R^2T^4$
 - How much smaller is Sirius B?
 - Apparent mag of Sirius A is -1.5
 - Apparent mag of Sirius B is 8.7
1. The mag of Sirius B is 4 steps of 2.5 fainter than that of Sirius B.
 2. The flux of Sirius B is approximately 10,000 fainter.
- The radius of Sirius B is 1/100 that of Sirius A.
 - Sirius B is about the size of the Earth.

http://chandra.harvard.edu/photo/2000/0065/0065_optical.jpg

Summarizing question

- Why was finding of Sirius B's spectral class crucial to discovery of white dwarfs?

Energy production in stars

- Big questions
 - What powers the sun?
 - Where does carbon come from?
 - How long does the sun live?
 - What happens to the sun when it dies?
- Lifetime of the sun
 - Chemical reactions
 - Gravitational energy
 - Nuclear fusion
- Fusion

19th Century “Energy Crisis”

- Luminosity of sun $L=4\times 10^{26}$ Watt
- Mass $m=2\times 10^{30}$ kg
- How long will the sun last if the energy is produced by burning coal? $C+O_2\rightarrow CO_2$
 - Life time = $m\times(E/m)/L$
 - $E/m=9$ MJ/kg
 - 1500 years
- Earth is much older than that.

Extract Energy from Gravity

- Luminosity of sun: $L=4 \times 10^{26}$ Watt
- Mass $m=2 \times 10^{30}$ kg
- How long will the sun last if the energy is produced by the sun contracting?
- If material falls from R_{sun} to $0.9R_{\text{sun}}$,
 - Energy = $\frac{1}{2} m v^2 = m g h = m (GM_{\text{sun}}/R_{\text{sun}}^2)(0.1R_{\text{sun}})$
 - Life time = $m \times (E/m)/L$
 - 1.6 Million years
- Kelvin's calculation includes material falling not just on surface. Got 100 Myr.
 - Kelvin thought earth could be this old, but later in 19th century, age of earth was shown to be much larger.



William Thomson
Lord Kelvin
1824-1907
www-history.mcs.st-andrews.ac.uk/history/PictDisplay/Thomson.html

$E=mc^2$

- Crisis: No solution with physics of 19th century.
- Einstein's new theory (1906)
 - Energy can change into mass, and mass can change into energy.
 - $E = m c^2$.
 - Energy = mass \times (speed of light)².
- Changing a little mass produces a lot of energy. Compare kinetic energy $\frac{1}{2} m v^2$ with $m c^2$.
 - Speed of light $c = 300,000$ km/s
 - Air in blast furnace moves at 0.2 km/s
- Chemical reaction $C+O_2 \rightarrow CO_2$
 - $E=m c^2/100,000,000,000$. One part in 100 billion of mass disappears and changes into energy.
- Sun contracts by 10%
 - $E=m c^2/1,000,000$. One part in a million of mass disappears and changes into energy.
- H fuses to produce He
 - $E=m c^2/140$. A part in 140 of the mass disappears and changes into energy.



Nuclear fusion



Hans Bethe
1906-2005

- In a nuclear reaction, converting a significant fraction of the mass to energy is possible.
 - Hans Bethe figured out the nuclear physics of how this happens.
 - $4\ ^1\text{H} \rightarrow\ ^4\text{He} + \text{neutrinos} + 2e^+ + \text{energy}$
 - 4 hydrogen nuclei fuse
 - One helium nucleus is produced
1. Which is heavier? A box of hydrogen and a box of helium, neutrinos, and positrons made from the hydrogen?
- Box containing H
 - Box containing the products: He, neutrinos, and positrons
 - The two boxes have the same mass.

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1906-2005

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- $4\ ^1\text{H} \rightarrow\ ^4\text{He} + \text{neutrinos} + 2e^+ + \text{energy}$
 - 4 hydrogen nuclei fuse
 - One helium nucleus is produced
- $4\ ^1\text{H}$ weighs 0.7% more than $^4\text{He} + \text{neutrinos} + 2e^+$
 - Part of the mass has been converted into energy.
 - Amount of energy is $E=0.007mc^2$. Most of mass remains.
- Life time = $m \times (E/m) / L$
 - $m \times (0.007mc^2/m) / L$
 - 100Byr
 - In reality sun uses 10% of fuel. Lifetime is 10Byr

4 ^1H



$^4\text{He} + 2e^+ + \nu$

Lighter by 0.7%

Proton-proton chain

- Two paths for fusing hydrogen into helium
 - Carbon-nitrogen-oxygen cycle (important in more massive stars)
 - Proton-proton chain (main process in sun)
 - Step 1: Two protons fuse to produce a deuterium nucleus (${}^2\text{H}$), a positive electron, and a neutrino.
$$p+p \rightarrow d+e^++\nu$$
 - Deuterium is an isotope of H with one neutron.
 - A neutrino is almost massless, not charged, and interacts very weakly.
1. Did the number of nucleons change? Charge?
- A. YY
 - B. YN
 - C. NY
 - D. NN

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1. Did the number of nucleons change? Charge?
- Nucleons are conserved (except in some exotic interactions).
 - Charge is absolutely conserved.