

**Baade (1944)**

## Stellar Populations

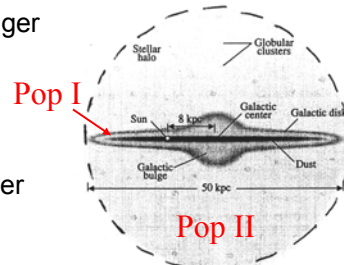
**X, Y, Z = mass fractions**

X ~ 0.73 (H)

Y ~ 0.25 (He)

Z ~ 0.02 (metals)

- Abundances
- Kinematics
- Ages
- Pop I: Metal rich ( $Z \sim 0.02$ ), disk, younger
  - Disk field stars (up to 10-12 Gyr old)
  - Open clusters
  - Gas
  - Star formation regions
- Pop II: Metal poor ( $Z \sim 0.001$ ), halo, older
  - Globular clusters (12-15 Gyr)
  - Halo field stars
  - Bulge??? ....but includes Super Metal Rich (SMR) stars.
- Abundance Determinations
  - Stellar spectroscopy
    - $[Fe/H]$ , etc.  $\rightarrow \log(N_{Fe}/N_H) - \log(\text{solar})$
    - Iron ejected by SNe Ia after about  $10^9$  yrs.
  - Stellar colors
  - HII regions



	<b>[Fe/H]</b>
Thin Disk	-0.5 $\rightarrow$ +0.3
Thick Disk	-0.6 $\rightarrow$ -0.4
Halo	-2.5 $\rightarrow$ -0.8
Bulge	-1.0 $\rightarrow$ +1.0

## Closed Box Model

(and friends and relatives)

Metallicity  
 $Z = M/G$   
 $Z_{\odot} \sim 0.02$

Gas  $\rightarrow$  stars  $\rightarrow$  enriched gas

$S$  = mass of stars

$M$  = mass of metals (heavy elements) in ISM

$G$  = total mass of gas in ISM

Assume instantaneous recycling.

From each new generation of stars:

$dS$  = mass of low mass stars added to  $S$

$p dS$  = mass of heavy elements added to  $M$  from massive stars in this generation.

where  $p$  = yield.

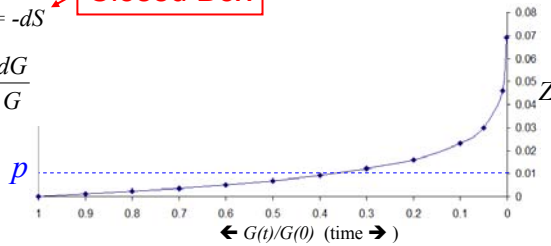
$$dM = p dS - Z dS$$

$$= -p dG + Z dG \quad \text{since } dG = -dS$$

$$dZ = d\left(\frac{M}{G}\right) = \frac{dM}{G} - \frac{M}{G^2} dG = -p \frac{dG}{G}$$

$$Z(t) = -p \ln [G(t)/G(0)]$$

$$G(t) = G(0) e^{-Z(t)/p}$$



Instantaneous recycling

Closed Box

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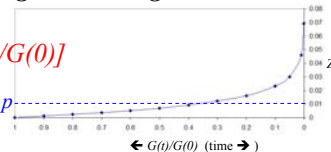
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## G dwarf problem

$$S[Z < Z(t)] = S(t) = G(0) - G(t)$$

$$= G(0) \{ 1 - e^{-Z(t)/p} \}$$

where  $Z(t)$  = gas metallicity at time  $t$

Compare to case when gas had some arbitrary fraction  $\alpha$  of that metallicity:

$$\frac{S[Z < \alpha Z(t)]}{S[Z < Z(t)]} = \frac{1 - X^\alpha}{1 - X}$$

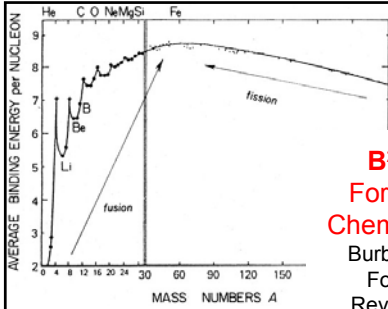
$$\text{where } X = e^{-Z(t)/p} = \frac{G(t)}{G(0)} \sim 0.1 - 0.2$$

Predicts broad distribution in metallicity of stars.

$$\rightarrow S[Z < 1/4 Z_{\odot}] = 0.4 S[Z < Z_{\odot}]$$

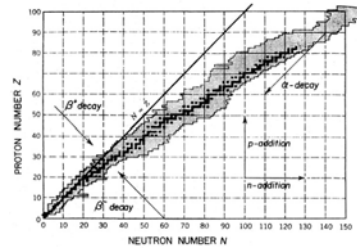
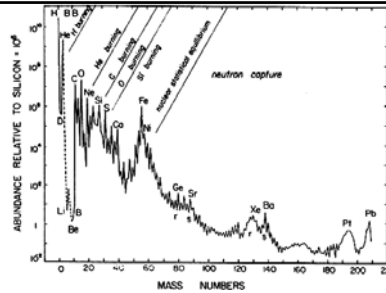
Very different than what is observed in solar neighborhood:

$$S[Z < 1/4 Z_{\odot}] = 0.02 S[Z < Z_{\odot}]$$



**B<sup>2</sup>FH (1957)**  
**Formation of the Chemical Elements**

Burbidge, Burbidge, Fowler & Hoyle.  
 Reviews of Modern Physics, 29, 547.



**Gradual processes in Interiors of Stars**

- H burning ( $4H \rightarrow He$ )
- $\alpha$  process (C,O,Ne,Mg,Si,S...)
- s process
  - slow neutron capture, relative to beta-decay timescale

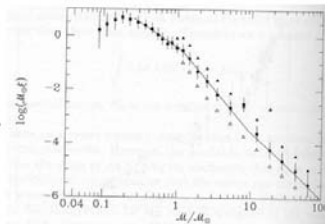
**Supernovae**

- e process
  - nuclear statistical equilibrium
  - iron peak elements
- r process
  - rapid neutron capture

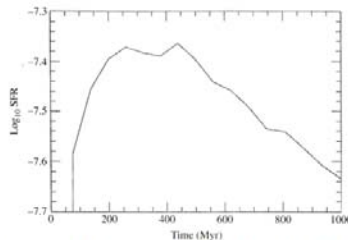
		P PROCESS										R PROCESS	
		N →											
		112	114	115	116	117	118	119	120	121	122	123	124
Sb51										2.8%	4.3%		
Sn50	Z	1.02%	0.69%	0.36%	14.3%	7.6%	24.1%	8.5%	32.5%	27%	4.6%	6.1%	
In49	Z			4.2%		90.8%	15.1%						
Cd48	Z	110	111	112	113	114	116						
		12.2%	12.8%	24.0%	12.3%	28.6%	54%	7.6%					

**The Initial Mass Function (IMF)**

- $dN = N_0 \xi(M) dM$  = number of stars born with masses in range  $M, M+dM$
- Salpeter (1955) IMF:  $\xi(M) \propto M^{-2.35}$
- Scalo (1986) IMF:
  - $\xi(M) \propto M^{-2.45}$  for  $M > 10M_\odot$
  - $\xi(M) \propto M^{-3.27}$  for  $1 < M < 10M_\odot$
  - $\xi(M) \propto M^{-1.83}$  for  $0.2 < M < 1M_\odot$



- Others as well.
- Star Formation rate =  $\psi(t)$
- Stellar birthrate function



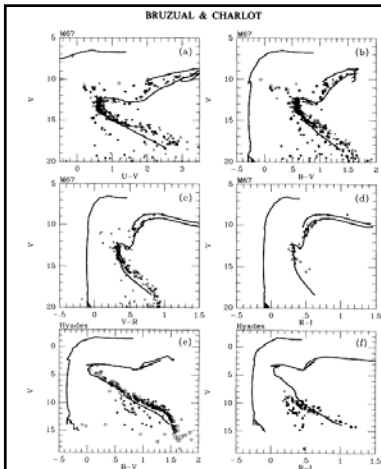
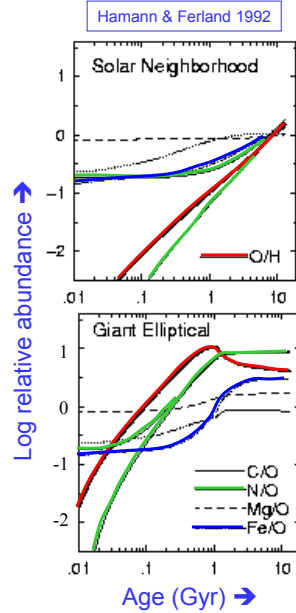
[CO Fig. 26.18]

$B(M,t) = \psi(t) \xi(M) dM dt$

= number of stars born per unit volume with masses in range  $M, M+dM$  in time interval  $t, t+dt$ . [CO eqn. 26.4]

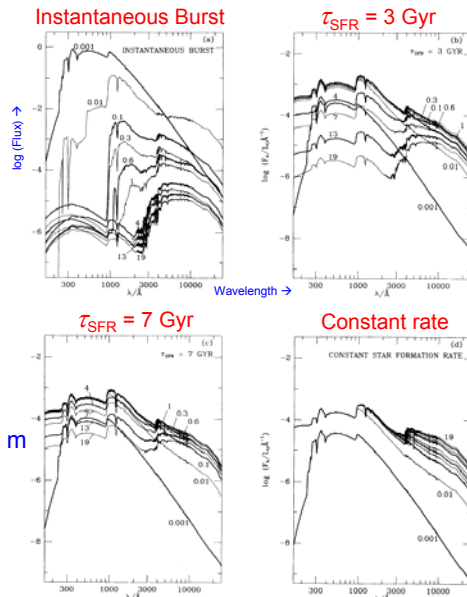
# Modeling chemical enrichment

- One zone, accreting box model.
  - Start with pure H, He mix.
  - Further H, He falls in at specified rate.
- Follow evolution of individual elements H, He, C, N, O, Ne, Mg, Si, S, Ar, Ca and Fe.
- Subdivide stellar population into three classes of stars:
  - $< 1M_{\odot}$  nothing recycled
  - $1.0 - 8.0 M_{\odot}$  fraction give white dwarf supernovae
  - $> 8M_{\odot}$  Core collapse supernovae.
- Assume that each class of stars spews specified % of its mass of each element back into ISM at end of a specified lifetime.
- Must provide IMF to specify mix of star masses.
- Two extreme models:
  - "Solar neighborhood": conventional IMF, slow stellar birthrate, slow infall (15% gas at 10 Gyr).
  - "Giant Elliptical": flatter IMF, 100x higher birthrate, fast infall (15% gas at 0.5 Gyr).



## Population Synthesis Models

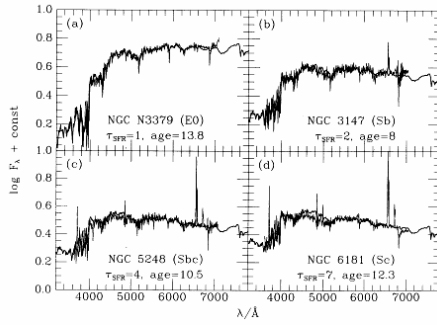
Bruzual & Charlot (1993); Worthey et al (1994)



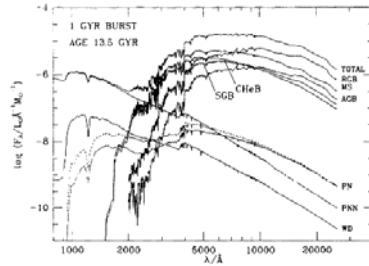
### Ingredients:

- Isochrones = evolution of star of mass  $m$
- IMF = number of stars formed with each  $m$
- $\rightarrow$  evolving composite spectrum  $f_{\lambda}(\tau)$
- Star formation rate  $\Psi(t) = \tau^{-1} \exp(-t/\tau)$
- $F_{\lambda}(t) = \int \Psi(t-\tau) f_{\lambda}(\tau) d\tau$

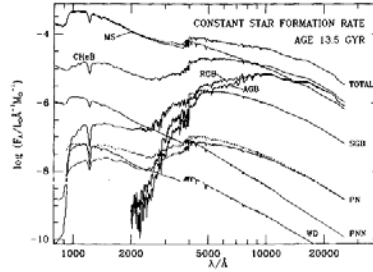
## Some Bruzual & Charlot results



Models fitted to real spectra for different galaxy types.



Components of E galaxy spectrum



Components of late-type spiral galaxy spectrum