

# Cosmology

Thornton and Rex, Ch. 16

# Expansion of the Universe

- 1923 - **Edwin Hubble** resolved Andromeda Nebula into separate stars.
- 1929 - **Hubble** compared radial velocity versus distance for 18 nearest galaxies. He found that on average they were receding with velocity proportional to their distance.

□ Hubble's Law:

$$v = H R$$

$H = \text{Hubble constant} = 72 \text{ km/s/Mpc}$   
(1 pc "parsec" = 3.26 light-years)

- Soon verified with better data from more distant galaxies.

- Radial velocity determined by doppler shift ("red shift").
- Distance is much harder to measure. Requires a "standard candle"-some object in the galaxy whose intrinsic brightness is known, to calibrate the distance. Hubble used a type of variable star called a Cepheid Variable. This is only possible for the most nearby galaxies.
- Hubble constant was uncertain by a factor of 2 until very recently (1998). Supernovae in the more distant galaxies helped pin down H with greater precision.

# General Relativity

1917 - Einstein completed his General Theory of Relativity. He then set out to solve his equations for the universe, assuming it was:

- 1) Isotropic - It looks the same in all directions.
- 2) Homogeneous - It looks the same from any place in the universe.
- 3) Static - It looks the same at all times.

Einstein found no solutions!

He modified his equations by adding a term called "the **Cosmological Constant**".

"My biggest blunder" - Einstein

# General Relativity

Space-time  
Curvature



$$R_{\mu\nu} - g_{\mu\nu} R/2$$

"Curvature  
Tensor"

caused  
by



$$= -8\pi G$$

Newton's  
constant

mass  
(energy)



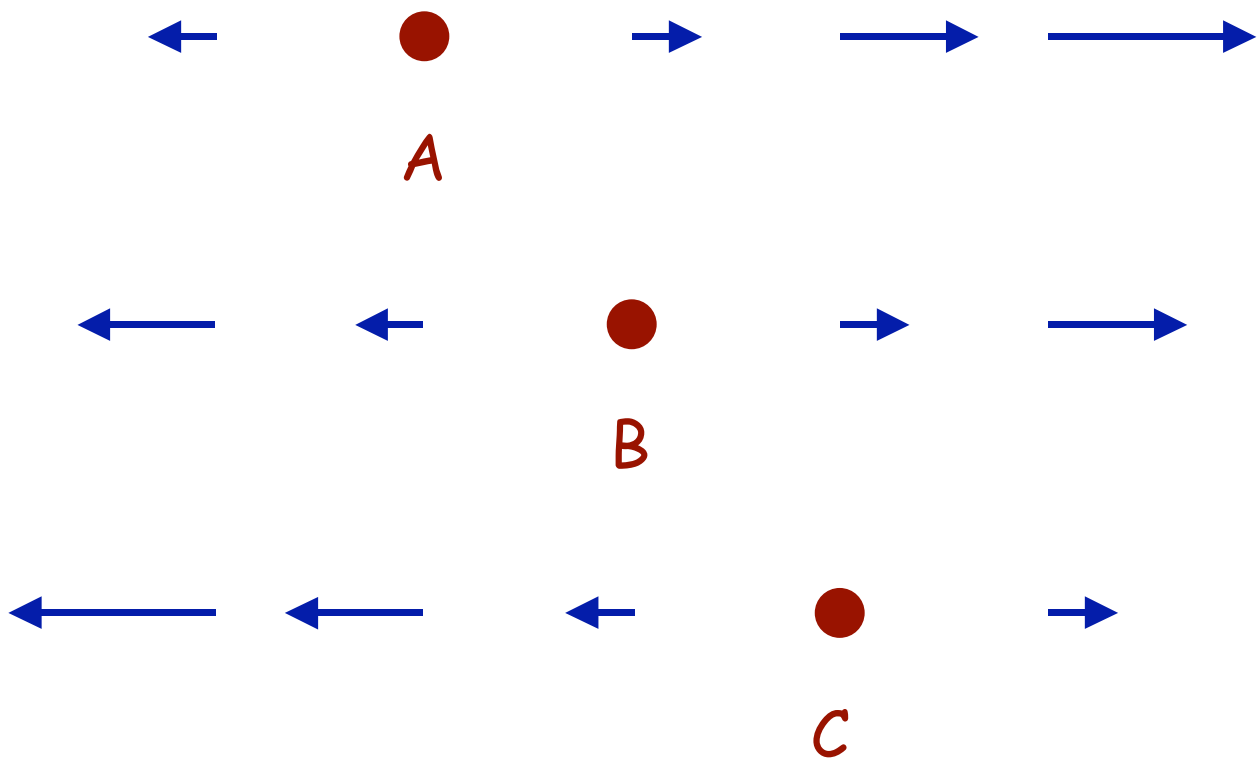
$$T_{\mu\nu}$$

"Energy-  
momentum  
Tensor"

Adding a cosmological constant

$$R_{\mu\nu} - g_{\mu\nu} R/2 = -8\pi G (T_{\mu\nu} - \Lambda g_{\mu\nu})$$

- A few years later Alexandre Friedmann solved Einstein's original equations.

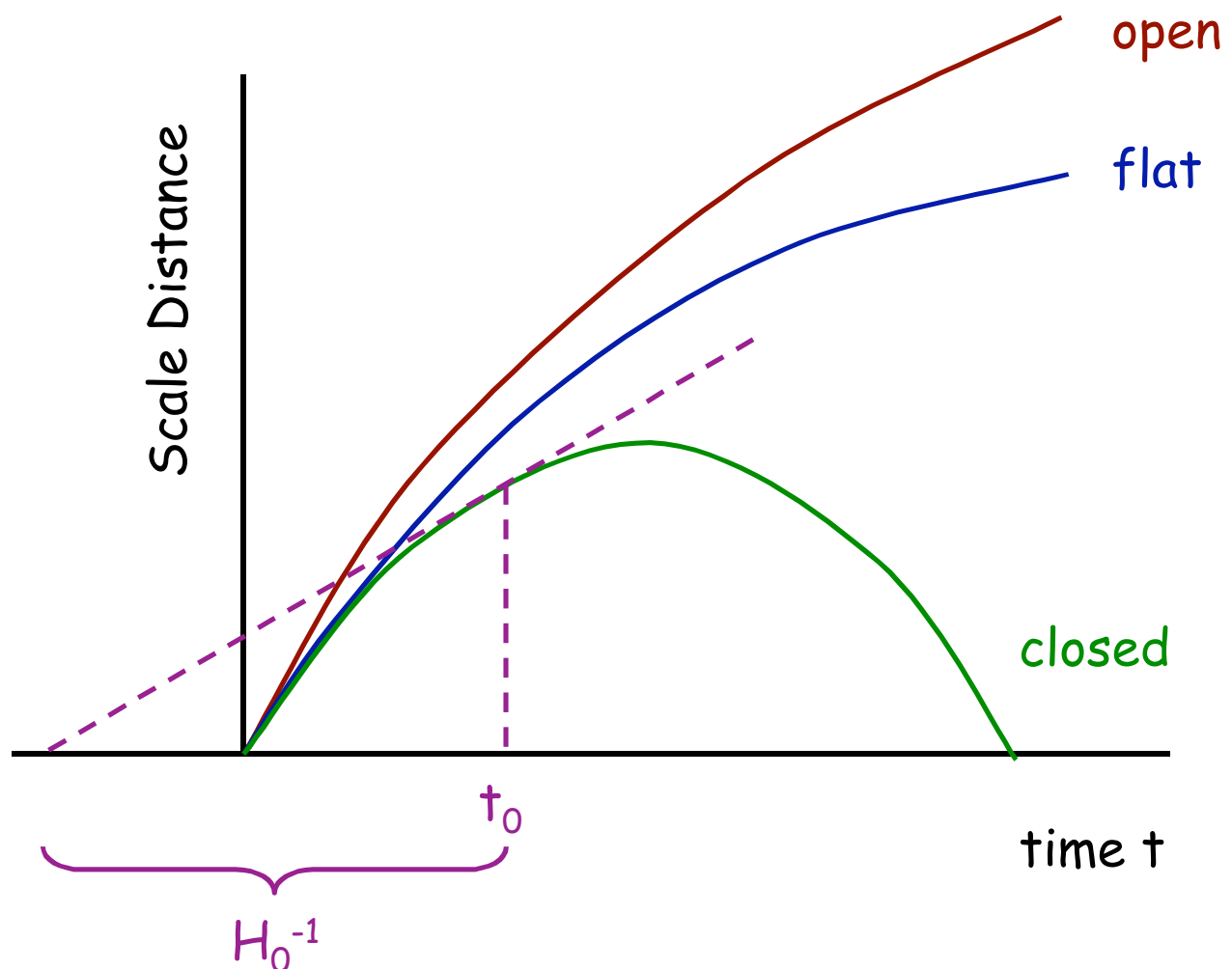


"Homogeneity implies Hubble's Law"

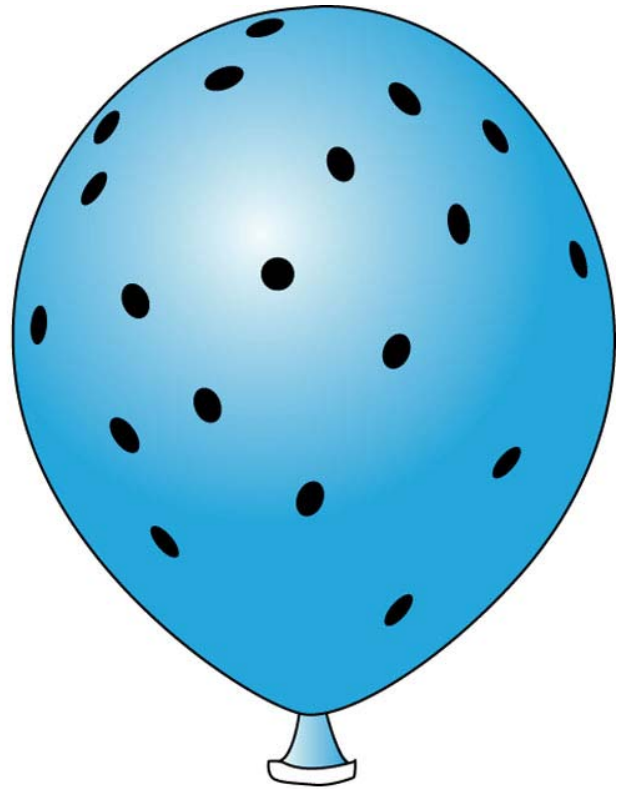
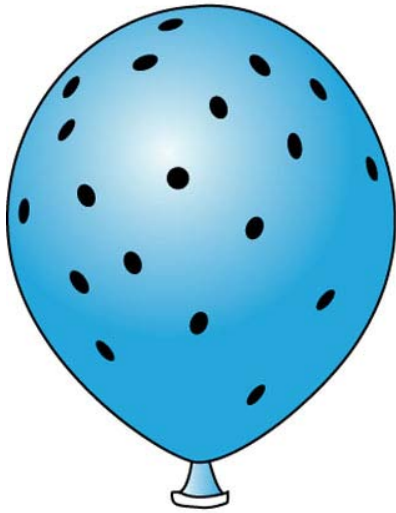
$$v = H R$$

Friedmann found 3 qualitatively different solutions, depending on the density of matter  $\rho$  in the universe:

- 1) Closed universe,  $\rho > \rho_{\text{crit}}$  (finite)
- 2) Open universe,  $\rho < \rho_{\text{crit}}$  (infinite)
- 3) Flat universe,  $\rho = \rho_{\text{crit}}$  (infinite)



# Hubble Expansion of Universe





From the curves, we see

- 1) Hubble constant is constant in space.  
It is not constant in time.  
 $H_0$  is the constant now at time  $t_0$ .
- 2) The equations predict that the universe was a point at some time in the past - "The Big Bang." The age of the universe must be less than

$$(H_0)^{-1} \approx 14 \text{ billion years}$$

The critical density is

$$\rho_{\text{crit}} = \frac{3}{8\pi G} (H_0)^2$$

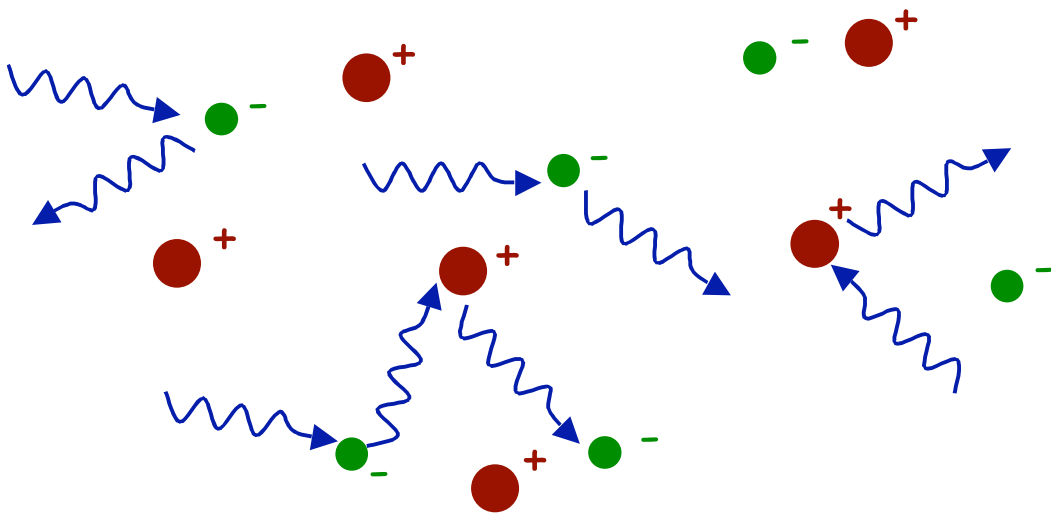
# Cosmic Microwave Background Radiation

- 1964 - Penzias and Wilson discovered radiation coming from the sky, corresponding to a blackbody temperature of 3 K.
- About the same time, Peebles had predicted this radiation as a remnant of the "big bang" and Dicke was setting up an experiment to look for it.
- Dicke's group corroborated the observation of Penzias and Wilson.

(This radiation had been predicted much earlier in the 40's and 50's by calculations of Gamow, Alpher, and Herman.)

# Explanation of the CMB Radiation

- Very early universe, less than  $7 \times 10^5$  years after the "big bang."
  - The energy of photons was high enough to keep electrons and protons from combining into neutral atoms.
- Photons were in thermal equilibrium with charged particles.
- The spectrum of the radiation was a blackbody spectrum with characteristic temperature  $T$ .



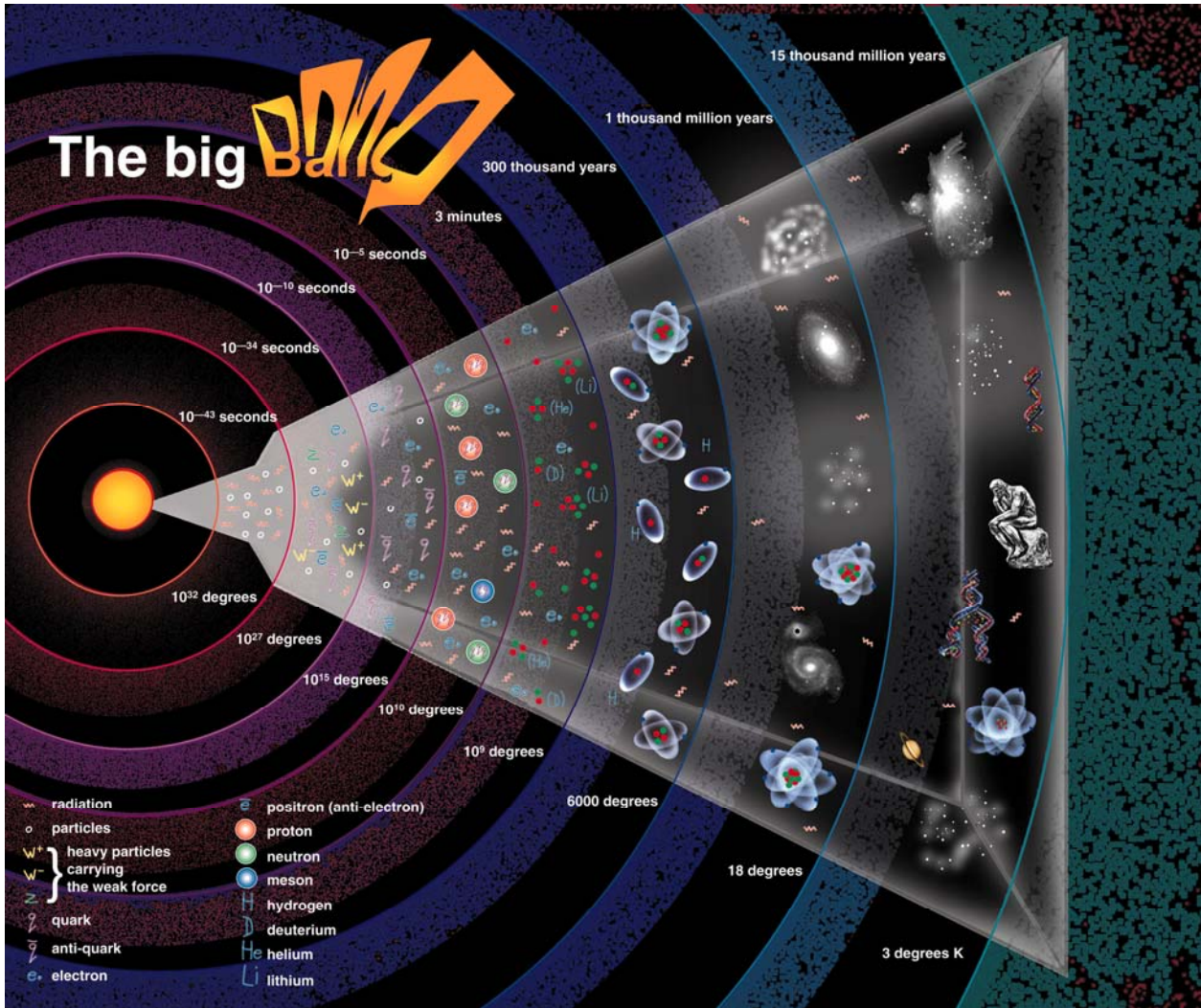
- As the universe expanded, the temperature fell. Around  $T \sim 3000$  K, the average photon energy,

$$E \sim \frac{3}{2} k T \sim \text{less than } 1 \text{ eV},$$

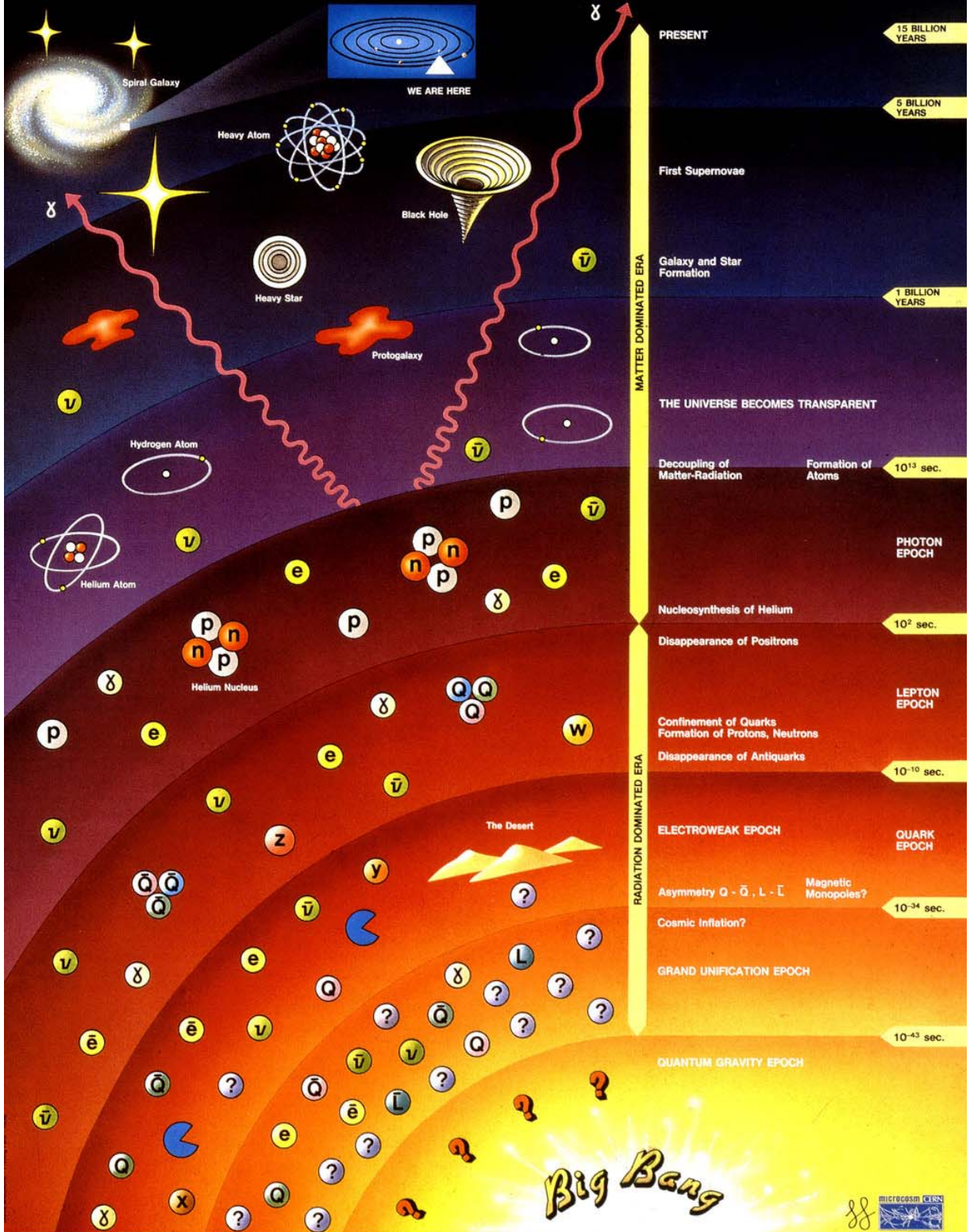
became too small to keep atoms from forming. At that point the universe became transparent, the photons decoupled from matter, and fell out of thermal equilibrium.

- As the universe continued to expand, electromagnetic waves stretch with the universe. The blackbody spectrum remains, but the effective temperature falls.
- We see the spectrum today as a blackbody spectrum at 2.73 K.

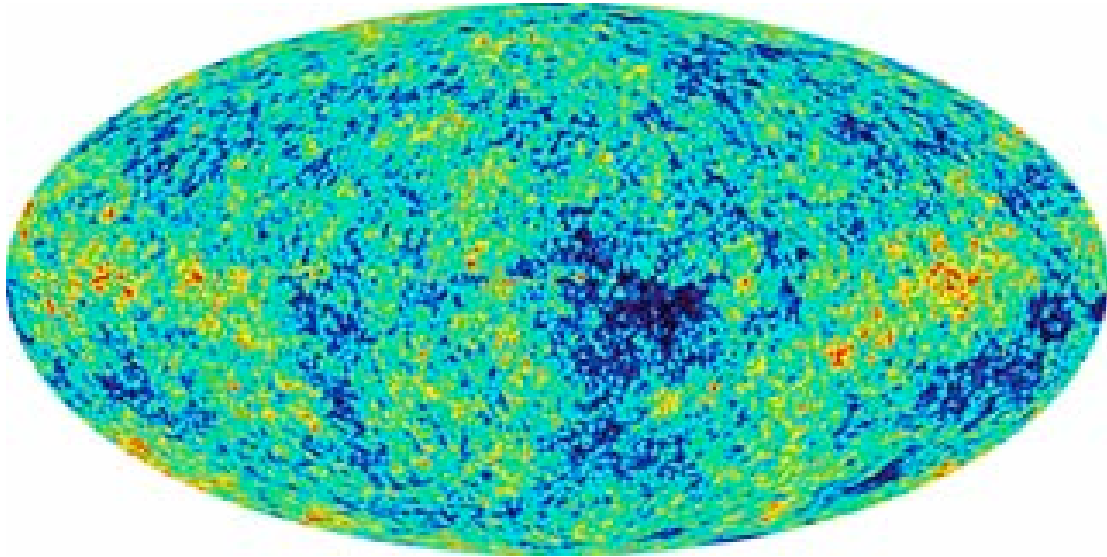
- The radiation is very isotropic (i.e, the temperature changes little in all directions of the sky).
- However, in the early 1990's the Cosmic Background Explorer (COBE) satellite found small deviations. Recently, this has been refined to amazing precision by the Wilkinson Microwave Anisotropy Probe (WMAP).



# History of the Universe



# Wilkinson Microwave Anisotropy Probe (WMAP)



The average temperature of the Microwave Background radiation is 2.73 K. This map shows the tiny fluctuations ( $\Delta T \sim 10^{-6}$  K) around this temperature on the sky.

The fluctuations correspond to "seeds" for structure formation in the early universe.



## Conclusions from WMAP (and others)

The universe is 13.7 Billion Years old.

The universe is flat. It will not re-  
contract.

Only 4% of the universe is made of  
Baryonic matter (essentially atoms).  
The rest is 23% unknown matter  
(called Cold Dark Matter) and 73%  
"Dark energy". The dark energy could  
be Einstein's cosmological constant.

## Open Questions

- Why is the universe flat?
- How can different areas of the universe be in thermal equilibrium, if light has not had time to travel between them? (the "horizon problem")

**Inflation**, a theory where the universe expanded exponentially for a brief period of time, may be able to solve these problems.

- What is the Cold Dark Matter?
- What is the Dark Energy?
- Why is the universe made of matter, but no anti-matter?

