

## Newton's Laws of Motion—22 Jan

- What is the reason for Kepler's three laws?
- Newton's Law of Gravity
- Modern view of Kepler's Laws
  - K1 & K3 can be derived from Newton's laws of motion
  - Emmy Noether: K2 can be derived from fact that laws of physics do not depend on direction.

## Announcements

- Angel homework
  - Homework 2 is due Thurs, 1/29, at 6:00am.
  - If you have a problem with Angel
    - Call the Angel helpdesk 355-2345 (open 24/7)
- Slides on Angel
  - Click on the date on the syllabus
- Public lectures tonight
  - Mark Voit (author of our textbook)
    - Milky Way's biggest black hole
    - Planetarium, 7:30
  - Neil deGrass-Tyson (TV personality)
    - Footprints in the Sands of Science
    - Wharton Pasant Theatre, 7:30 (Need ticket)

## “Natural” motion for Newton & Aristotle

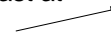
- Natural motion is motion that needs no explanation: the object naturally moves that way.
- Aristotle: For heavenly objects, natural motion is motion in a circle with the same speed. For base objects, natural motion is rest.
  - A book falls off the table and comes to rest on the floor. This needs no explanation because rest is the natural state.
- Newton: Natural motion is moving at the same speed in the same direction.
  - Newton's First Law: In the absence of a force, an object moves at the same speed in the same direction.
- Q: A book falls off the table and lands on the floor. For Newton, what is natural?
  - a. The book is on the floor.
  - b. The book is halfway to the floor.
  - c. The book is just starting to fall.
  - d. I shove the book off the table.
- What do I need to find out before answering the question?

- Q: Venus moves around the sun in a circle at the same speed. Does Newton consider this motion natural?
  - a. Yes, Venus is a heavenly object.
  - b. Yes, the speed is the same.
  - c. No, the direction is not always the same.
  - d. No, Venus is not at rest.
- What do I need to find out? Definitions?









- Q: Venus moves around the sun in a circle at the same speed. Does Newton consider this motion natural?
  - a. Yes, Venus is a heavenly object.
  - b. Yes, the speed is the same.
  - c. No, the direction is not always the same.
  - d. No, Venus is not at rest.
- Newton: The direction of Venus' motion changes. Something is causing the direction to change.

## Newton's Second Law









- Newton's First Law: In the absence of a force, an object moves at the same speed in the same direction.
- Velocity is the combination of speed and direction of motion
  - Specify speed and direction: I drive 10° north of east at 50mph.
  - Draw an arrow. Length specifies speed











## Change in velocity


- Q The velocity changed in
  - a. Case A only
  - b. Case B only
  - c. Neither cases A nor B
  - d. Both cases A and B
- Case A
  - Velocity at start 
  - Velocity after 1 s 
- Case B
  - Velocity at start 
  - Velocity after 1 s 
- Case C
  - Velocity at start 
  - Velocity after 1 s 
- Case D
  - Velocity at start 
  - Velocity after 2 s 

## Acceleration

- Q The velocity changed in
  - a. Case A only
  - b. Case B only
  - c. Neither cases A nor B
  - d. Both cases A and B
- **Acceleration** is change in velocity divided by amount of time
  - Acceleration is arrow from the tip of the beginning velocity to the tip of the ending velocity divided by time
- Draw the acceleration for cases C & D. The length of the acceleration is greatest for which case? A, B, C, or D
- Case A
  - Velocity at start 
  - Velocity after 1 s 
- Case B
  - Velocity at start 
  - Velocity after 1 s 
- Case C
  - Velocity at start 
  - Velocity after 1 s 
- Case D
  - Velocity at start 
  - Velocity after 2 s 

## Newton's Second Law

- Newton's First Law: In the absence of a force, an object moves at the same speed in the same direction.
  - Newton's Second Law tells how to find the motion if there is a force.
    - $Force = mass \times acceleration$   
 $F = m \times a$
    - Acceleration is change in velocity divided by amount of time
  - Q5 The velocity changed in
    - a. Case A only
    - b. Case B only
    - c. Neither cases A nor B
    - d. Both cases A and B
  - Q6 The acceleration is greatest for which case? A, B, C, or D
- Case A
    - Velocity at start 
    - Velocity after 1 s 
  - Case B
    - Velocity at start 
    - Velocity after 1 s 
  - Case C
    - Velocity at start 
    - Velocity after 1 s 
  - Case D
    - Velocity at start 
    - Velocity after 2 s 

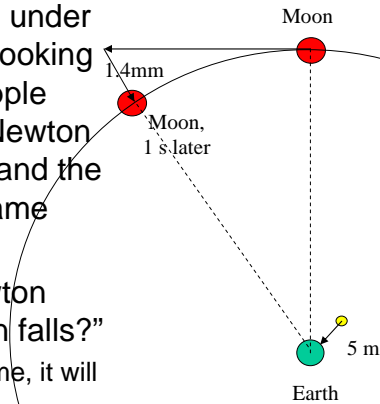


## Newton's Second Law

- Newton's First Law: In the absence of a force, an object moves at the same speed in the same direction.
- Newton's Second Law tells how to find the motion if there is a force.
  - $Force = mass \times acceleration$   
 $F = m \times a$
- Q5 Me & my cat are in the car. My mass is 100kg, and the mass of my cat is 4kg. The car goes from 0 to 50mph in 5s.
- Q The acceleration of me and my cat are
  - a. Same
  - b. Different
- Q The car exerts a force on me & my cat. The forces are
  - a. Same
  - b. Different

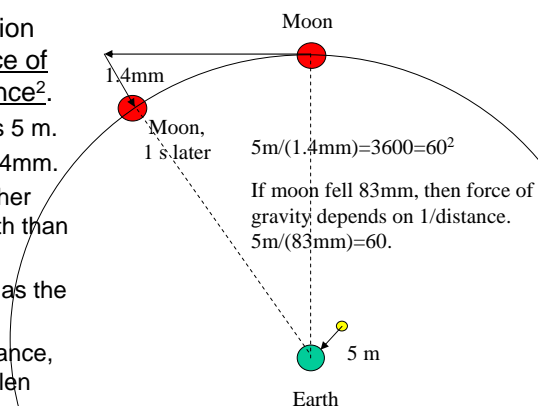
## Newton discovers the law of gravity

- Newton was sitting under an apple tree and looking at the moon. An apple falls on his head. Newton realizes the moon and the apple fall for the same reason.
- Q: What does Newton mean by “the moon falls?”
  - a. After a very long time, it will hit the earth.
  - b. It is falling from its natural path.



## Newton discovers the law of gravity

- Newton realizes the moon and the apple fall for the same reason. He does a calculation and concludes that the force of gravity depends as  $1/\text{distance}^2$ .
  - In 1 second, an apple falls 5 m.
  - In 1 second, moon falls 1.4mm.
  - The moon is 60 times farther from the center of the earth than the apple.
  - Moon falls  $1/60^2$  as much as the apple.
  - If force depends on  $1/\text{distance}$ , then moon would have fallen 83mm.



## Newton's Law of Gravity

- Force between sun and earth  
 $\text{Force} = G \text{mass}_{\text{Sun}} \text{mass}_{\text{Earth}} / \text{Distance}^2$ 
  - Force decreases with square of distance.
  - This is a universal law. Law applies to all. Two planets pull on each other.
  - This law is reciprocal: Sun pulls on the Earth; Earth pulls on the sun.
- Earth's natural motion is motion at constant speed in a straight line. How does sun make Earth deviate from its natural motion?
  - Force on earth =  $\text{mass}_{\text{Earth}} \times \text{acceleration}$  (Newton 2<sup>nd</sup>)
  - $G \text{mass}_{\text{Sun}} \text{mass}_{\text{Earth}} / \text{Distance}^2 = \text{mass}_{\text{Earth}} \text{acceleration}$
  - $\text{acceleration} = G \text{mass}_{\text{Sun}} / \text{Distance}^2$
  - Acceleration (how much the velocity changes in 1 s) is proportional to the mass of the sun and inversely to the square of the distance.