

LECTURE # 32

Note Title

4/8/2009

CALENDAR PRESENTATIONS

- (1) ~~Quantum Hall effect~~
Graphene
- (2) ~~Carbon Nanotubes~~
Excitons and exciton-polaritons
Mesoscopic physics and single electronics
Spectroscopy of quantum dots and quantum wires
- (3) ~~Spintronics in metals/semiconductors~~
Neutron and electron scattering in solids
Solid state devices for quantum information processing
- (5) ~~Magnetic properties of solids~~
- (4) ~~Superconductivity~~
~~FULLERENES~~

(3)	Acharyya, Rakhi Bremer, Marshall T] APR	27
(5)	Deninno, Matthew Luke Devi, Pampa] APR	29
(1)	Do, Dat Thanh] MAY	1
(4)	Doan, Tri Cao Kittimanapun, Kritsada] MAY	8
(2)	Latt, Kyaw Zin Miller, Nicholas Joel Xu, Kaijie] MAY	8

PAPER FORMAT: DOUBLE SPACE 12 pt

LIMIT 5 PAGES INCLUDING FIGS & REFS



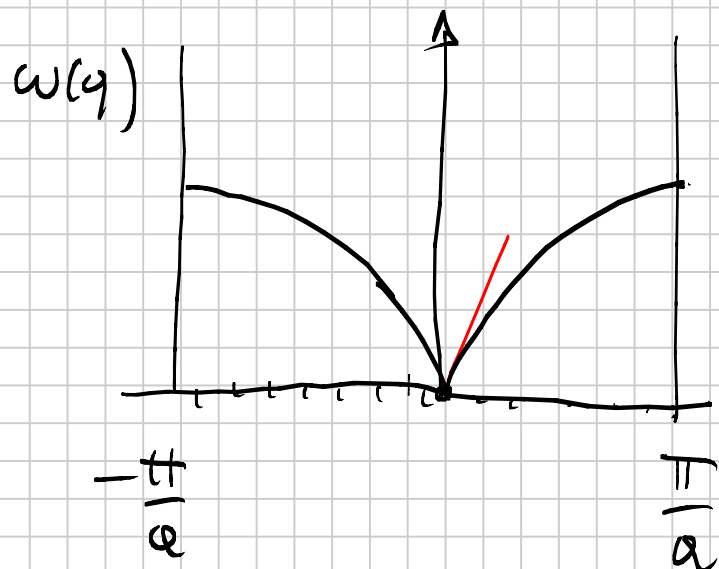
FIND THE NORMAL
MODES OF OSCILLATIONS
LABELED BY q IN

THE FIRST BRILLOUIN ZONE

$$u_m(q) = e^{i(qma - \omega(q)t)}$$

$$\lambda = \frac{2\pi}{q}$$

WE FOUND $\omega(q) = \sqrt{\frac{4K}{M}} \left| \sin \frac{qa}{2} \right|$



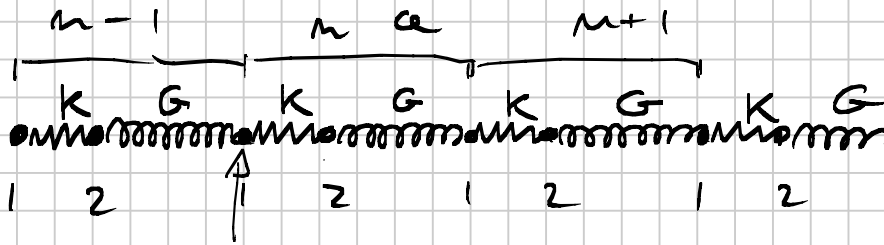
$$\sqrt{\frac{4K}{M}}$$

SMALL q $\lambda \gg a$

$$\omega(q) \sim v_s q$$

$$\left(\frac{1}{\hbar} \omega(q) = \frac{1}{\hbar} v_s q \right)$$

ACOUSTIC MODES



ASSUME SAME MASS M

m_{1m} m_{2m}

UNIT CELLS
 N

$q = N$

$2N$ ATOMS

$\Rightarrow 2N$ NORMAL MODES

$\Rightarrow 2$ DIFFERENT MODES FOR EACH q

$$\begin{cases} M \ddot{u}_{1m} = -K(u_{1m} - u_{2m}) - G(u_{1m} - u_{2m-1}) \\ M \ddot{u}_{2m} = -G(u_{2m} - u_{1m+1}) - K(u_{2m} - u_{1m}) \end{cases}$$

$$\begin{cases} u_{1m}(q) = \epsilon_1 e^{i(qma - \omega t)} \\ u_{2m}(q) = \epsilon_2 e^{i(qa - \omega t)} \end{cases}$$

$$u_{2m-1} = e^{-iqa} u_{2m}$$

$$\begin{cases} [M\omega^2 - (K+G)]\varepsilon_1 + (K+G e^{-iqa})\varepsilon_2 = 0 \\ (K+G e^{+iqa})\varepsilon_1 + [M\omega^2 - (K+G)]\varepsilon_2 = 0 \end{cases}$$

$$M \begin{pmatrix} \varepsilon_1 \\ \varepsilon_2 \end{pmatrix} = 0$$

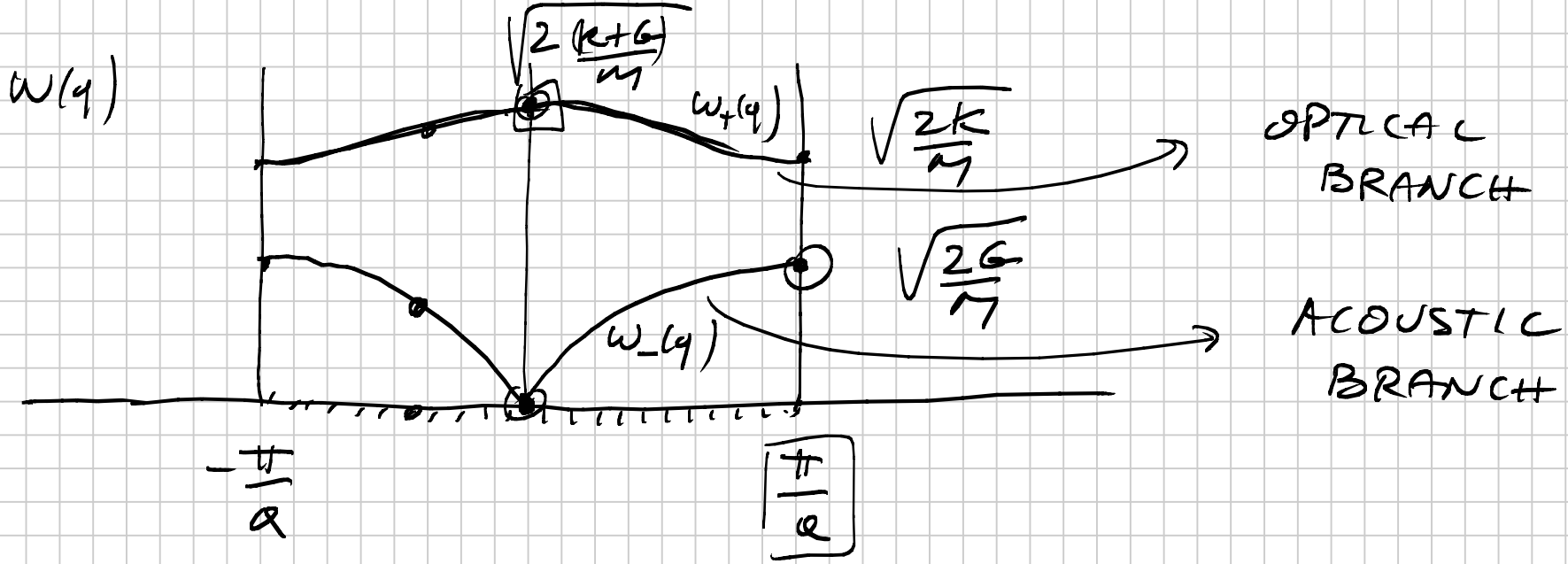
DET $M = 0 \Rightarrow$ GIVES NON TRIVIAL SOLUTIONS



$$\omega_{\pm}^2(q) = \left(\frac{K+G}{M} \right) \pm \frac{1}{M} \sqrt{K^2 + G^2 + 2KG \cos qa}$$

$$\frac{\varepsilon_2}{\varepsilon_1} = \begin{pmatrix} - \\ + \end{pmatrix} \frac{K + G e^{iqa}}{|K + G e^{iqa}|}$$

NORMAL
MODES



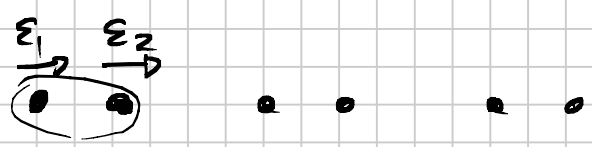
NORMAL MODES AT $q = 0$

ACOUSTIC MODE

$\omega_-(q) \quad q \rightarrow 0$

$$\frac{\epsilon_2}{\epsilon_1} = \frac{k + G e^{iqa}}{(k + G e^{iqa})} \rightarrow 1$$

$\Rightarrow \epsilon_1$ PARALLEL TO ϵ_2



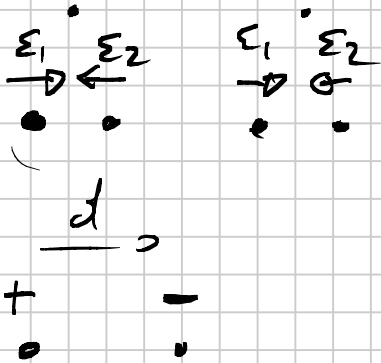
FOR ACOUSTIC MODE

1 & 2 ARE "IN PHASE"

OPTICAL MODE AT $q = 0$

$$\omega_+(q) \rightarrow \sqrt{2 \frac{\epsilon_1 + \epsilon_2}{\mu}}$$

$$\frac{\epsilon_2}{\epsilon_1} \rightarrow 0 \quad -1$$



OPTICAL MODE OF OSCILLATION

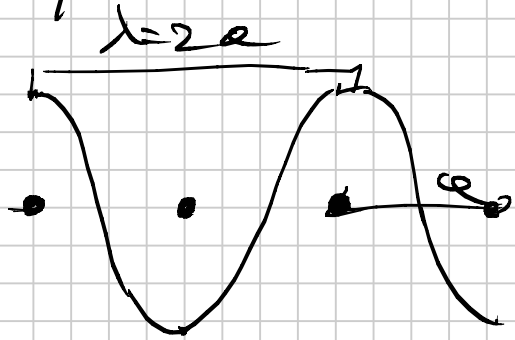


THE OSCILLATING EM FIELD CAN EXCITE THE DIPOLE OSCILLATION

NORMAL MODES AT THE ZONE

BOUNDARY $q = \frac{\pi}{a}$

$$\lambda = \frac{2\pi}{q} \Rightarrow \lambda = 2a$$



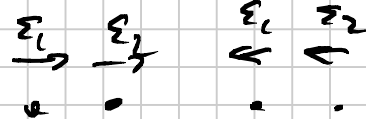
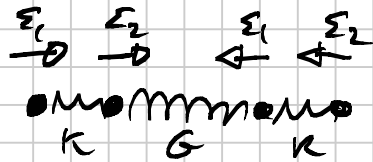
ACOUSTIC

MODE

AT

$$q = \frac{\pi}{a}$$

$$\omega_-(\frac{\pi}{a})$$



$$\omega_- \propto \sqrt{\frac{b}{\mu}}$$

OPTICAL

MODE

AT

$$q = \frac{\pi}{a}$$

$$\omega_+(\frac{\pi}{a})$$

$$\frac{\omega_+}{\omega_-} \rightarrow 1$$



$$\omega_+(\frac{\pi}{a}) \sim \sqrt{\frac{K}{\mu}}$$

3D $\vec{u} \parallel \vec{q}$ LONGITUDINAL
 $\vec{u} \perp \vec{q}$ 2 TRANSVERSAL MODES

••••• $\langle E \rangle$? ENERGY

$$\langle E \rangle = \langle T \rangle + \langle V \rangle$$

$$\langle T \rangle = \frac{K_B T}{2} \cdot 3 \quad (3D)$$

$$\langle V \rangle = ?$$

VIRIAL THEOREM CLASSICAL MECHANICS

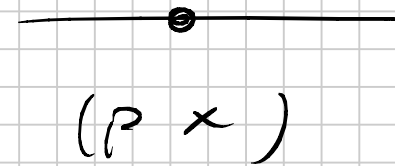
$$V \sim (r_i - r_j)^\lambda$$

$\langle V \rangle$ IS PROP TO $\langle T \rangle$ ACCORDING TO

$$2 \langle T \rangle = \lambda \langle V \rangle$$

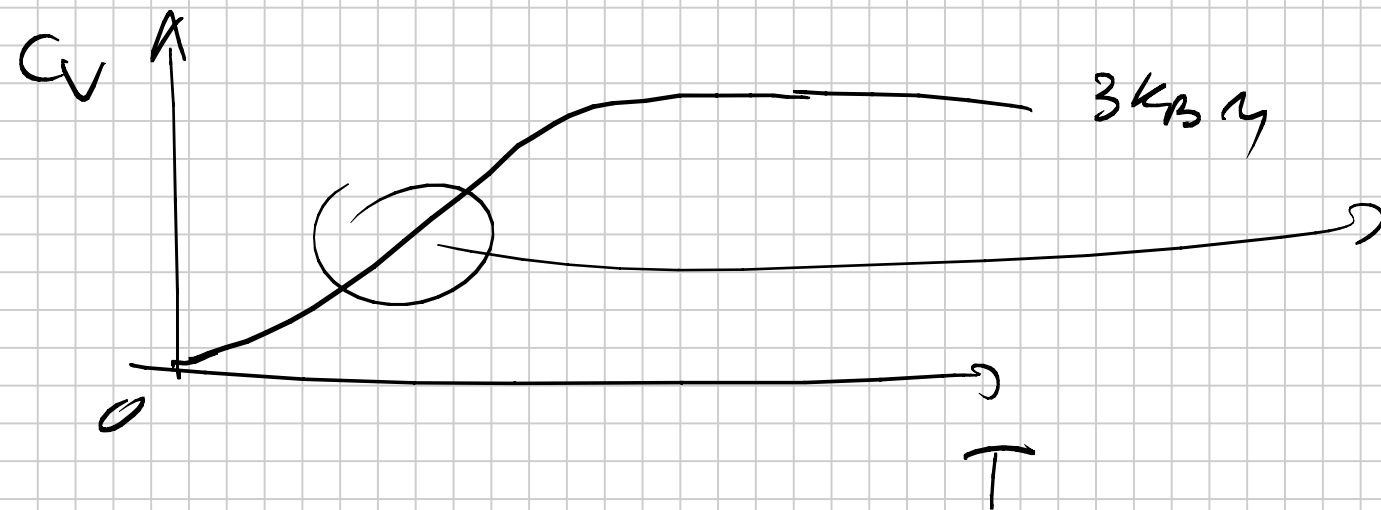
$\lambda = 2$ FOR SPRINGS

$$\Rightarrow \langle V \rangle = \langle T \rangle$$



$$\langle E \rangle = \frac{3}{2} k_B T + \frac{3}{2} k_B T \rightarrow 3 k_B T$$

$$C_V = \frac{1}{T} \frac{\partial \langle E \rangle}{\partial T} = 3 k_B \frac{N}{V} = 3 k_B n$$



NEEDS
QUANTUM
MECHANICS
