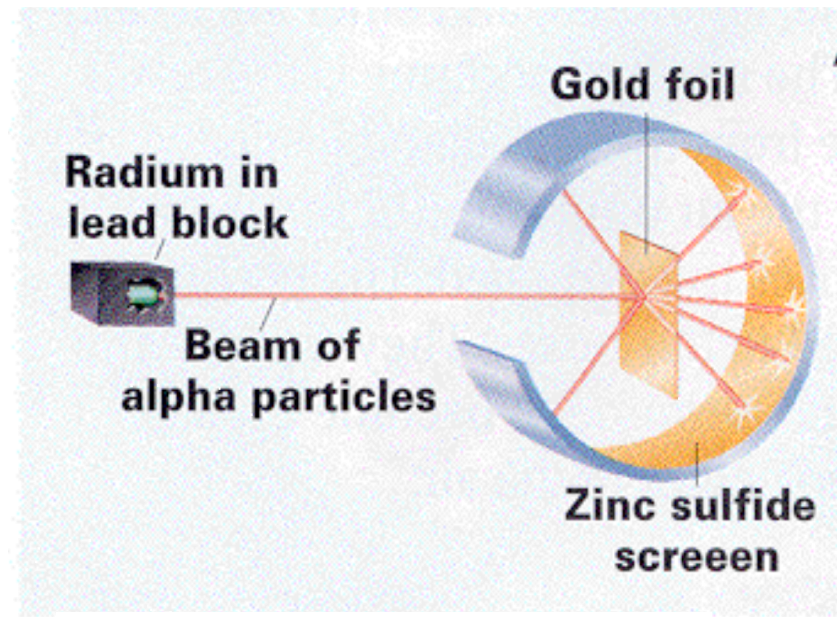
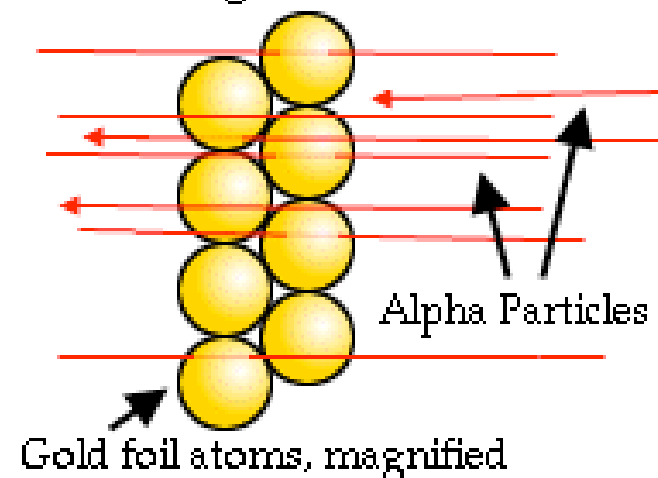


Experiment

- Rutherford had two grad students, Marsden and Geiger.
- It was decided that Geiger would gain some practice by conducting a series of experiments with gold and alpha particles.
- The positively charged Alpha Particles were expected to go through the gold atoms and be slightly deflected.



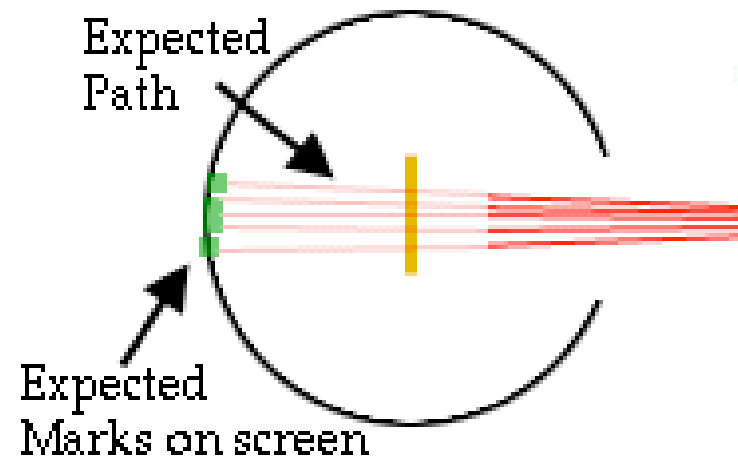
Detail of Gold Foil
According to old Atom Model



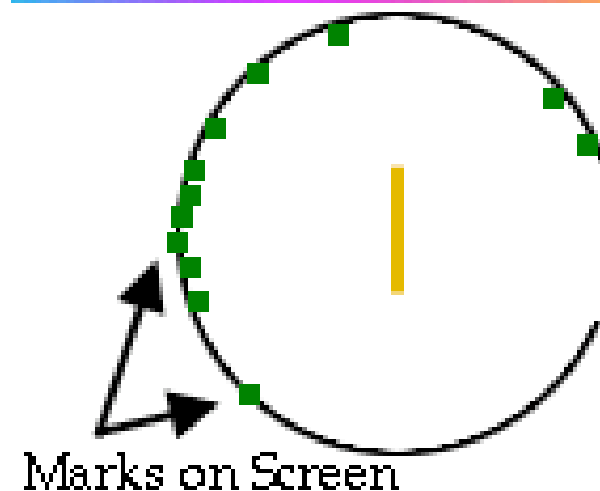
Surprise, surprise, surprise

- On the screen, marks were only expected to appear in a limited region.
- Geiger was to explore the places where no results were anticipated.
- Marsden had to excitedly tell Rutherford that the new student had actually gotten results!
- Some were almost straight back!

The Predicted Result:

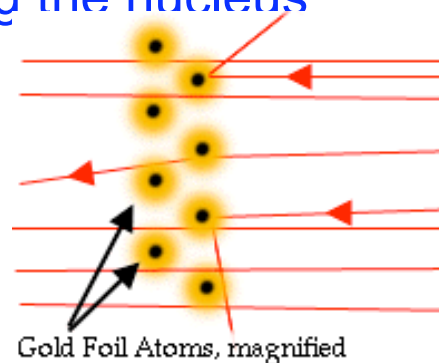


The Result

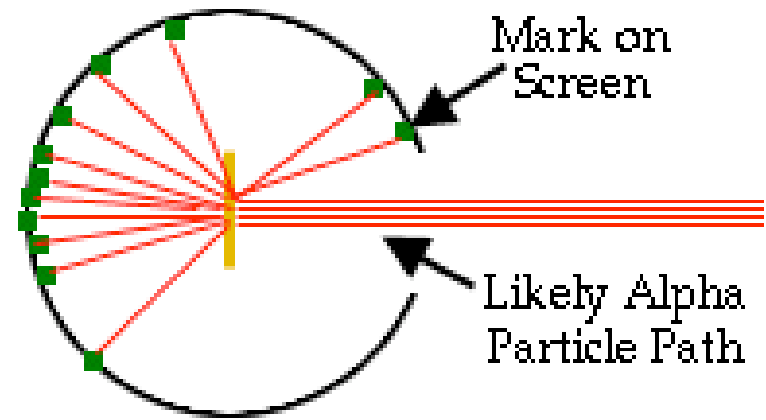


Cannonballs and tissue paper

- Rutherford would later compare it to firing a cannonball at a piece of tissue paper and having the ball bounce back!
- Rutherford quickly realized that a small, very dense and positively charged nucleus would account for the paths of the alpha particles.
- It took a lot of geometry and statistics to eventually convince other physicists and to show how big the nucleus was.

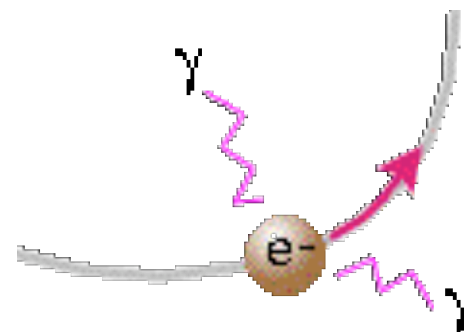
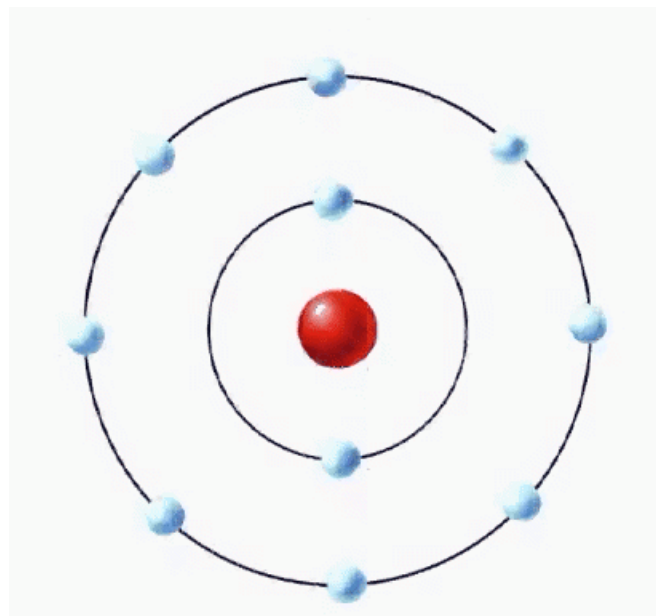


Extrapolation of Result:



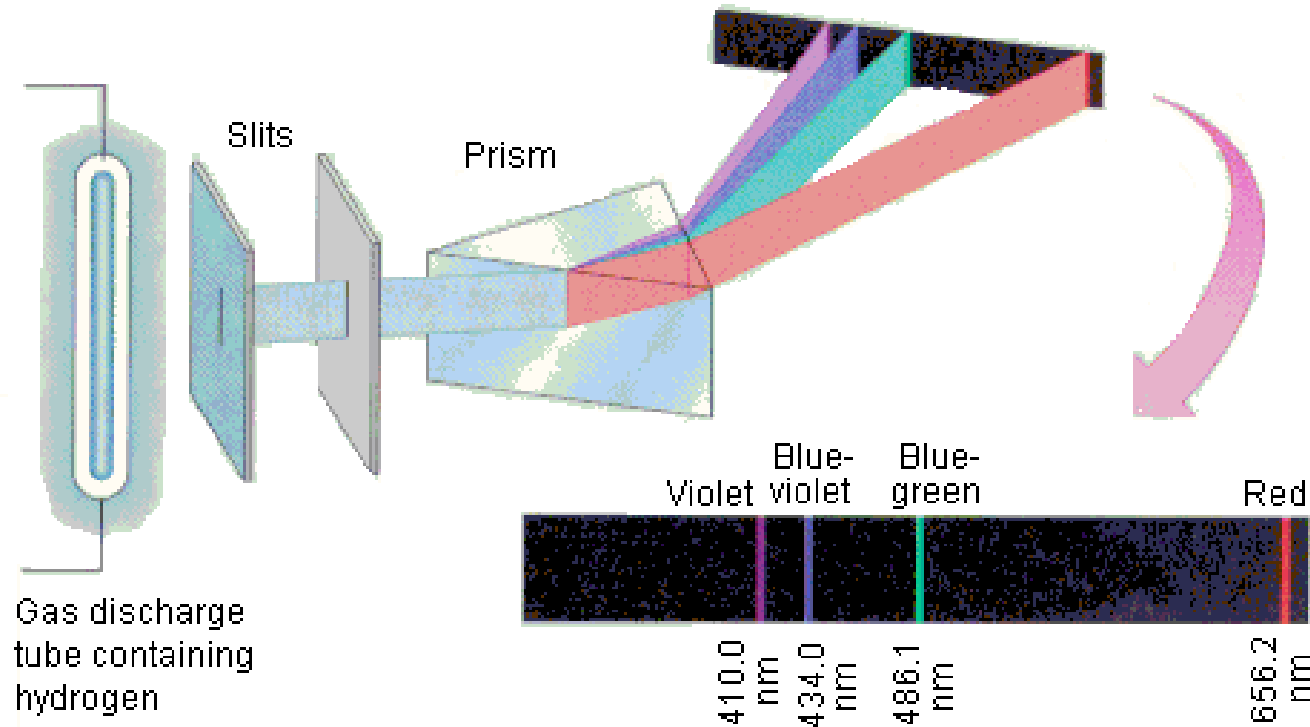
Solar system model

- This led to the classic model of the atom- similar to the solar system
- Distant electrons orbit a massive nucleus due to electrical forces of attraction.
- Rutherford's model was very appealing but there were some "minor" problems that had to be solved.
- What held the nucleus together to be so small? AND...
- The orbiting electrons were giving off light, due to Conservation of Energy, they should eventually spiral into nucleus!
 - ◆ remember that accelerating charges radiate energy

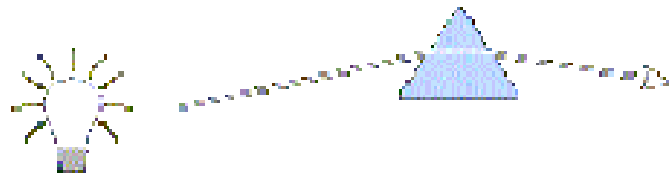


Another problem with Solar System Model

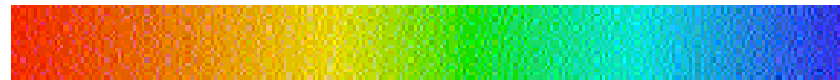
Emission and absorption spectra of gases like hydrogen indicate only certain wavelengths of light are emitted or absorbed by the atoms.



Spectra



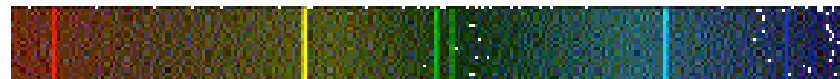
Continuous Spectrum



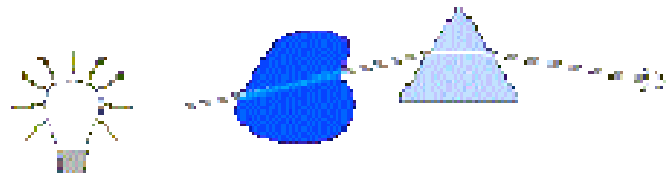
Hot Gas



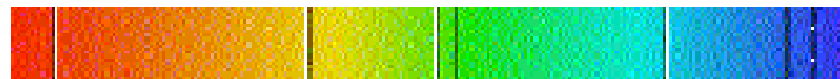
Emission Spectrum



Cold Gas

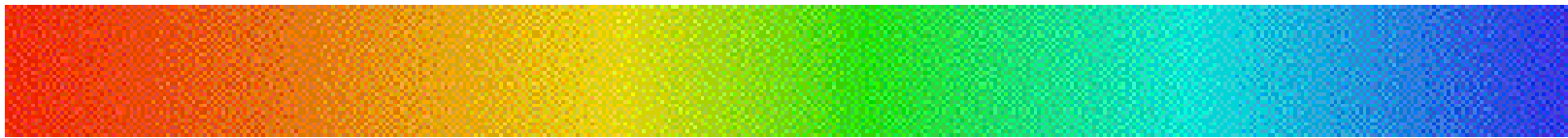


Absorption Spectrum

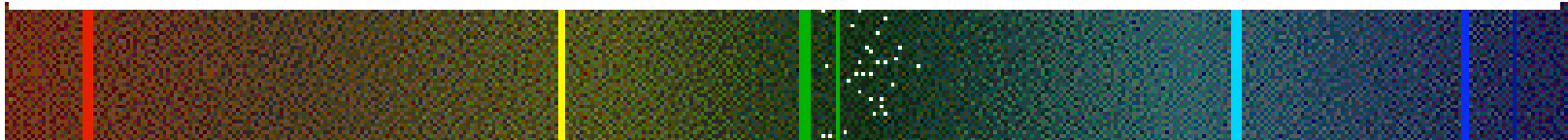


Spectra

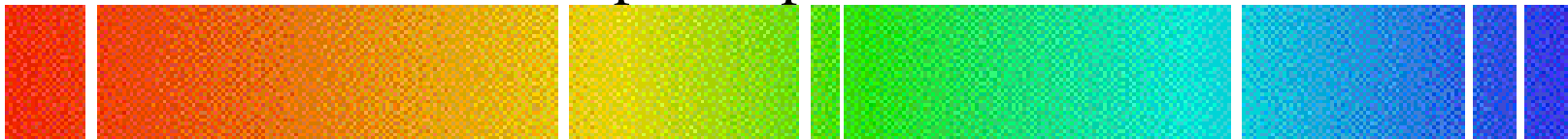
Continuous spectrum



Emission spectrum

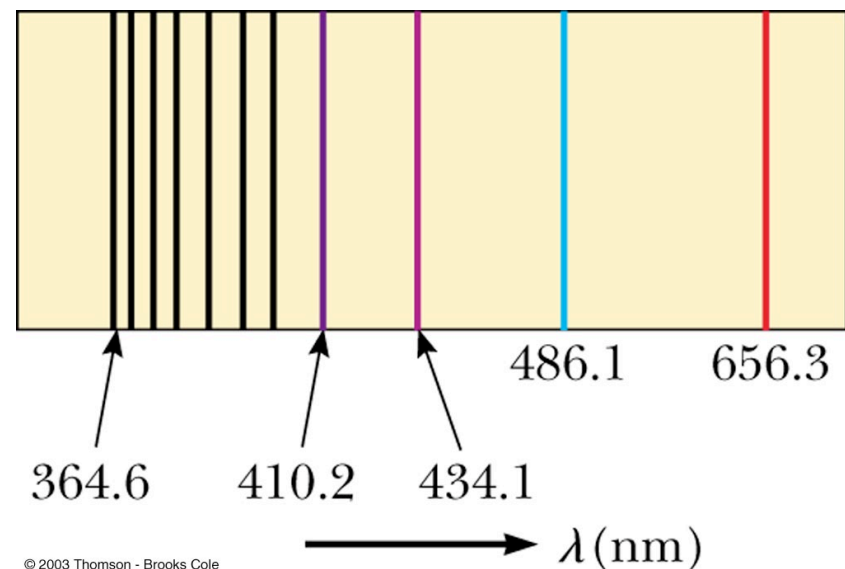


Absorption spectrum



Look at wavelengths of emission spectrum of H₂

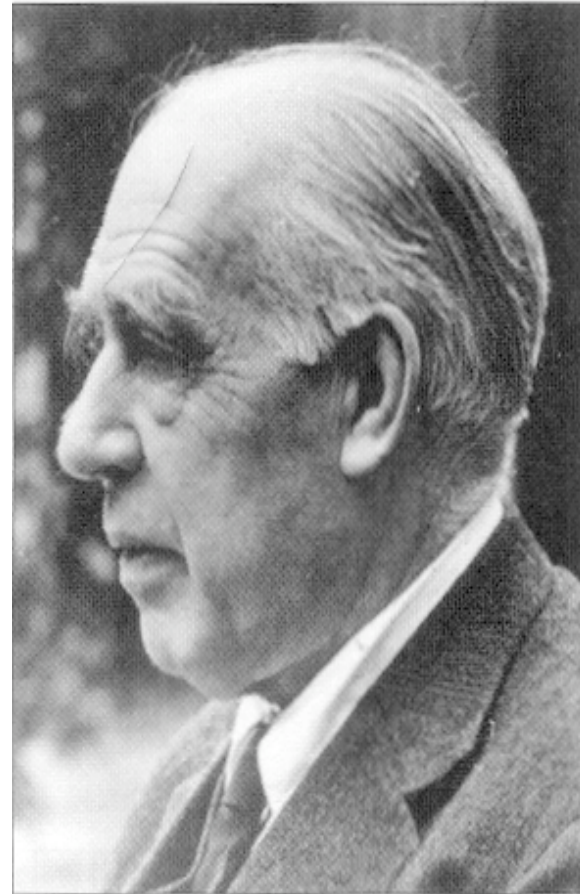
- Consider the 4 wavelengths marked to the right
 - ◆ all in visible region of EM spectrum
 - ◆ Named the Balmer series after Johann Balmer who found that the wavelengths could be described by a simple empirical equation
$$\frac{1}{\lambda} = R_H \left(\frac{1}{2^2} - \frac{1}{n^2} \right)$$
 - ◆ n has integral values of 3,4,5,... and R_H is the Rydberg constant
 - ▲ R_H=1.0973732X10⁷m⁻¹



Why this pattern?

Bohr to the rescue

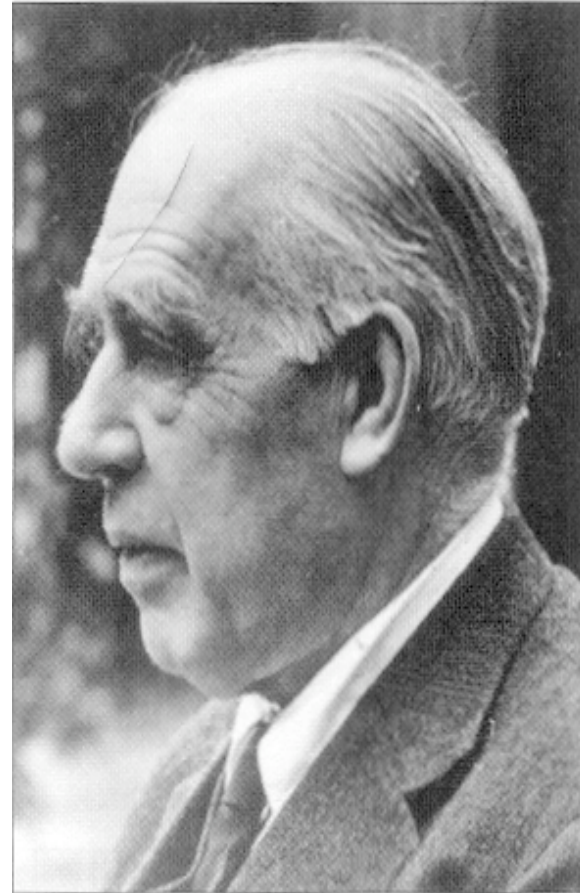
- In 1905, Einstein had proposed the wave/particle duality of light with the photon.
- In 1913, Bohr used the concept in creating a quantum model of the atom.



Niels Bohr, Danish physicist
(1885–1962)

A Niels Bohr interlude

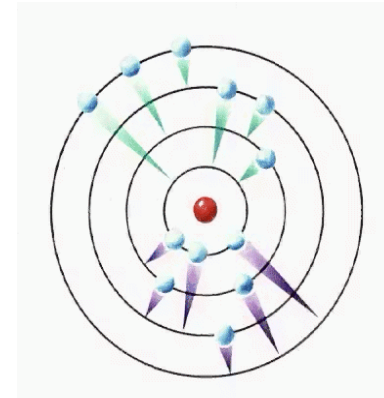
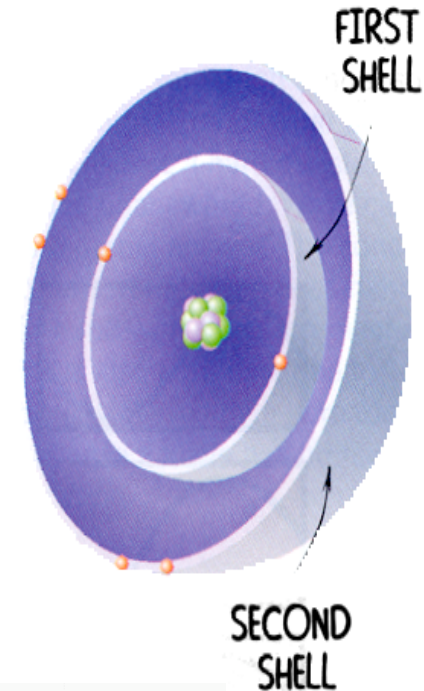
- Active participant in early development of quantum mechanics and provided much of its philosophical underpinnings
 - ◆ *Copenhagen interpretation*
- Bohr headed the Institute for Advanced Studies in Copenhagen, under the support of the Carlsberg brewery
- Participated in Manhattan project during WWII
 - ◆ play currently on Broadway called *Copenhagen* deals with Bohr and Heisenberg



Niels Bohr, Danish physicist
(1885–1962)

Bohr's model of the atom

- Only certain stable orbits exist for the electrons.
- While at these orbitals, they do not give off photons.
- Electrons can only move from orbital to another orbital by gaining or releasing photons (a quanta of energy).
 - ◆ $E_i - E_f = hf$
- Size of electron orbits is determined by constraints on electron's orbital angular momentum
 - ◆ $m_e v r = n \hbar \quad n=1,2,3,\dots$

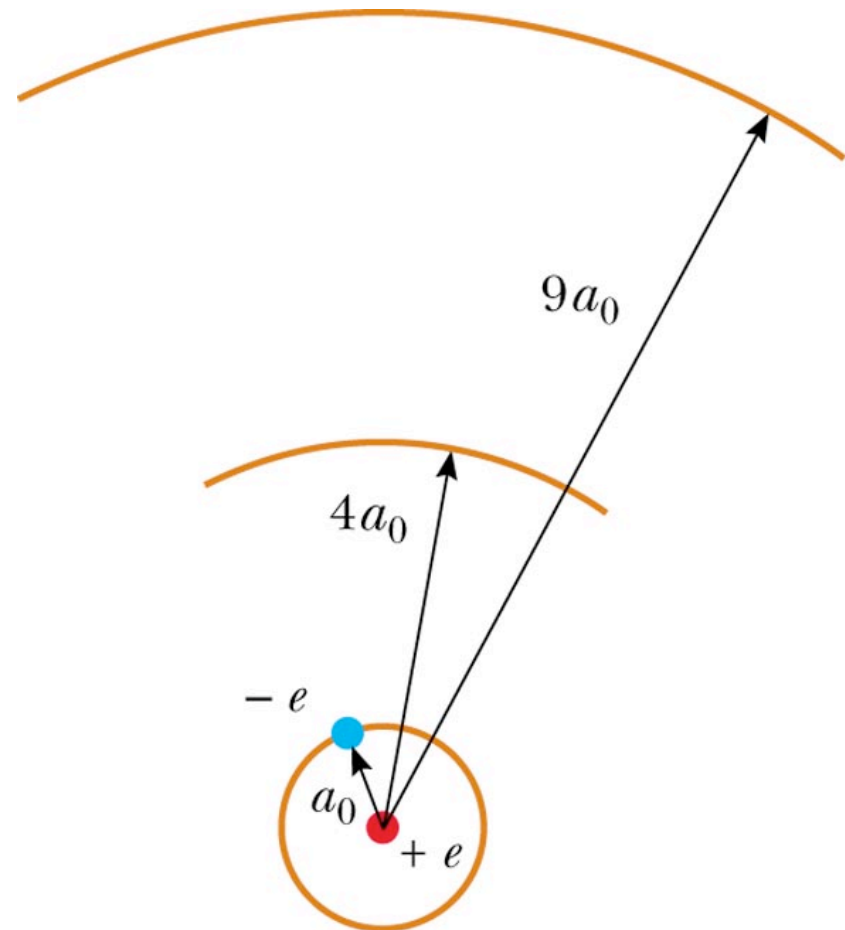


Electron orbits

- Electrons can only exist in certain allowed orbits

$$r_n = \frac{n^2 \hbar^2}{m_e k_e e^2}$$

- ◆ $a_0 = \hbar^2 / (m_e k_e e^2)$
= 0.0529 nm is called the Bohr radius and corresponds to $n=1$



$$r_n = n^2 a_0 \quad n = 1, 2, 3, \dots$$

Energies of orbitals

- Energies of quantum states given by

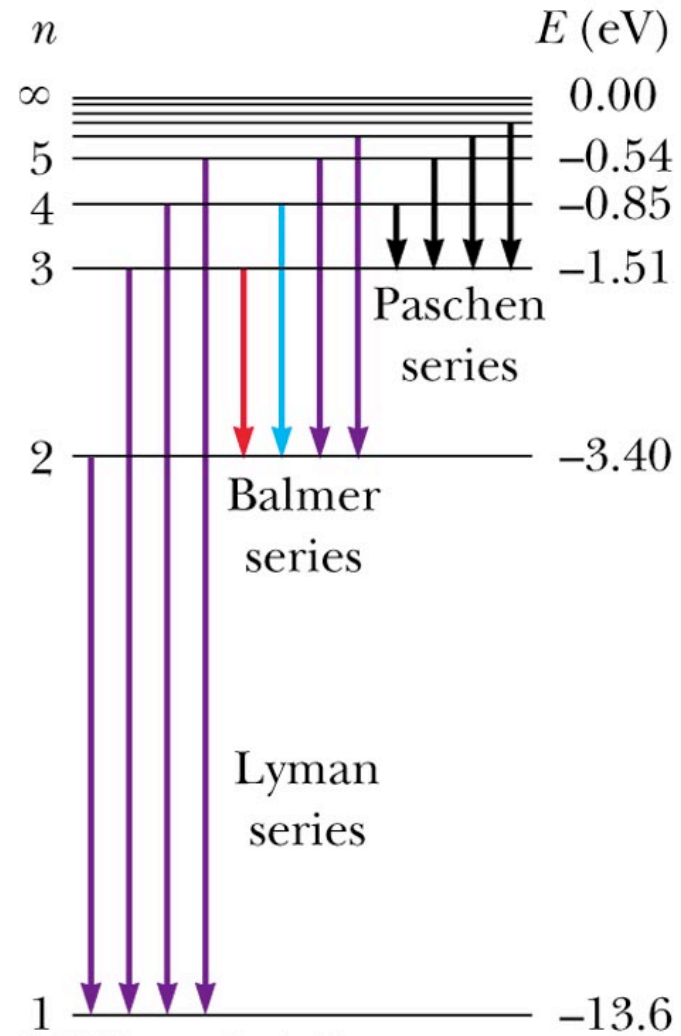
$$E_n = - \frac{m_e k_e^2 e^4}{2\hbar^2} \left(\frac{1}{n^2} \right)$$

$$E_n = - \frac{13.6}{n^2} \text{ eV}$$

$$n = 1, 2, 3, \dots$$

also write

$$\frac{1}{\lambda} = R_H \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$$



Extension of Bohr model to other atoms

- Energies of quantum states given by

$$E_n = - \frac{Z^2 m_e k_e^2 e^4}{2\hbar^2} \left(\frac{1}{n^2} \right)$$

$$E_n = - \frac{13.6 Z^2}{n^2} \text{ eV}$$

$$n = 1, 2, 3, \dots$$

- Bohr model of the atom was a great success in some areas
 - ◆ explains Balmer and other series
 - ◆ predicts a value for the Rydberg constant in agreement with data
 - ◆ predicts the energy levels of hydrogen
 - ◆ can also be applied to hydrogen-like atoms
 - ▲ ionized so contains only 1 electron
 - ▲ Z protons

Arnold Sommerfeld

- Extended Bohr's ideas to include possibility of elliptical orbits
- Thesis advisor to most Europe's theorists



Nomenclature

- Bohr's quantization of angular momentum led to *principal quantum number* n
- In Sommerfeld's model, also have *orbital quantum number* l
 - ◆ l goes from 0 to $n-1$
 - ▲ so $n=1$ only has $l=0$
 - ▲ $n=2$ has $l=0,1$
 - ◆ electron in n th orbital can move in any of the l suborbitals
- All states with same principal quantum number n are said to form a shell
 - ◆ states with given values of n and l are said to form a subshell

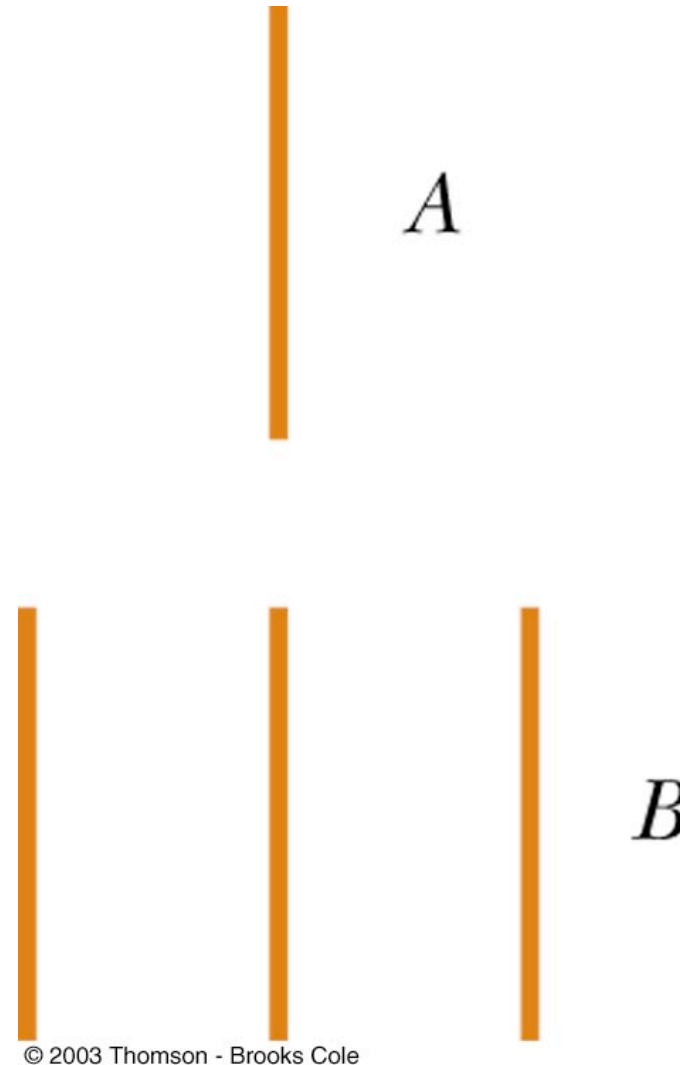
TABLE 28.1

Shell and Subshell Notations

n	Shell Symbol	ℓ	Subshell Symbol
1	K	0	<i>s</i>
2	L	1	<i>p</i>
3	M	2	<i>d</i>
4	N	3	<i>f</i>
5	O	4	<i>g</i>
6	P	5	<i>h</i>
⋮		⋮	

Not another quantum number

- Yes, another quantum number
- It was discovered that the spectral lines of a gas are split into several closely spaced lines when the gas is placed in a strong magnetic field
 - ◆ Zeeman effect
- Energy of an electron is slightly modified when it's in a magnetic field
 - ◆ Introduce new quantum number m_l , the *orbital magnetic quantum number*
 - ◆ m_l is restricted to integer values from $-l$ to $+l$



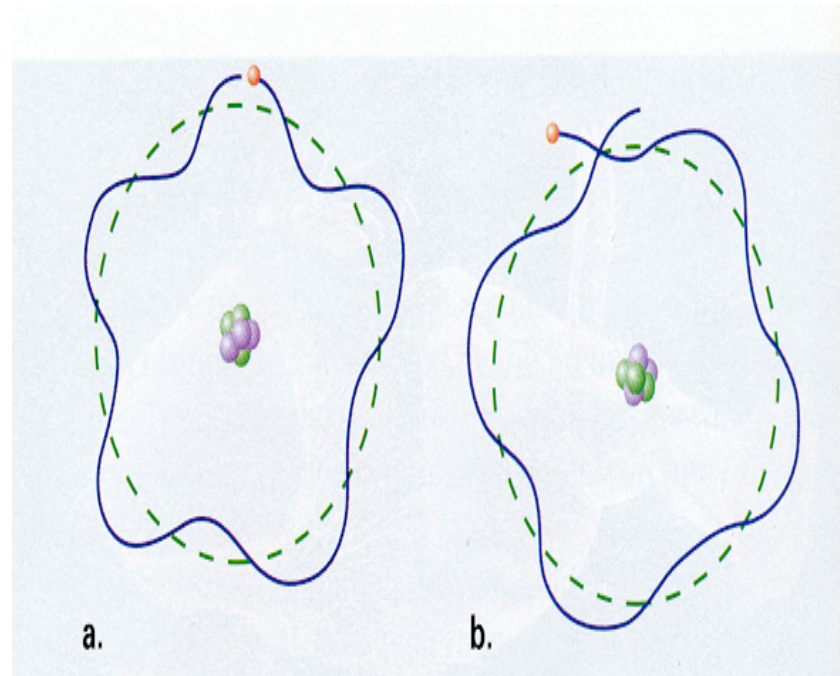
Complete nomenclature

TABLE 28.2 Three Quantum Numbers for the Hydrogen Atom

Quantum Number	Name	Allowed Values	Number of Allowed States
n	Principal quantum number	1, 2, 3, . . .	Any number
ℓ	Orbital quantum number	0, 1, 2, . . . , $n - 1$	n
m_ℓ	Orbital magnetic quantum number	$-\ell, -\ell + 1, . . . , 0, . . . , \ell - 1, \ell$	$2\ell + 1$

Enter de Broglie again

- Bohr's model worked but it lacked a satisfactory reason why.
- De Broglie suggested that all particles have a wave nature.
 - ◆ $\lambda = h/p$



It was the Wave Nature of the electron that determined the nature of the orbits.