PHY251 Summer 2009: Practical #2

THE SPRING: Hooke's Law

OBJECTIVES:

- To investigate how a spring behaves when it is stretched under the influence of an external force. To verify that this behavior is accurately described by Hooke's Law.
- To measure the spring constant k.

THEORY

An ideal spring is remarkable in the sense that it is a system where the generated force is **linearly dependent** on how far it is stretched. Hooke's law describes this behavior, and you would like to verify this in lab today. Hooke's Law states that to extend a string by an amount Δx from its previous position, one needs a **force** F which is determined by $F = k\Delta x$. Here k is the **spring constant** which is a quality particular to each spring. Therefore in order to verify Hooke's Law, you must verify that the force F and the distance the spring is stretched are proportional to each other (that just means linearly dependent on each other). The constant of proportionality is k.

In our case the external force is determined by attaching a mass m to the end of the spring. The mass will of course be acted upon by gravity, so the force exerted downward on the spring will be $F_g = mg$. See Figure 1. Consider the forces exerted on the attached mass. The force of gravity (mg) is pointing downward. The force exerted by the spring ($k\Delta x$) is pulling upwards. When the mass is attached to the spring, the spring will stretch until it reaches the point where the two forces are equal but pointing in opposite directions:

$$F_{s} - F_{g} = 0$$
 or
$$k\Delta x = F_{g} = mg \tag{1}$$

This point where the forces balance each other is known as the **equilibrium point**. The spring + mass system can stay at the equilibrium point indefinitely as long as no additional external forces act on it. The relationship (1) allows us to determine the spring constant k when m, g, and Δx are known or can be measured. This is how you will be determining k today.

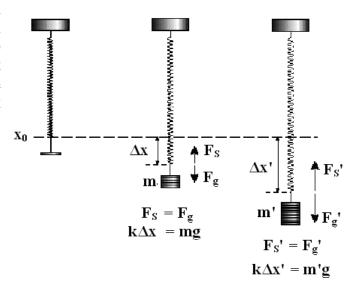


Figure 1: The spring in equilibrium.

PROCEDURE

The mass of the support table, m_0 is 50.0 g. Attach the support table for the masses to the spring. With the zero end of a meter stick on the lab table, measure the position of the end of the spring after the support table has been attached. This position is the initial position x_0 .

Start the measurement with an attached mass of 120 grams. Then increase the mass in steps of 20 grams, making a total of 5 measurements. Measure the corresponding position of the spring for each mass. This results in a series of measurements m_i and x_i . To calculate the forces due to gravity and the spring calculate $\Delta x_i = x_i - x_0$ and $\Delta m_i = m_i - m_0$. Also calculate the error on the distance the spring extends, $\delta(\Delta x_i)$. The corresponding forces for gravity and the spring are $F_o = \Delta mg$ and $F_s = k\Delta x$.

Right now you do not know k, so you will only have your spreadsheet calculate F_g for you. But remember, at equilibrium positions such as we are measuring, F_g equals F_s !

Graph F_g vs. Δx . Add error bars for Δx to your graph. Note that these error bars are horizontal. Now have the computer fit your plot with a best fit line. The slope and its uncertainty determine the spring constant k in Hooke's Law.

Hand in:

- Your spreadsheet.
- The formula view of the spreadsheet.
- The graph with linear fit and error bars for Δx .
- Answers to the questions.

Questions:

- 1. Is your data consistent with Hooke's Law? Explain.
- 2. What value did you find for the spring constant k from your graph?
- 3. Is the spring constant you measured consistent with the value given to you by the lab instructor? Justify your answer by showing your work.
- 4. How would F_g and Δx change if this experiment was done on the moon where the gravitational acceleration is six times smaller than on earth?

Comparing Data

It is often necessary to compare two different pieces of data or results of two different calculations and determine if they are compatible (or consistent). In just about every experiment in this course you will be asked if two quantities are compatible or consistent. The following describes how to determine if two pieces of data are consistent (or compatible). Use this procedure to answer the question at the end and use it as a reference whenever you are asked if two pieces of data are compatible or consistent. Let's denote the pieces of data by d_1 and d_2 . If $d_1 = d_2$ or $d_1 - d_2 = 0$, clearly they are compatible. We often use Δ (pronounced "Delta") to denote the difference between two quantities:

$$\Delta = d_1 - d_2 \tag{8}$$

This comparison must take into account the uncertainties in the observation of both measurements. The data values are $d_1 \pm \delta d_1$ and $d_2 \pm \delta d_2$. To perform the comparison, we need to find $\delta \Delta$. The addition/subtraction rule for uncertainties is:

$$\delta \Delta = \delta \mathbf{d}_1 + \delta \mathbf{d}_2 \tag{9}$$

Our comparison becomes, "is zero within the uncertainty of the difference Δ ?" This is the same thing as asking if:

$$|\Delta| \le \delta \Delta \tag{10}$$

Equation (9) and (10) express in algebra the statement " d_1 and d_2 are compatible if their error bars touch or overlap." The combined length of the error bars is given by (9). $|\Delta|$ is the separation of d_1 and d_2 . The error bars will overlap if d_1 and d_2 are separated by less than the combined length of their error bars, which is what (10) says. Sometimes rather than a second measured value you are comparing your data to an expected value. If this is the case, replace $d_2 \pm \delta d_2$ with $e \pm \delta e$, where $e \pm \delta e$ is the expected value including its uncertainty.

Excel Data Table for the Practical Lab:

PHY 251 Lab Practical Exam Summer 2009

	g =	980 cm /sec ²			$\delta(X-X_0) = 2\delta X$	
Zero position of spring: Measure the va						he values
mass (m ₀)	X ₀	δΧ]		in the gray fields	
g	cm	cm				
50			Insert units		Calculate values	
		in the blue fields		in the yellow fields		
Spring extension vs. mass						
Mass (m)	m-m ₀	Х	X-X ₀	δ(X-X ₀)	Force (F _g)	
					, and the second	
120						1
140						•
160						
180						
200						

 $1 \text{dyne} = 1 \text{g*cm/s}^2$