

---

## The cosmic microwave background radiation

—18 Feb 2010

- Midterm exam
  - Key ideas. How to do better
- Cosmic microwave background radiation
  - Why is the existence of the CBR important for the history of the universe?
  - Important events
- Angular scale of fluctuations in the CBR
  - What is the physical length of the fluctuations?  
What is the density parameter of universe seen in the CBR?  
What is the age of the universe?



## Midterm exam

- Statistics

Quartiles: 15.5, 18, 22.75

Top score: 33/35

- Key ideas, misconceptions
  - Q1, on finding  $g^{\theta\theta}$   
 $a^\mu$  is not the same as  $a_\mu$ .
  - Q2a, on finding  $p^\mu$  for a photon on a radial path
  - Q2b, on finding the energy measured by an observer.
  - Q3, on a clock on Earth
  - Q4,



---

## The cosmic microwave background radiation

—18 Feb 2010

Penzias & Wilson, 1965, “A measurement of the excess antenna temperature at 4080Mc/s,” ApJ 142, 419.  
 “The excess temperature is ... isotropic, unpolarized, and free from seasonal variation.”

Why is this radiation with a temperature of 3K important for the history of the universe? DPRW explained.

Dicke, Peebles, Roll, & Wilkinson, 1965, “Cosmic Black-body Radiation,” ApJ 142, 414.  
 “Could the universe have been filled with black-body radiation from this possible high-temperature state?”

### Black-body radiation

A wavelength characterizes black body radiation

$$\lambda = \frac{hc}{kT}.$$

Alternatively, Wien's Law. Peak of the spectrum in wavelength is

$$\lambda_{\text{peak}} = 2.9 \text{ mm} \frac{1\text{K}}{T}$$

Because wavelengths expand with the universe, the wavelength of the black-body radiation increases with time and the temperature decreases.

The temperature of the radiation changes as  $a^{-1}$ .

Q: Why is this significant for the history of the universe?

The mass-energy density changes

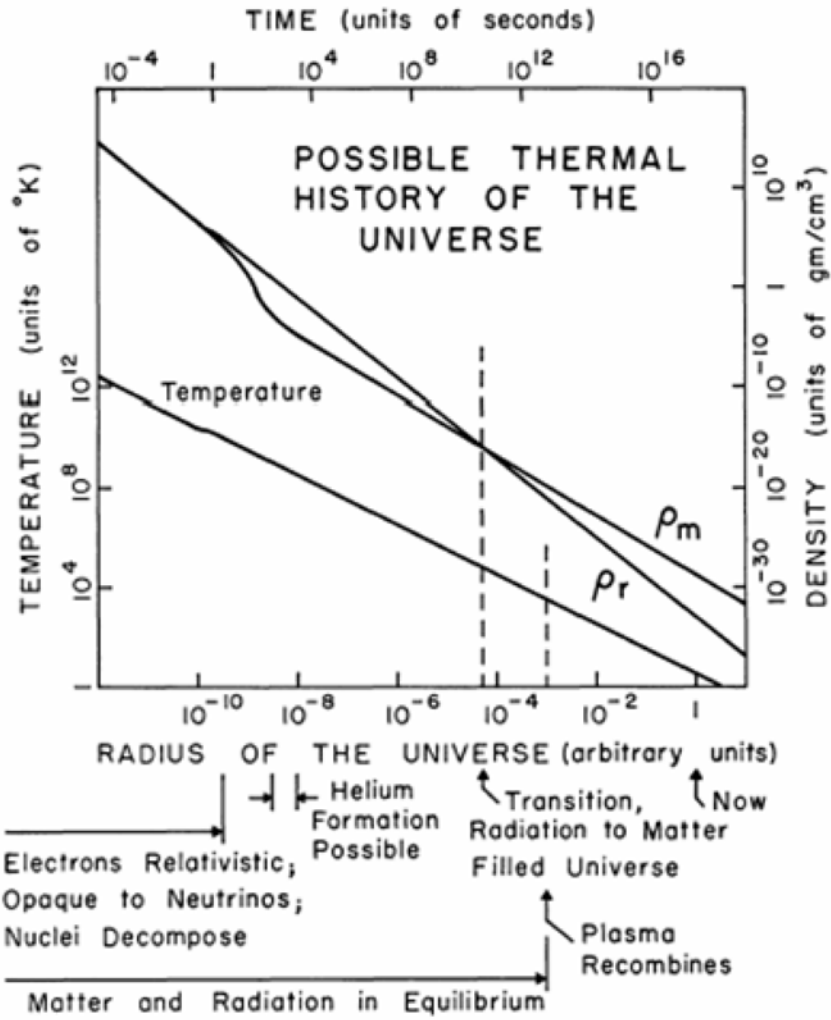
$$\rho_{\text{radiation}} \sim a^{-4}$$

whereas

$$\rho_{\text{pressureless matter}} \sim a^{-3}$$

$a^{-4}$  always beats  $a^{-3}$  for small enough  $a$ . At early times, the radiation determines the history of the universe.

Dicke, Peebles, Roll, Wilkinson



---

## Important events in the history of the universe

- "Recombination"

Universe changes from ionized to neutral at  $T=3000\text{K}$ .  $p + e^- \rightarrow H$

- Q: What is the expansion parameter at recombination?
- Q: The ionization energy of hydrogen is  $13.6\text{eV}=13.6 \times 11600\text{K}/\text{eV}=160,000\text{K}$ . Why does recombination occur at such a low temperature?
- The cross section for scattering for free electrons is much higher than for bound electrons.
- The universe was opaque before recombination.

The cosmic microwave background is a snapshot of the universe at recombination at 400, 000 years.

- Helium forms. The early universe was too hot for nuclei (other than n and p) to exist.
  - At  $a = 10^{-9}$ , the universe became cool enough for  $n + p \rightarrow {}^2\text{H}$ . Then  ${}^4\text{He}$  and trace amounts of  ${}^7\text{Li}$  and  ${}^3\text{He}$  form.

◀ | ▶

$$2.7 / 11\,600 \times 10^{*^9}$$

$$2.32759 \times 10^6$$