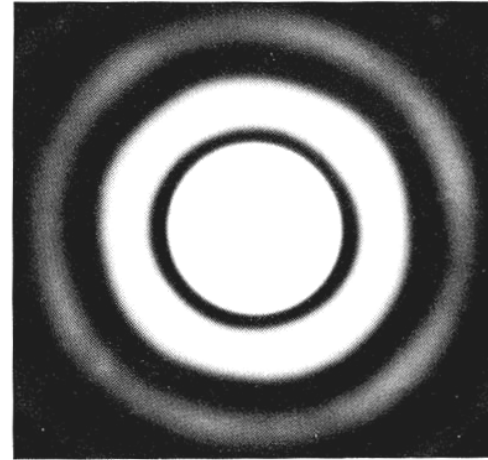


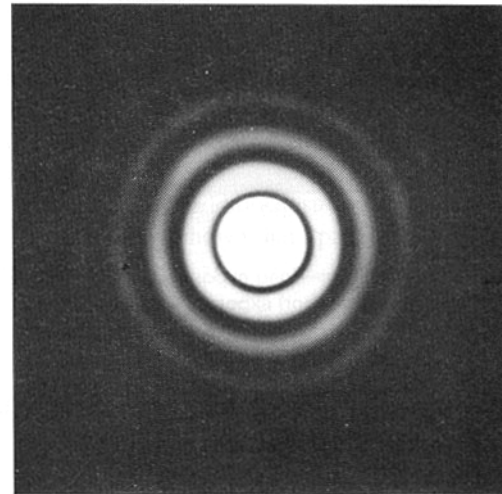
Diffraction from small and large circular apertures

Far-field
intensity pattern
from a small
aperture



Recall the Scale Theorem!
This is the Uncertainty
Principle for diffraction.

Far-field
intensity pattern
from a large
aperture



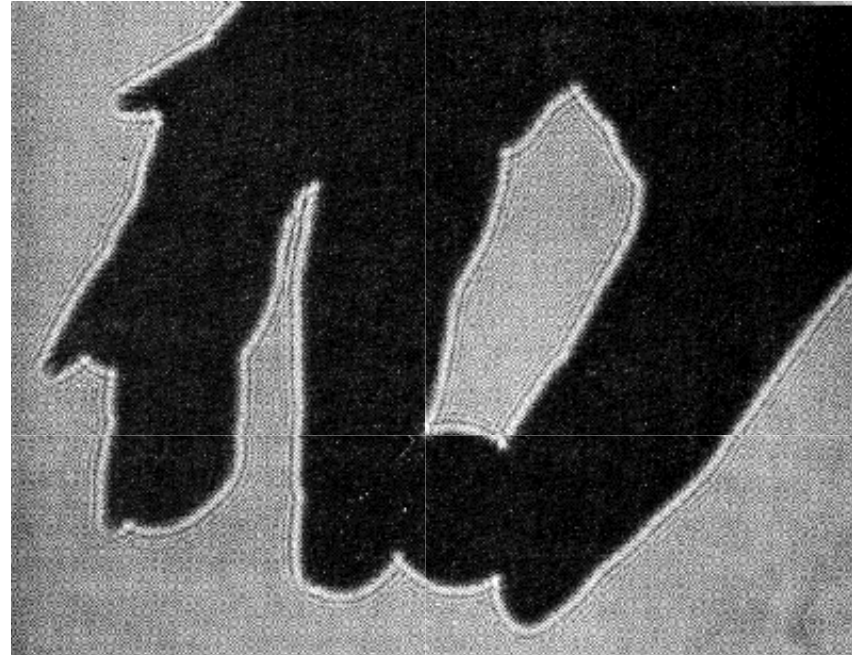
Diffraction

Light does not always travel in a straight line.

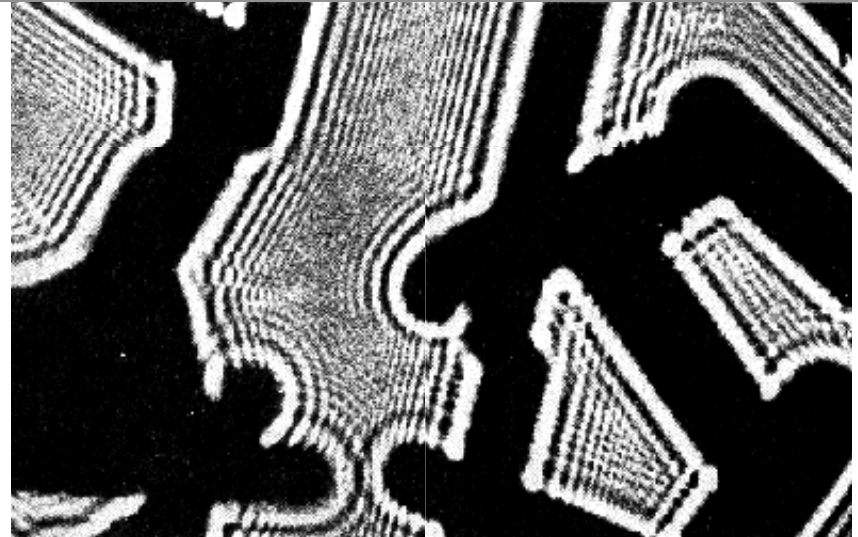
It tends to bend around objects. This tendency is called **diffraction**.

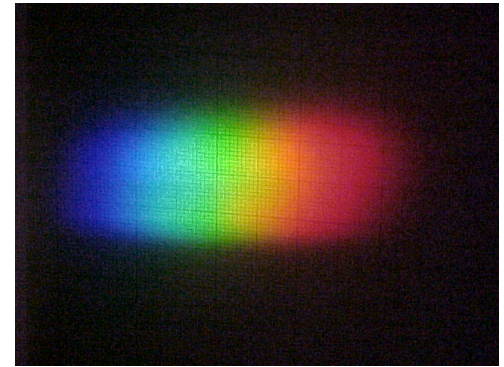
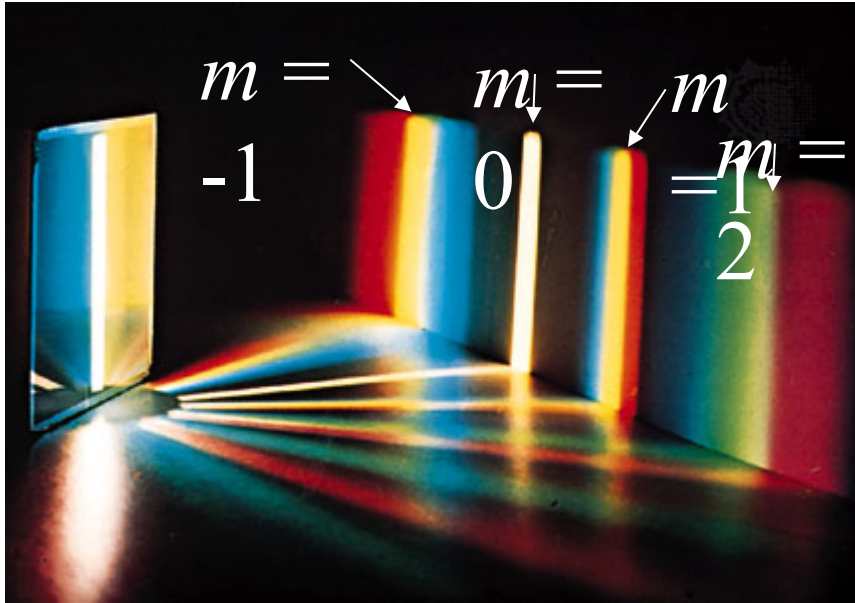
Any wave will do this, including matter waves and acoustic waves.

Shadow of a hand illuminated by a Helium-Neon laser



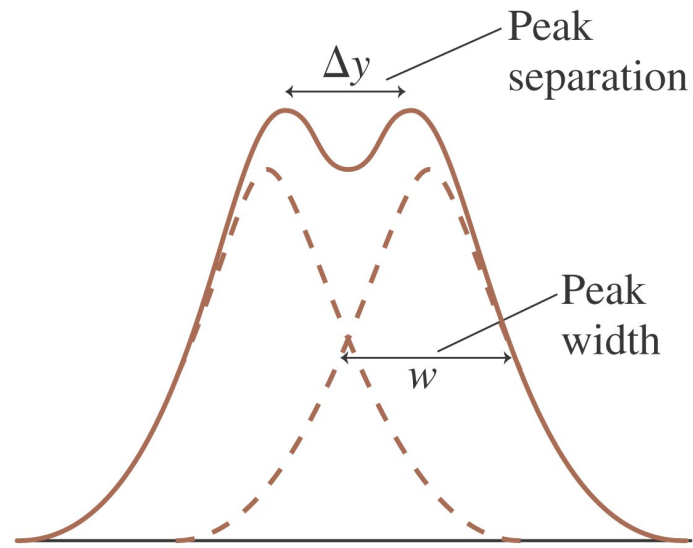
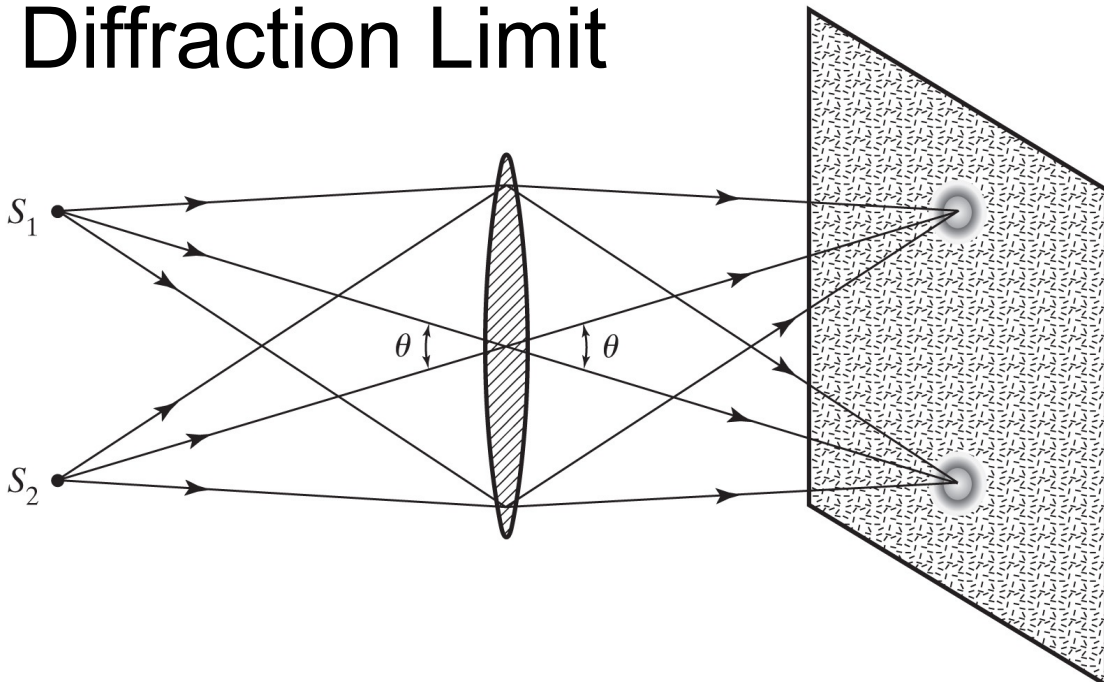
Shadow of a zinc oxide crystal illuminated by a electrons



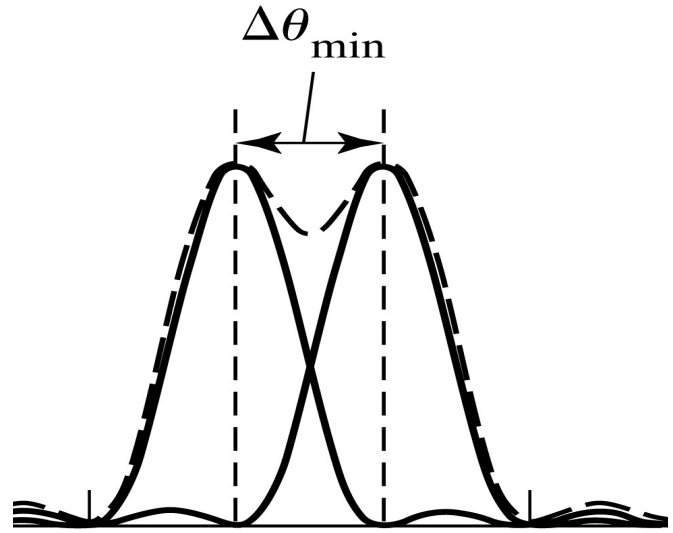
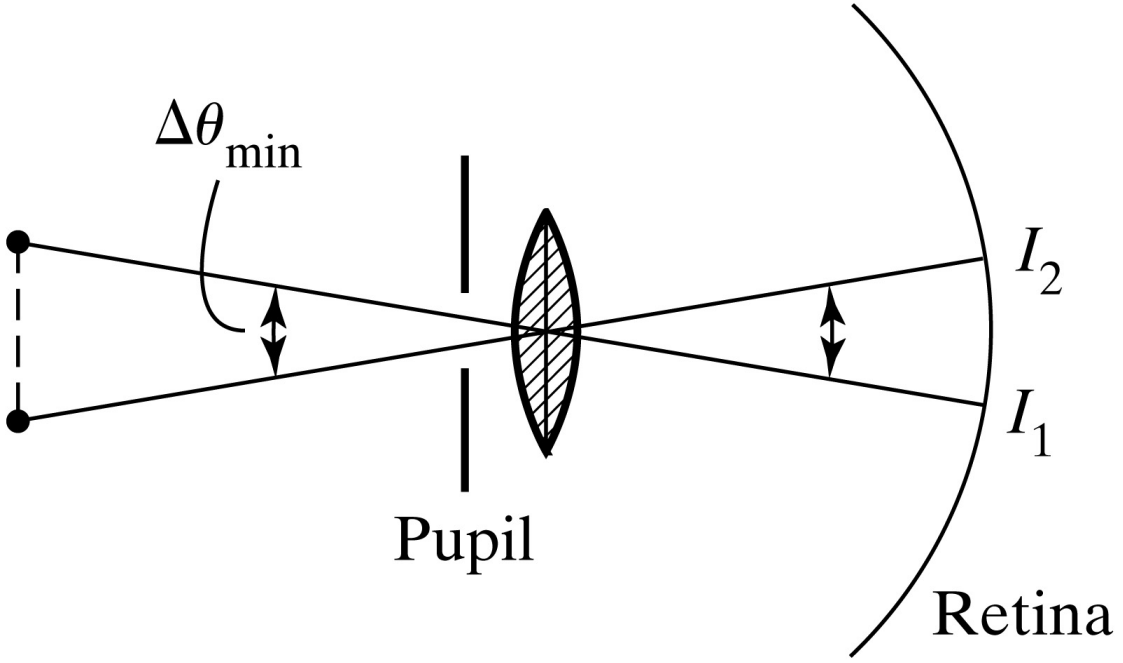


The dots on a CD are equally spaced (although some are missing, of course), so it acts like a diffraction grating.

Diffraction Limit



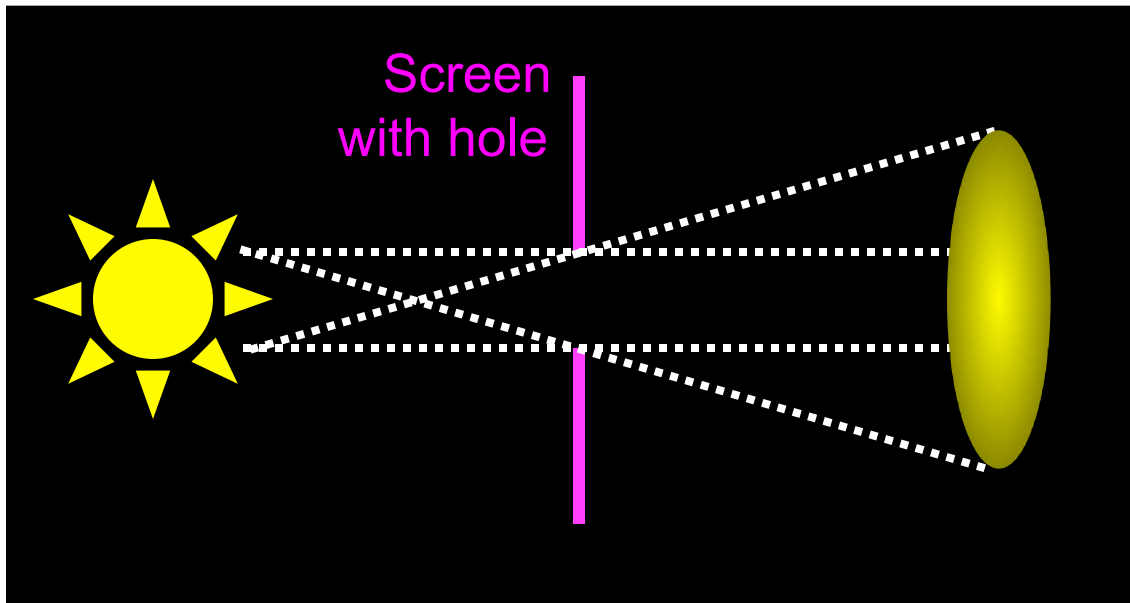
Two peaks are barely resolved when $\Delta y = w$.



Why it's hard to see diffraction

Diffraction tends to cause ripples at edges. But poor source temporal or spatial coherence masks them.

Example: a large spatially incoherent source (like the sun) casts blurry shadows, masking the diffraction ripples.

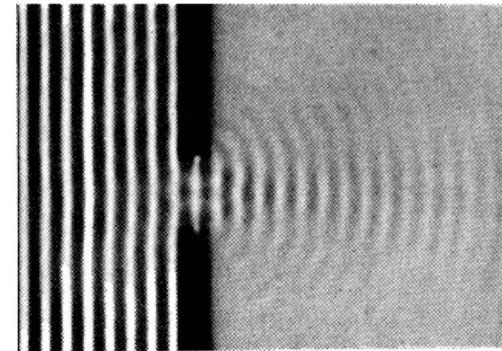


Untilted rays
yield a perfect
shadow of the
hole, but off-axis
rays blur the
shadow.

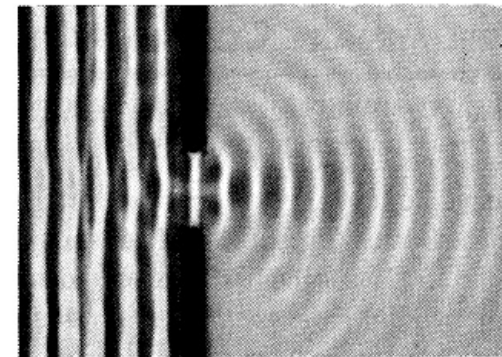
A point source is required.

Diffraction of a wave by a slit

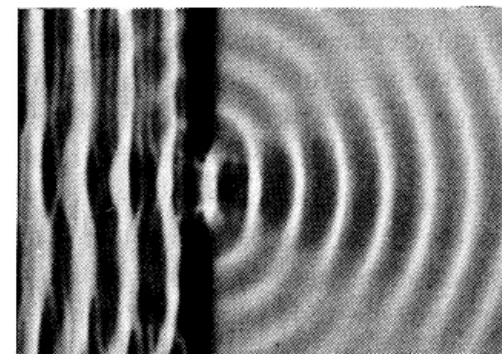
Whether waves in water or electromagnetic radiation in air, passage through a slit yields a diffraction pattern that will appear more dramatic as the size of the slit approaches the wavelength of the wave.



$\lambda = \text{slit size}$



$\lambda < \text{slit size}$



$\lambda \approx \text{slit size}$

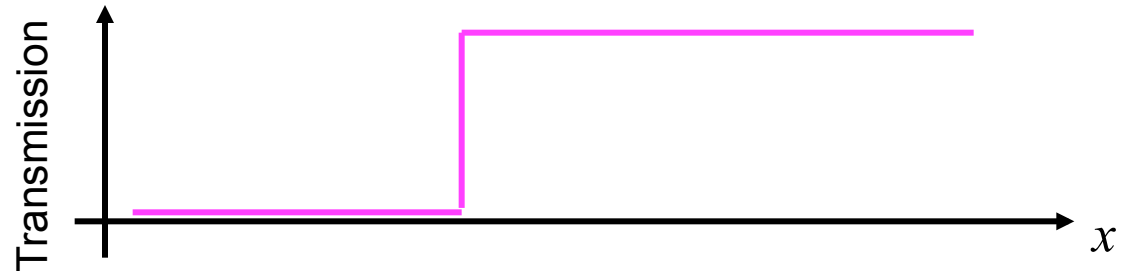
Diffraction of ocean water waves

Ocean waves passing through slits in Tel Aviv, Israel



Diffraction occurs for all waves, whatever the phenomenon.

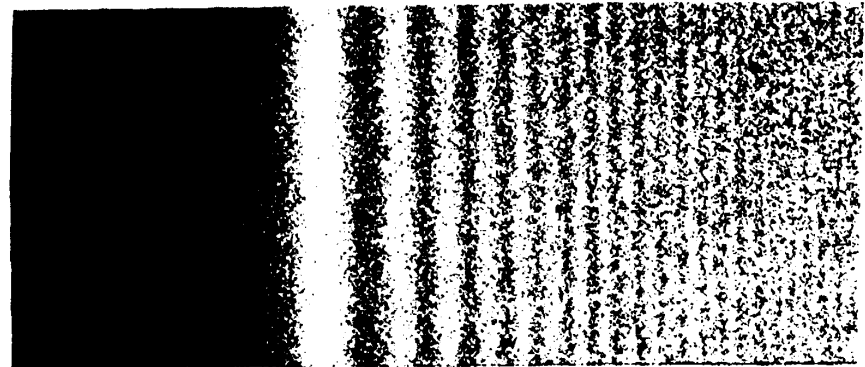
Diffraction by an Edge



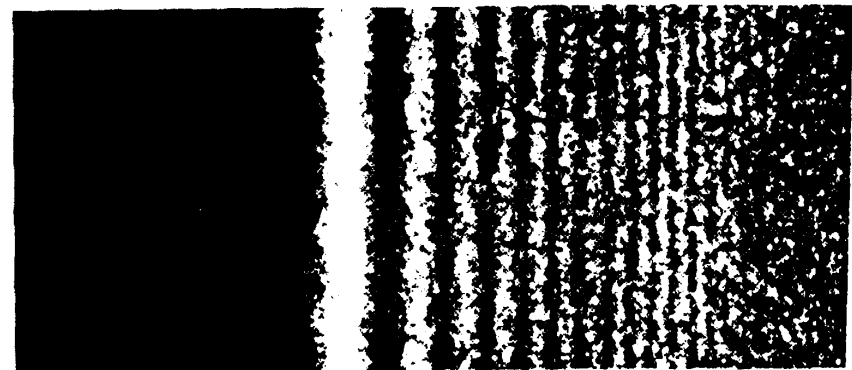
Even without a small slit, diffraction can be strong.

Simple propagation past an edge yields an unintuitive irradiance pattern.

Light passing by edge



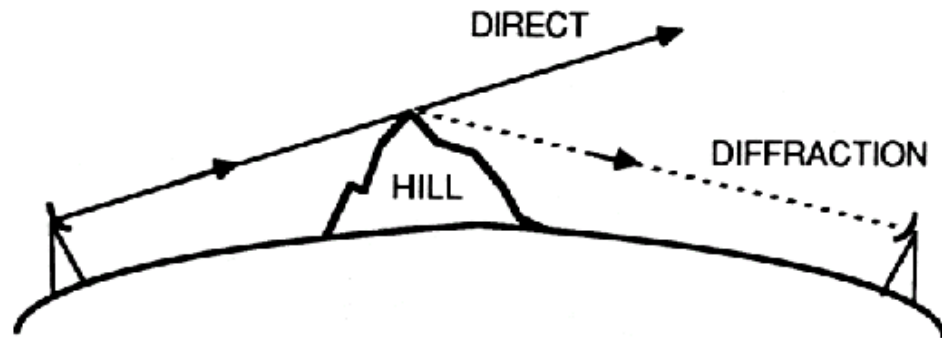
Electrons passing by an edge (MgO crystal)



Radio waves diffract around mountains.

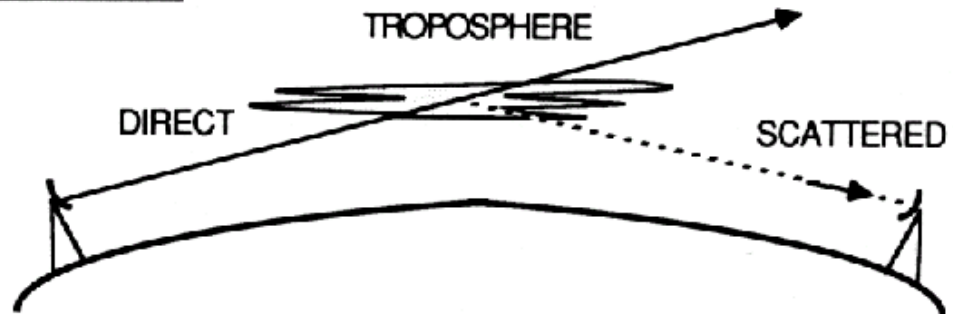
When the wavelength is km long, a mountain peak is a very sharp edge!

DIFFRACTION



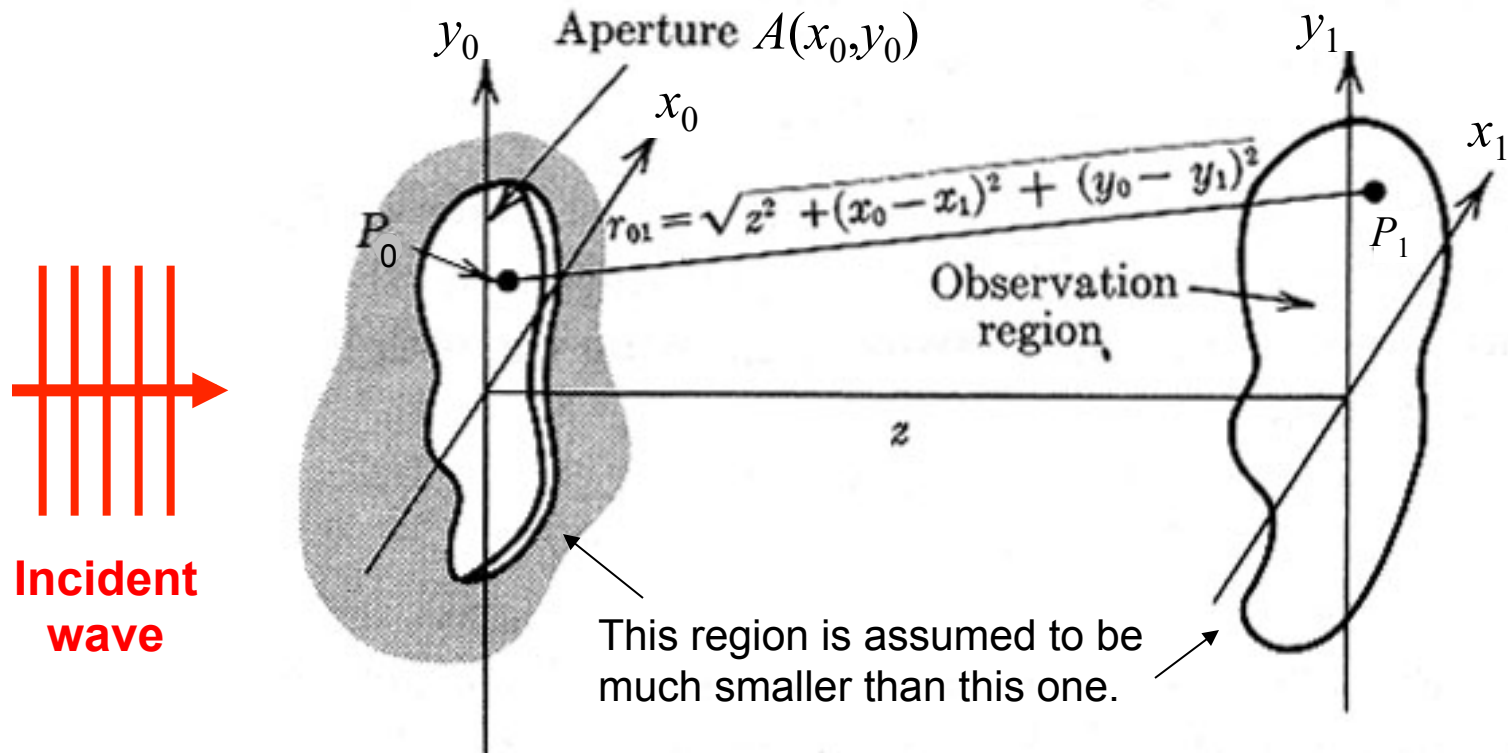
Another effect that occurs is scattering, so diffraction's role is not obvious.

TROPOSCATTER



Diffraction Geometry

We wish to find the light electric field after a screen with a hole in it. This is a very general problem with far-reaching applications.



What is $E(x_1, y_1)$ at a distance z from the plane of the aperture?

The Uncertainty Principle in Diffraction!

$$E(k_x, k_y) \propto \mathcal{F}\{A(x, y)E(x, y)\} \quad k_x = k x_1/z$$

Because the diffraction pattern is the **Fourier transform** of the slit, there's an uncertainty principle between the slit width and diffraction pattern width!

If the input field is a plane wave and $D_x = D_{x_0}$ is the slit width,

$$\Delta x \Delta k_x > 1$$

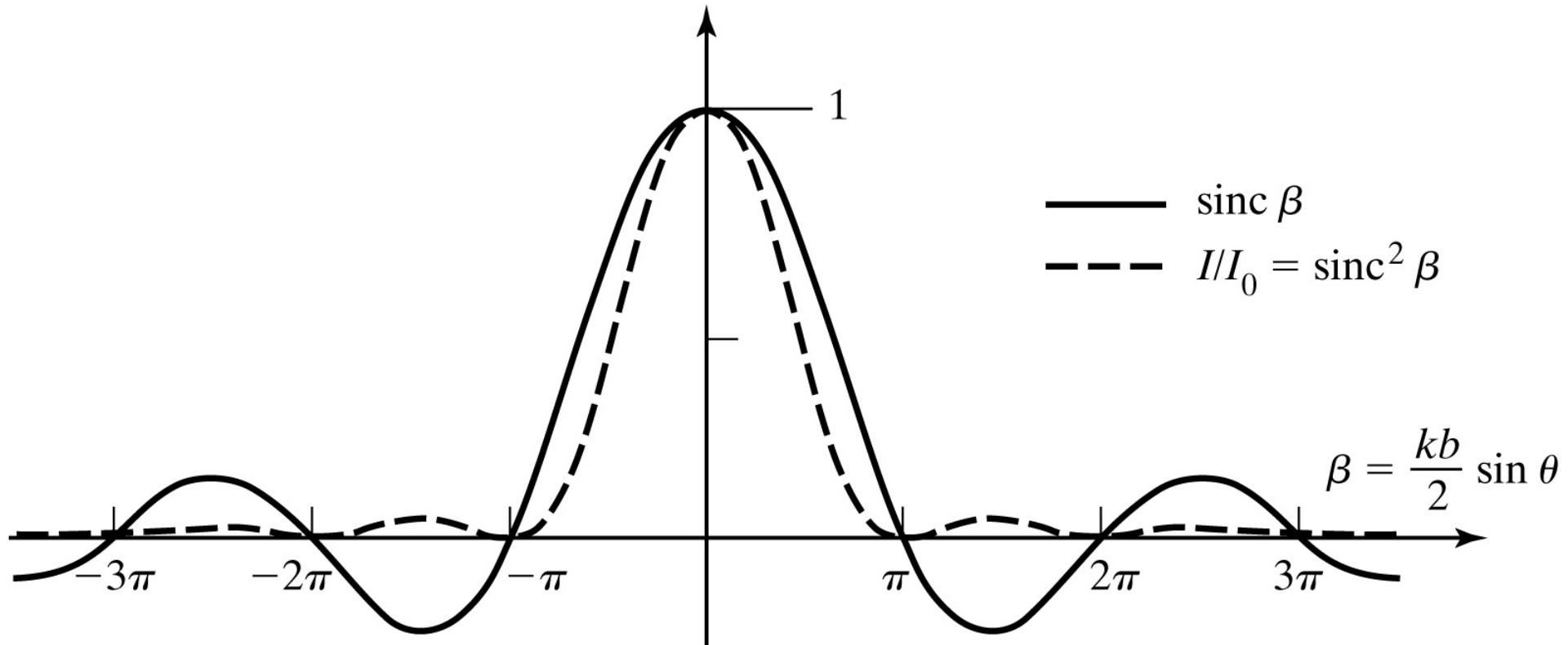
Or:

$$\Delta x_0 \Delta x_1 > z / k$$

The smaller the slit, the larger the diffraction angle and the bigger the diffraction pattern!

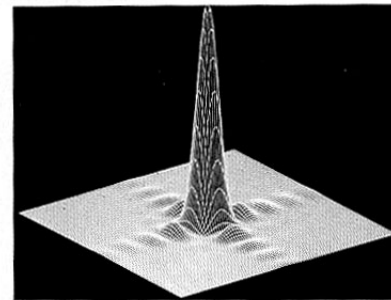
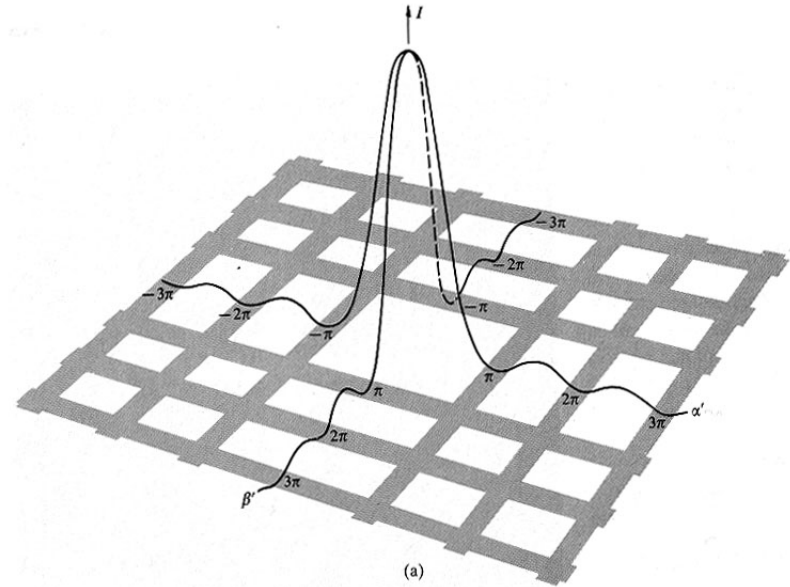
Fraunhofer Diffraction from a slit

Fraunhofer Diffraction from a slit is simply the Fourier Transform of a rect function, which is a sinc function. The irradiance is then sinc^2 .

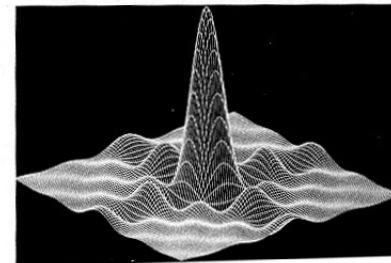


Fraunhofer Diffraction from a Square Aperture

The diffracted field is a sinc function in both x_1 and y_1 because the Fourier transform of a rect function is sinc.

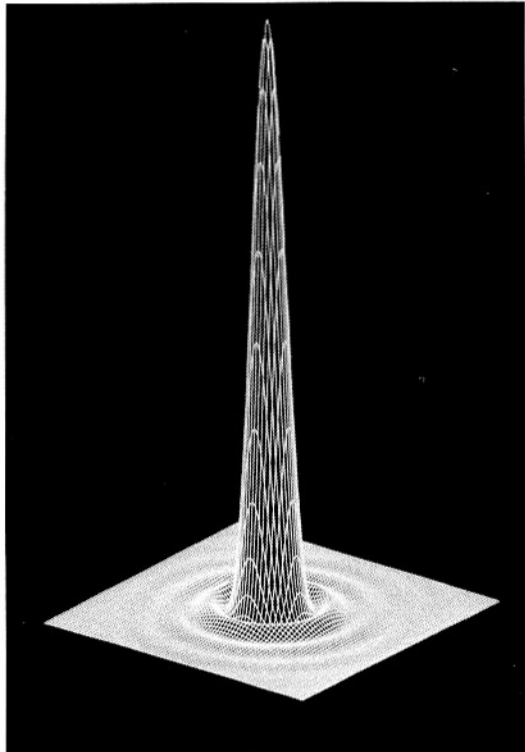


Diffracted irradiance

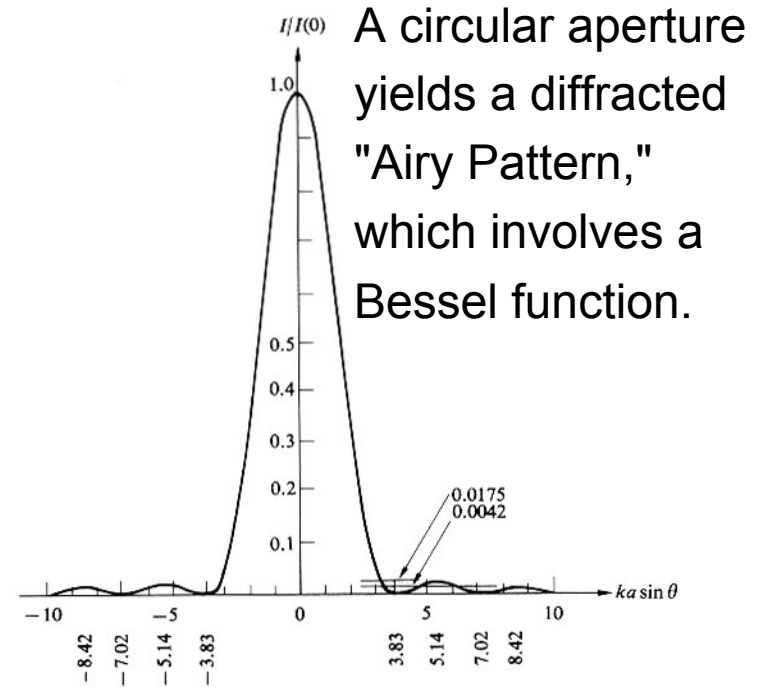


Diffracted field

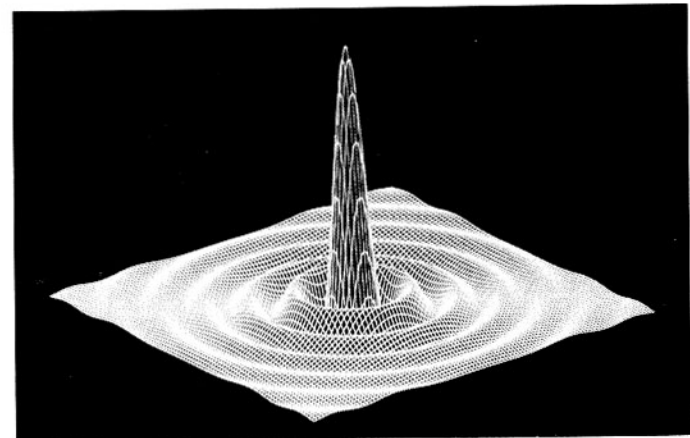
Diffraction from a Circular Aperture



Diffracted Irradiance



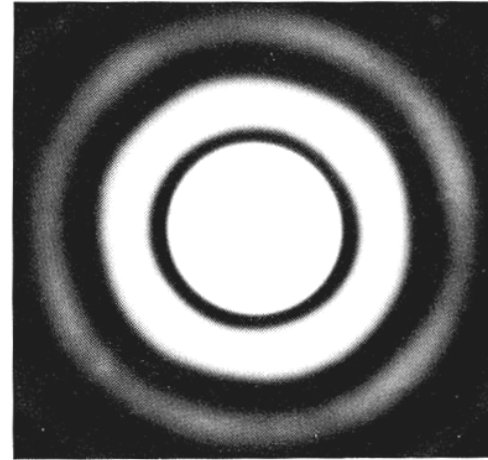
(a)



Diffracted field

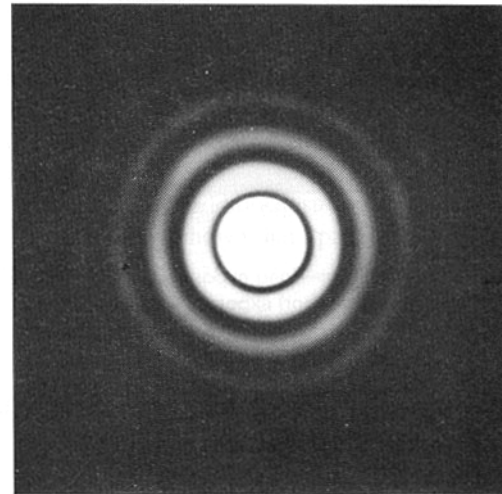
Diffraction from small and large circular apertures

Far-field
intensity pattern
from a small
aperture

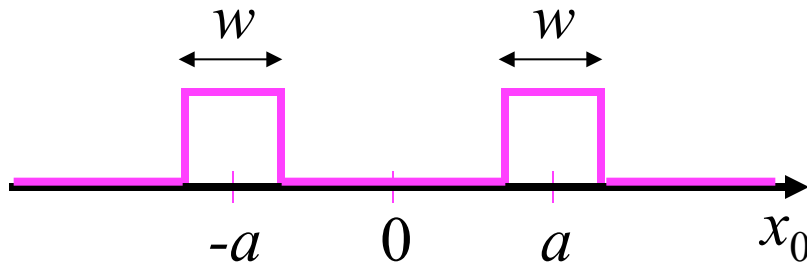


Recall the Scale Theorem!
This is the Uncertainty
Principle for diffraction.

Far-field
intensity pattern
from a large
aperture



Fraunhofer diffraction from two slits

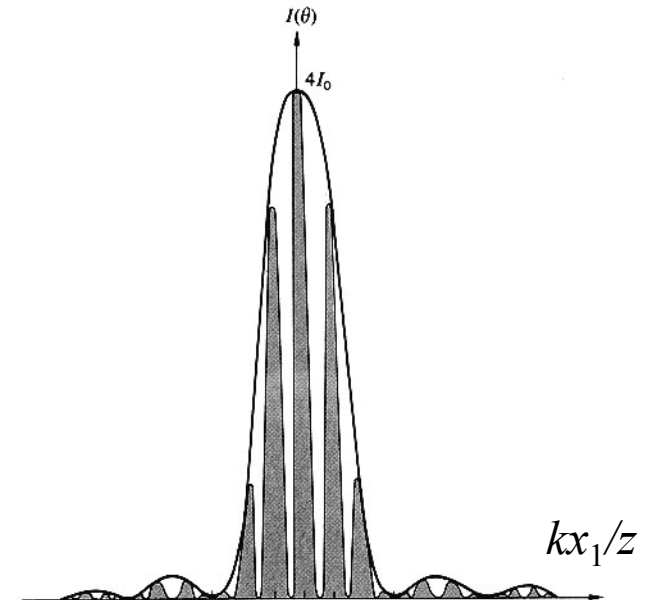
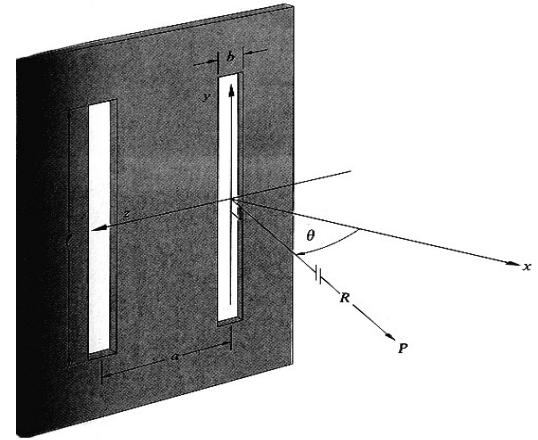


$$A(x_0) = \text{rect}[(x_0 + a)/w] + \text{rect}[(x_0 - a)/w]$$

$$E(x_1) \propto \mathcal{F}\{A(x_0)\}$$

$$\propto \text{sinc}[w(kx_1/z)/2] \exp[+ia(kx_1/z)] + \text{sinc}[w(kx_1/z)/2] \exp[-ia(kx_1/z)]$$

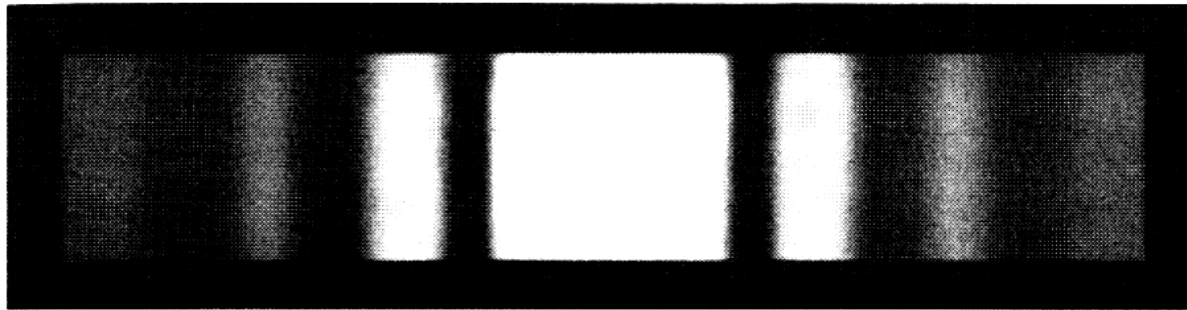
$$E(x_1) \propto \text{sinc}(w k x_1 / 2z) \cos(a k x_1 / z)$$



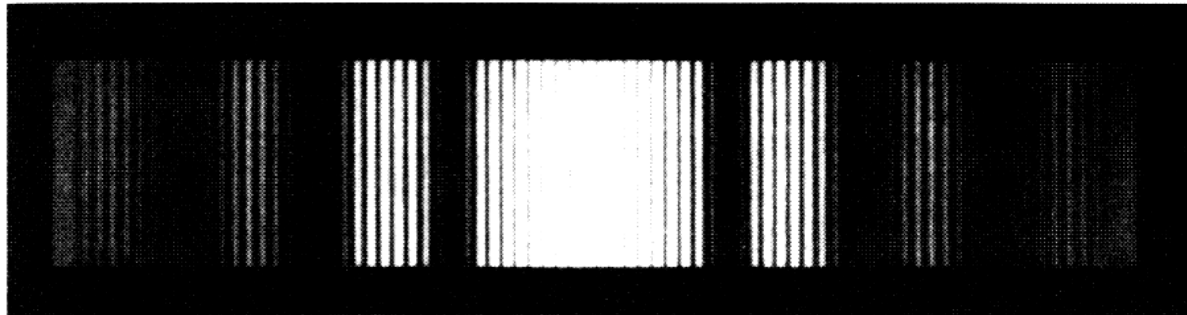
Diffraction from one- and two-slit screens

Fraunhofer diffraction patterns

One slit



Two slits



Diffraction Gratings

•Scattering ideas explain what happens when light impinges on a periodic array of grooves. Constructive interference occurs if the delay between adjacent beamlets is an integral number, m , of wavelengths.

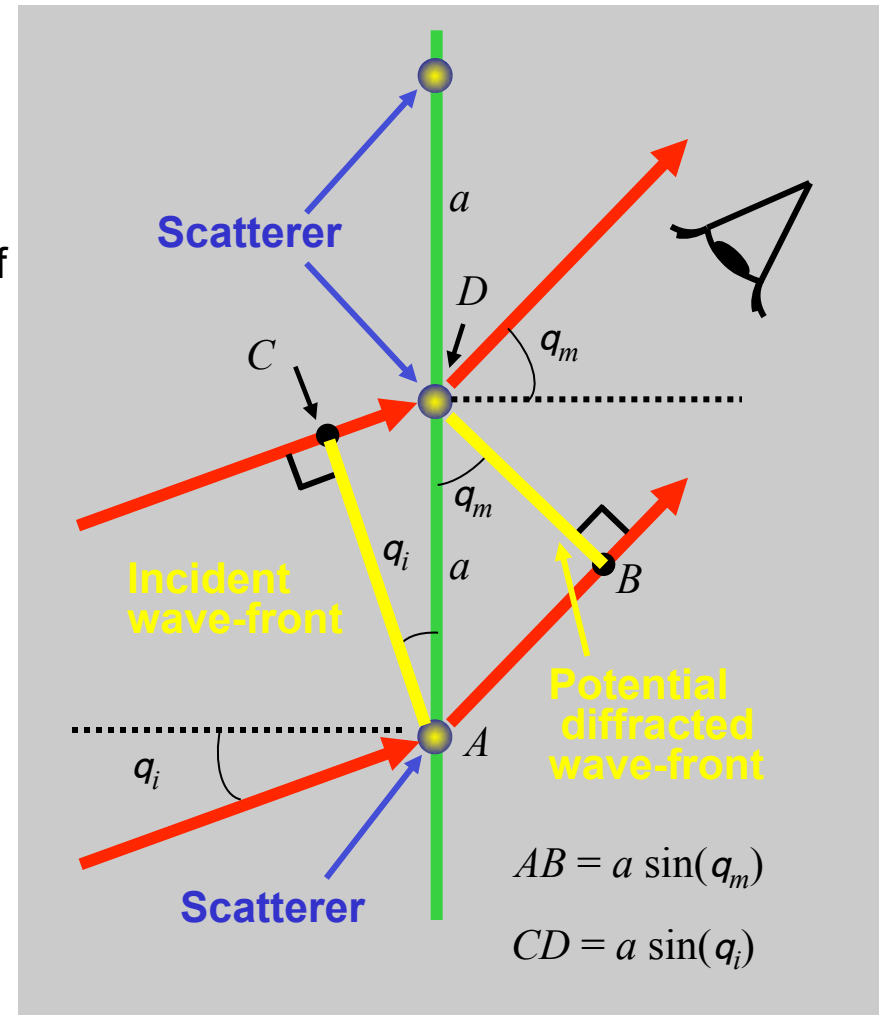
Path difference: $AB - CD = m\lambda$

$$a [\sin(\theta_m) - \sin(\theta_i)] = m\lambda$$

where m is any integer.

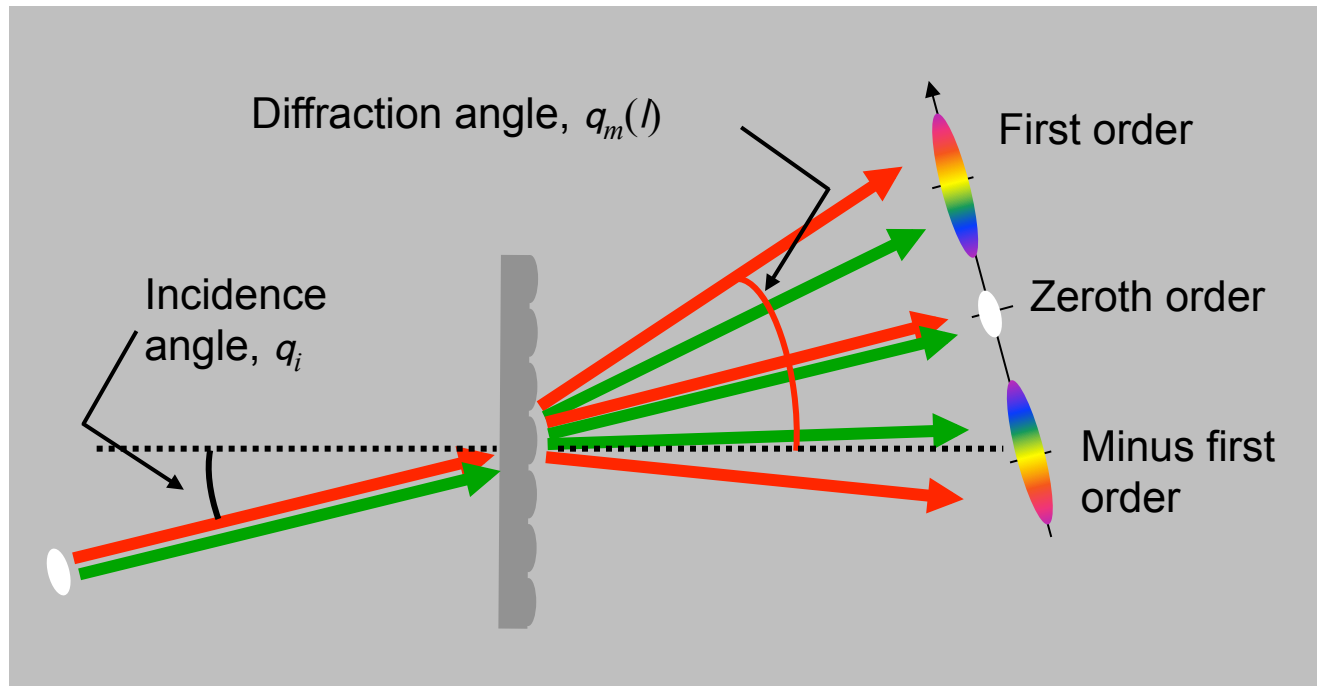
A grating has solutions of zero, one, or many values of m , or **orders**.

Remember that m and q_m can be negative, too.



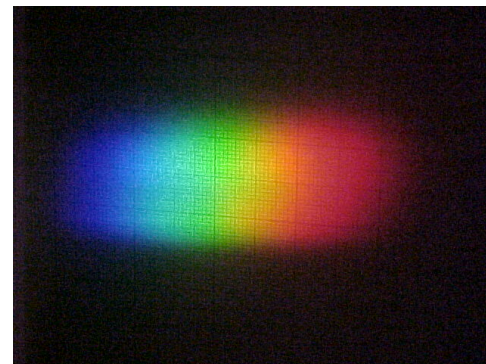
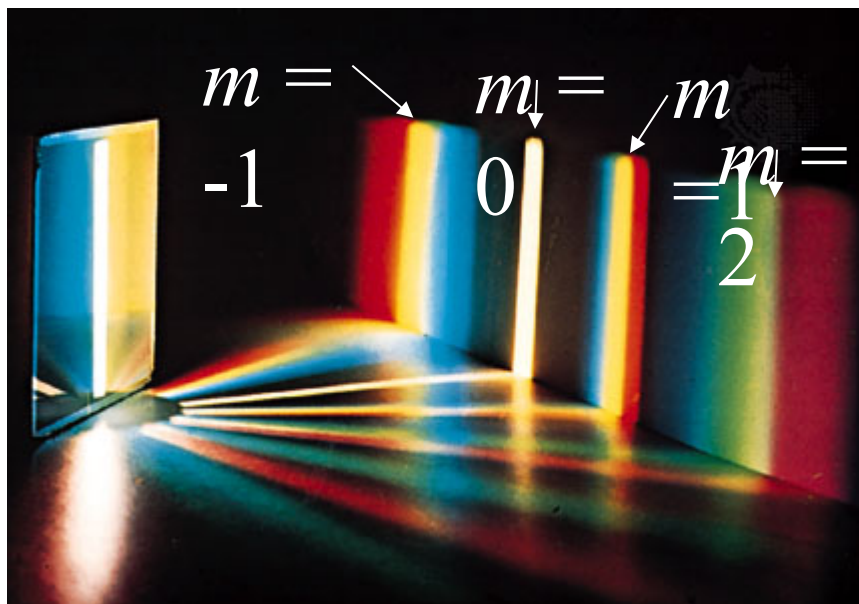
Diffraction orders

Because the diffraction angle depends on λ , different wavelengths are separated in the nonzero orders.

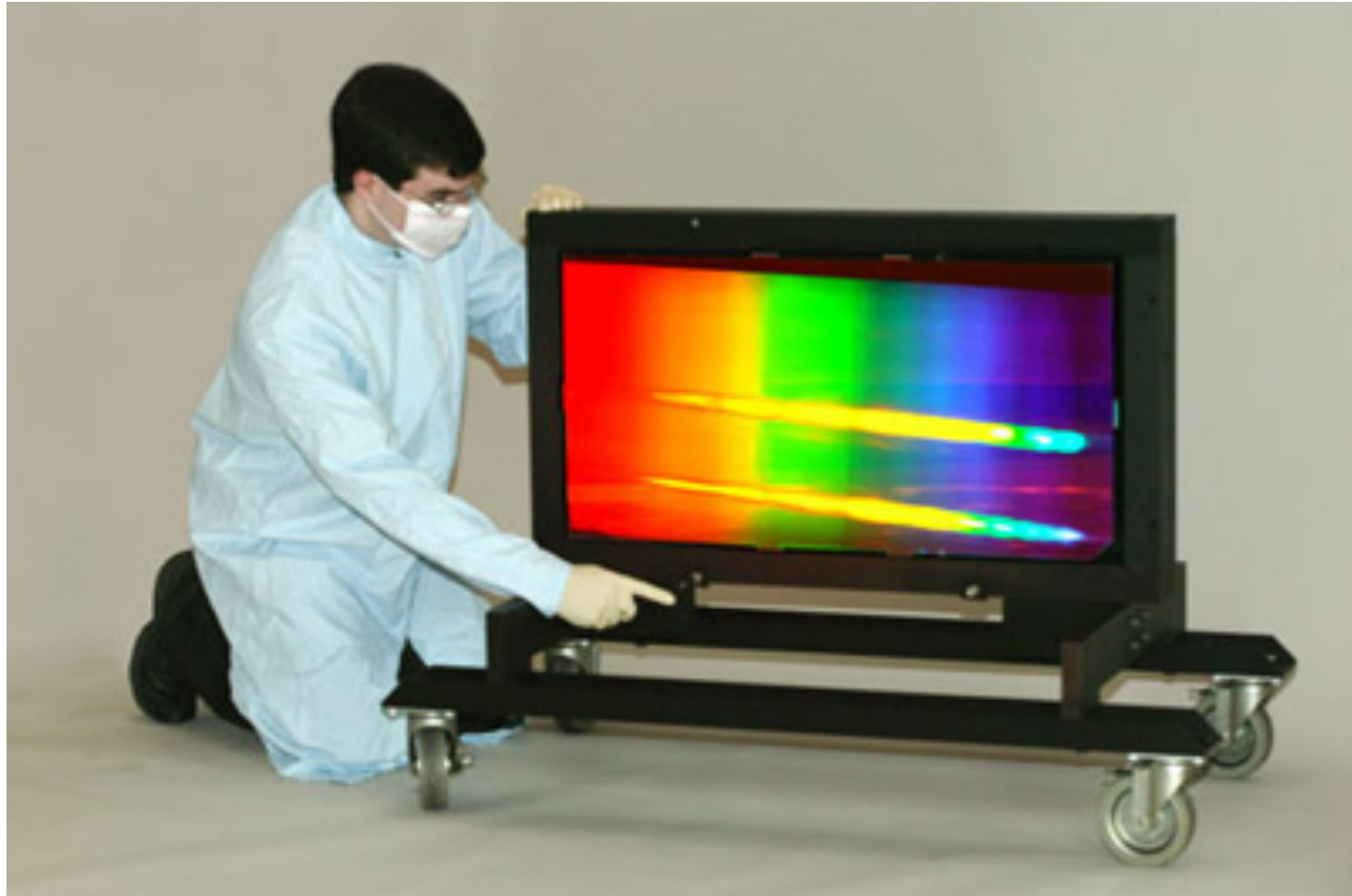


No wavelength dependence occurs in zero order.

The longer the wavelength, the larger its deflection in each nonzero order.



World's largest diffraction grating



Lawrence Livermore National Lab