Physics 842 – Fall 2011 Classical Electrodynamics II

Problem Set #5 – due Tuesday October 18

- 1. Imagine that at time t = 0 we place a localized macroscopic charge distribution $\rho(\mathbf{r})$ inside a conducting medium of conductivity σ . Describe how the charge density evolves in time. (The time scale for the charge to disperse is called the Maxwell relaxation time.)
- 2. A capacitor of arbitrary shape is filled with a dielectric medium with dielectric constant ε . If that same capacitor were filled with a conducting medium of conductivity σ , it would have a resistance *R*. Find the capacitance *C*.
- 3. The magnetoresistivity tensor relates the electric field to the current density, $E_i = \rho_{ik} j_k$. For the Drude model of magnetoconductivity we discussed in class, calculate ρ_{ik} for a uniform conducting medium in the presence of a constant magnetic field *B* pointing in the z direction.
- 4. A vacuum diode consists of two parallel plates (cathode and anode) separated by a distance *d*, held at a constant potential difference φ₀, inside an evacuated chamber. Electrons are emitted from the cathode by heating it. (We will assume that the velocity of the emitted electrons is initially zero, which is a good approximation for large enough φ₀.)

a) If the current density in the diode is *j*, calculate the electron velocity *v* and space charge density ρ as a function of *x*, where *x*=0 at the cathode and *x*=*d* at the anode. Assume that *j* is small enough that you can ignore the effects of ρ on the electric field.

b) For large *j* we cannot neglect the space charge. Using Poisson's equation and current conservation, derive a differential equation for $\phi(x)$.

c) Find a family of solutions to your equation that satisfy the boundary conditions $\phi(0)=0$ and $\phi(d)=\phi_0$. In the "space-charge limited" case, we have the additional condition that $d\phi/dx = 0$ at x=0. In this case, show that the current density *j* is proportional to $\phi_0^{3/2}$. This is a system that does not obey Ohm's Law!

Quiz #5

The quiz on Thursday, October 20, will consist of one of the following problems:

- Problems 1 4 on Problem Set #5
- Problems 1 and 3 at the end of Section 21