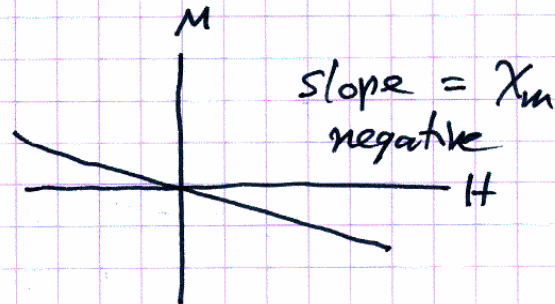
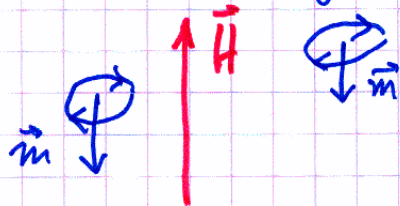


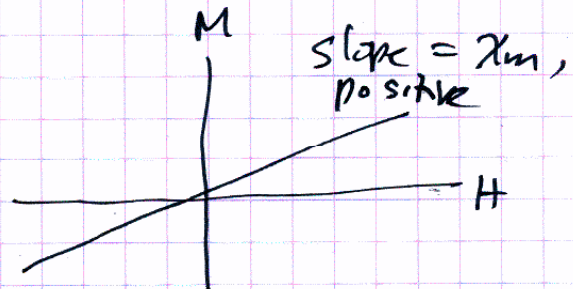
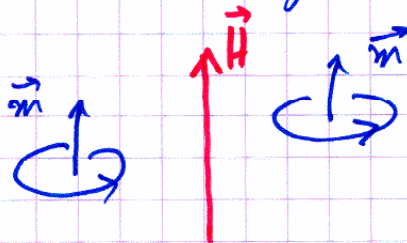
Ferromagnetism

• Diamagnetism



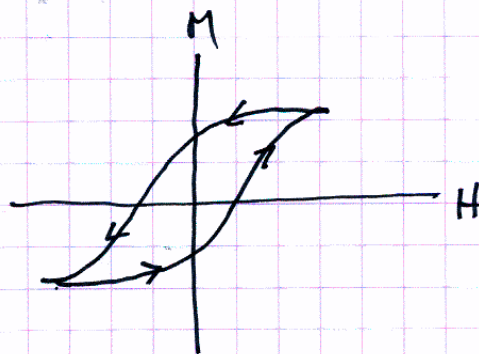
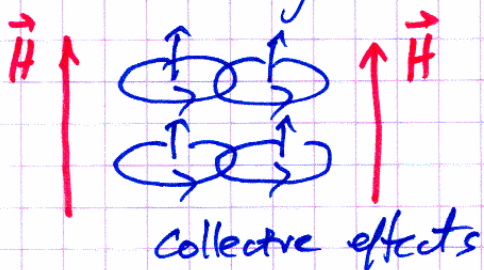
E.g., for Cu, $\chi_m = -9.6 \times 10^{-6}$

• Paramagnetism



E.g., Al, $\chi = 2.1 \times 10^{-5}$

• Ferromagnetism



Magnetic Domains

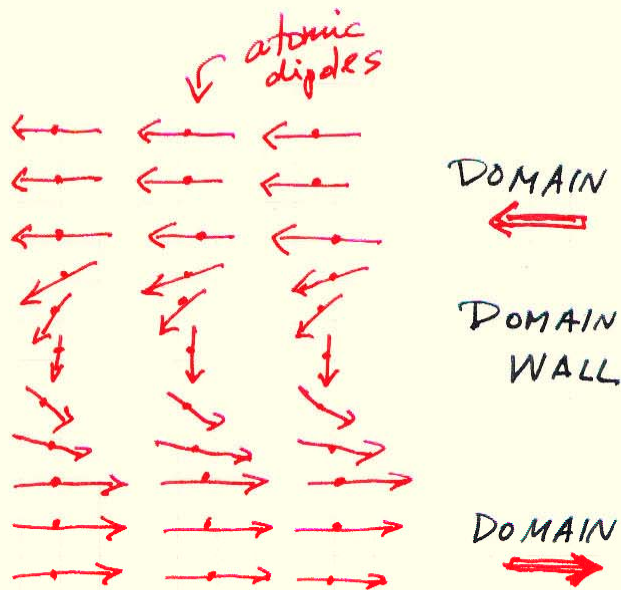
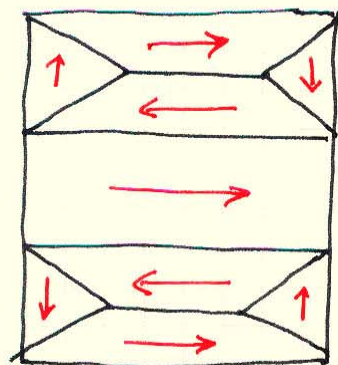
9.5/2

Consider a non-magnetized bar of iron.

Macroscopically, $\vec{M}(\vec{x}) = 0$.

But in small domains, all the atomic dipoles are aligned by the "exchange interaction," a quantum effect.

Magnetic domains



How small is a magnetic domain?

At room temperature, with field $\vec{H} = 0$, the range is 10^{15} to 10^{20} atoms for pure crystalline iron; the typical mass is micrograms.

A macroscopic sample is many domains, with random orientations; so bulk $\vec{M} = 0$.

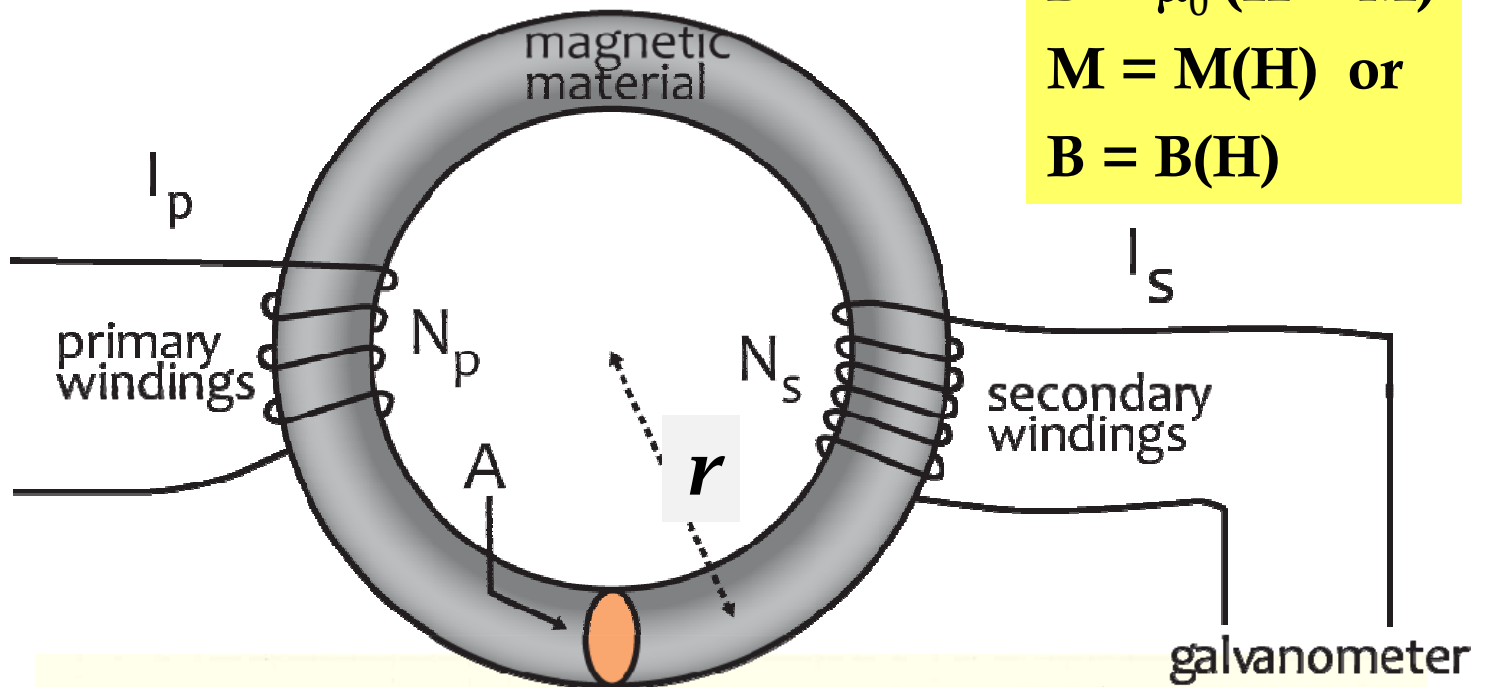
Now apply a magnetizing field \vec{H} .

Domain walls move; aligned domains grow and misaligned domains shrink.

\vec{M} develops parallel to \vec{H} .

The Rowland Ring ...

... for measuring **B** versus **H**



$$B = \mu_0 (H + M)$$

$$M = M(H) \text{ or}$$

$$B = B(H)$$

9.5/3

The primary current I_p creates a magnetizing field \vec{H} . When I_p changes, a current is induced in the secondary coil by electromagnetic induction. Observe ΔH and ΔB .

$$\oint \vec{H} \cdot d\vec{l} = I_{free}$$

$$H \cdot 2\pi r = N_p I_p$$

$$H = \frac{N_p I_p}{2\pi r}$$

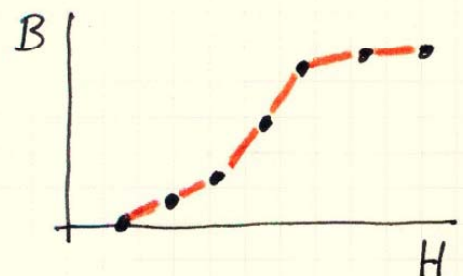
$$\Delta H = \frac{N_p \Delta I_p}{2\pi r}$$

$$emf = - \frac{d\Phi}{dt}$$

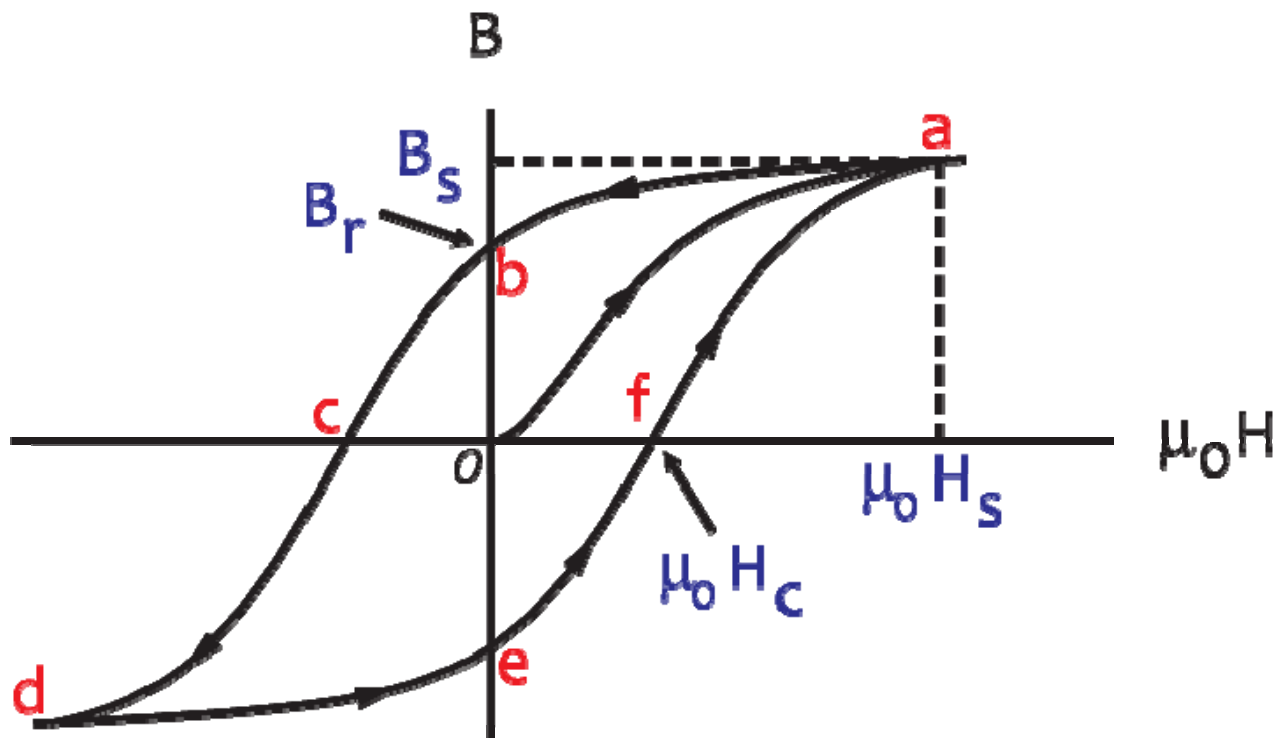
$$I_s R = N_s \frac{dB}{dt} A$$

$$\Delta B = \frac{R \Delta Q_s}{N_s A}$$

Trace out **B** versus **H**



Magnetization Curve of a Ferromagnet



B_s = saturation field (all domains aligned)
 B_r = remanent field (permanent magnet)
 H_c = coercive force (static field required to demagnetize the sample)

Hysteresis Loop

The energy per unit volume supplied for a cycle $abcdefa$ is equal to the area enclosed in the (H,B) plane; this is *heating* the magnet.

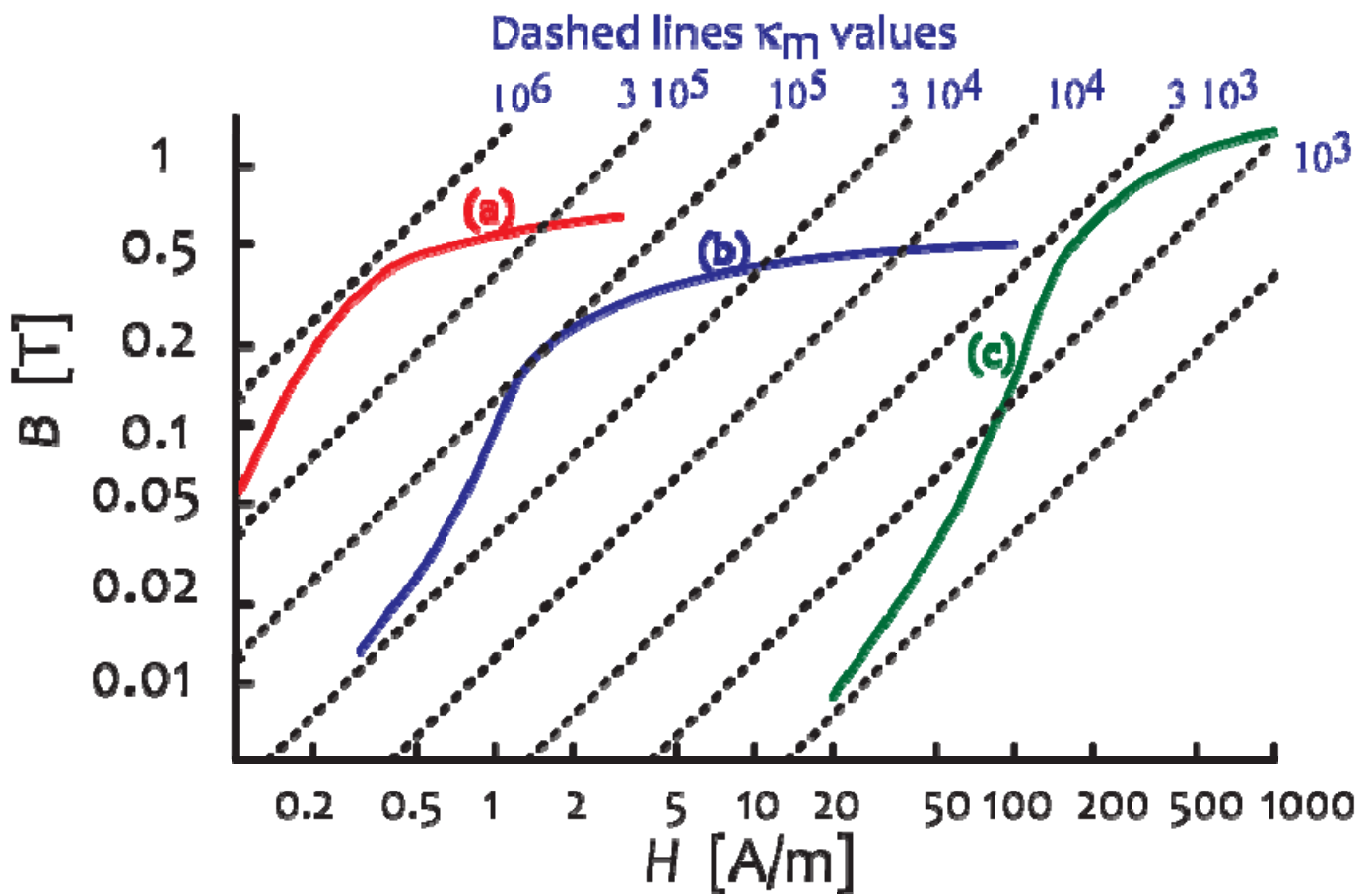
Applications

Permeability $\mathbf{B} = \mu \mathbf{H}$

For a ferromagnet, $\mathbf{B} = \mu(H) \mathbf{H}$

Relative permeability κ_m

$$\kappa_m = \frac{\mu}{\mu_0} = \frac{B(H)}{\mu_0 H}$$

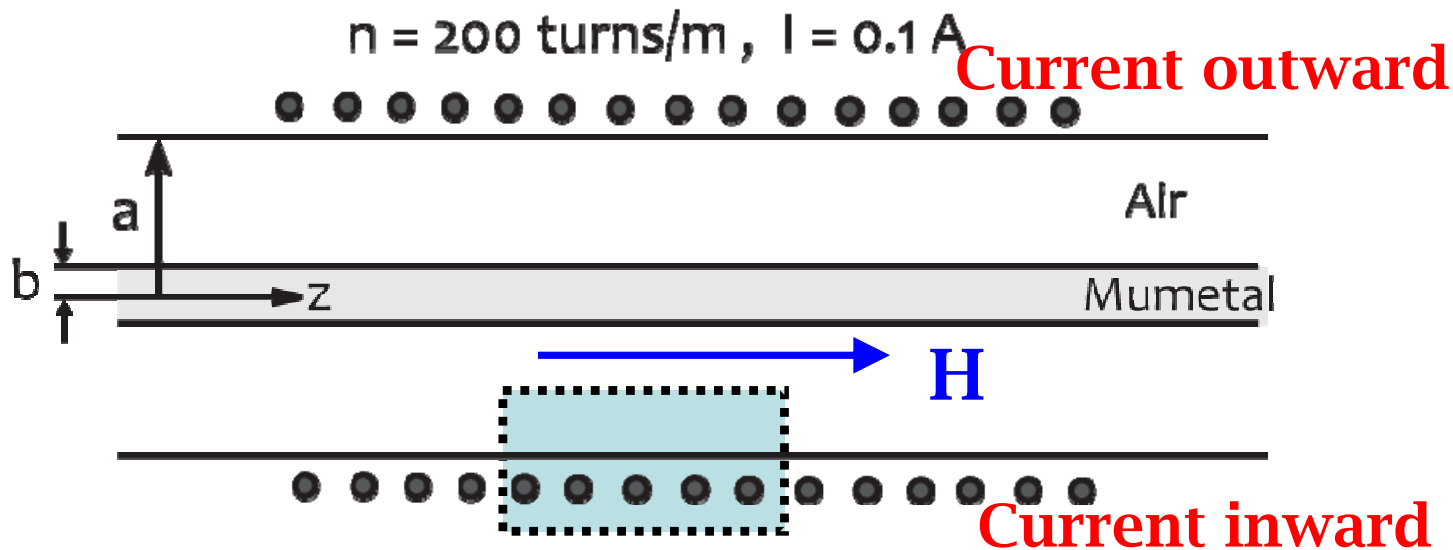


(a) Supermalloy; (b) Mumetal; (c) Iron

Ni(79%)Mo(5%)Fe(16%) Ni(77)Fe(15)Cu(4)Mo(4) Fe

Example

Consider a cylindrical solenoid with a thin core of mumetal on the axis of the cylinder. Determine H , B and M .



By symmetry $\vec{H} = H_z \hat{e}_z$ 9.5/6

Apply Ampère's law : $\oint \vec{H} \cdot d\vec{l} = I_{free}$

$$H L = n L I$$

$$H = n I \quad \text{inside the solenoid}$$

field	in the air	in the mumetal
H	$nI = 20 \text{ A/m}$	$nI = 20 \text{ A/m}$
B	$\mu_0 H = 2.5 \times 10^{-5} \text{ T}$	$0.45 \text{ T} \quad (*)$
M	0	$3.6 \times 10^5 \text{ A/m} \quad (**)$

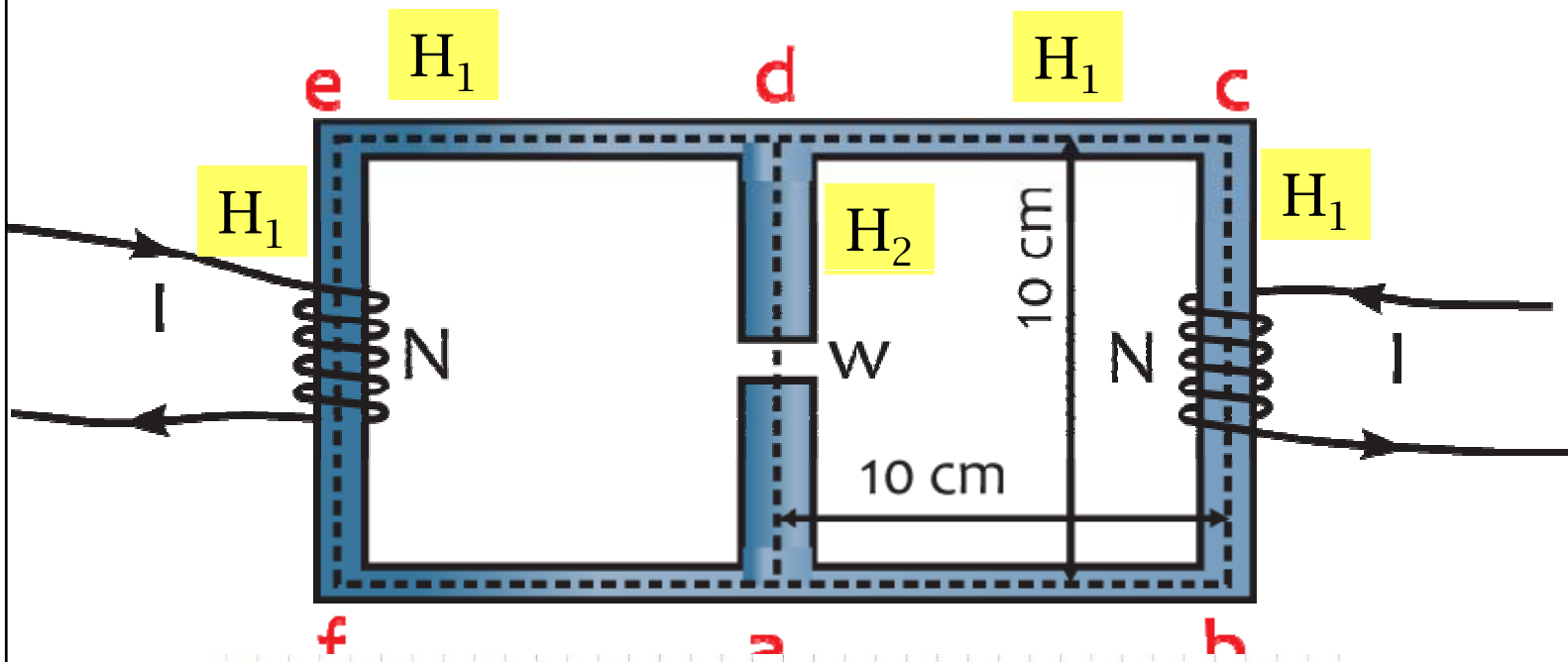
(*) See Curve (b)

$$(**) M = \frac{B}{\mu_0} - H \approx \frac{B}{\mu_0}$$

General Strategy for magnetic circuits 9.5/7

- (1) $\oint_C \vec{H} \cdot d\vec{l} = I_{\text{free}} \Rightarrow$ equations for \vec{H}
- (2) • $\vec{B} = \mu_0 \vec{H}$ in free space; or $\vec{H} = \vec{B} / \mu_0$
 - Use \vec{B} versus \vec{H} graph for ferromagnetic material.
- (3) B_n is continuous at any surface.
- (4) Solve the coupled equations.

Example Consider the iron electromagnet in the figure. Calculate the current I such that $B = 1$ tesla in the gap; $w = 1$ cm.



$$\oint_{abcda} \vec{H} \cdot d\vec{l} = NI$$

$$\hookrightarrow = 3H_1L + H_2(L-w) + H_{\text{gap}}w$$

$$H_{\text{gap}} = \frac{B_{\text{gap}}}{\mu_0} = \frac{1 \text{ T}}{4\pi \times 10^{-7} \frac{\text{Tm}}{\text{A}}} = 8.0 \times 10^5 \text{ A/m}$$

$$B_n \text{ is continuous so } B_2 = B_{\text{gap}} = 1 \text{ T}$$

$$B_2 = 1 \text{ T} \Rightarrow H_2 = 500 \text{ A/m} \quad (\text{see the graph})$$

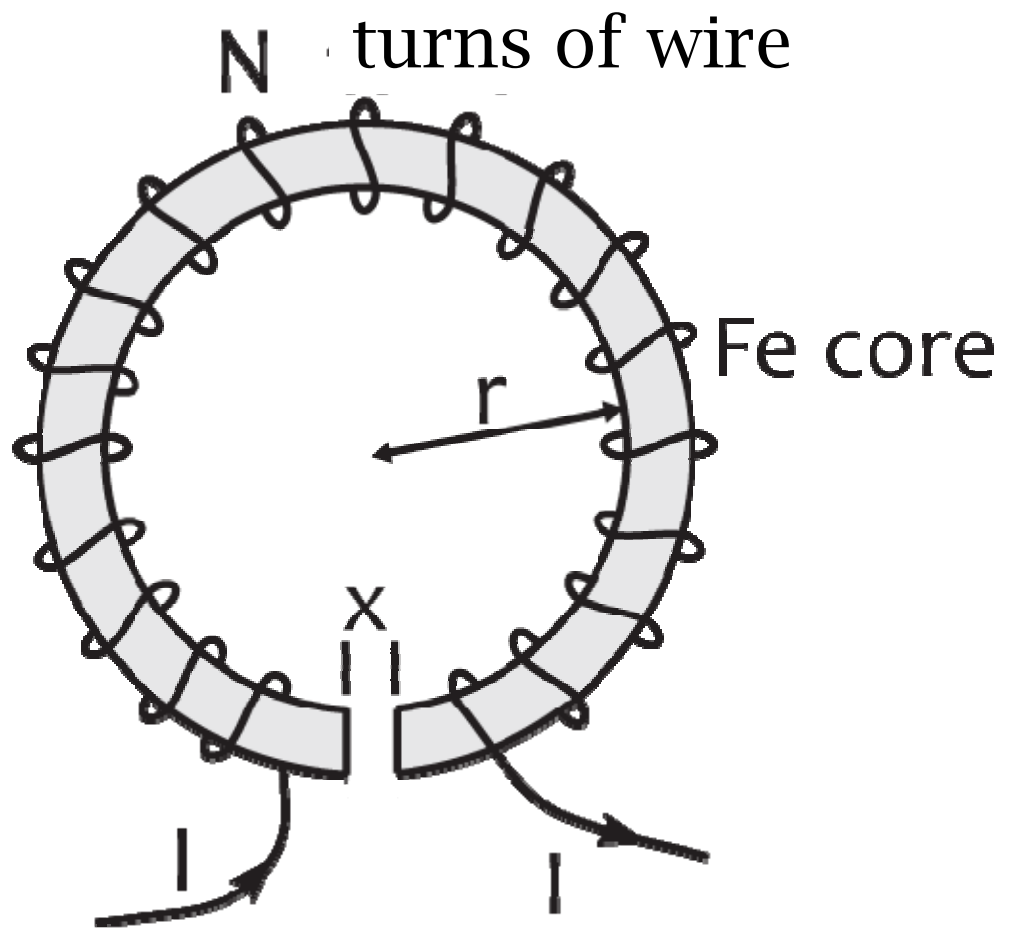
$$\text{Magnetic flux is conserved } (\oint_S \vec{B} \cdot d\vec{A} = 0)$$

$$\therefore B_1 + B_1 = B_2 \quad (\text{points a and d})$$

$$B_1 = 0.5 \text{ T} \Rightarrow H_1 = 185 \text{ A/m} \quad (\text{see the graph})$$

$$I = \frac{3H_1L + H_2(L-w) + H_{\text{gap}}w}{N} = 16 \text{ A.}$$

Quiz



Data:

$$N = 2000$$

$$2\pi r = 1 \text{ m}$$

$$x = 1 \text{ cm.}$$

Calculate the current I for which magnetic field in the gap would be 0.2 T.

