## Chapter 2

## Kinematics in One Dimension

Kinematics deals with the concepts that are needed to describe motion.

**Dynamics** deals with the effect that forces have on motion.

Together, kinematics and dynamics form the branch of physics known as *Mechanics*.

#### 2.0 Definitions

Speed v: is a positive scalar Velocity  $\vec{\mathbf{v}}$ : is a vector.

Instantaneous - at a time t.

Magnitude of the velocity vector is the speed, v.

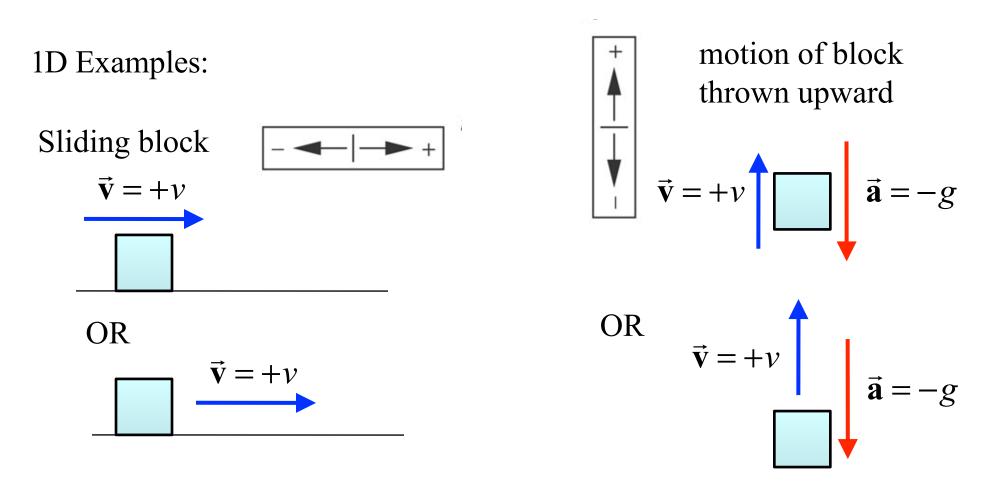
Direction - for projectiles (2 or 3D), direction is an angle.

- for motion along a line (1D), direction is a sign.

$$\vec{\mathbf{v}} = +v \quad \text{or} \quad \vec{\mathbf{v}} = -v$$

#### 2.0 Definitions, continued

In Chapter 2: All motion is along a line. It could be horizontal (cars, boats, humans), or vertical (acceleration due to gravity) MUST decide which direction is going to be POSITIVE



#### 2.0 Definitions, continued

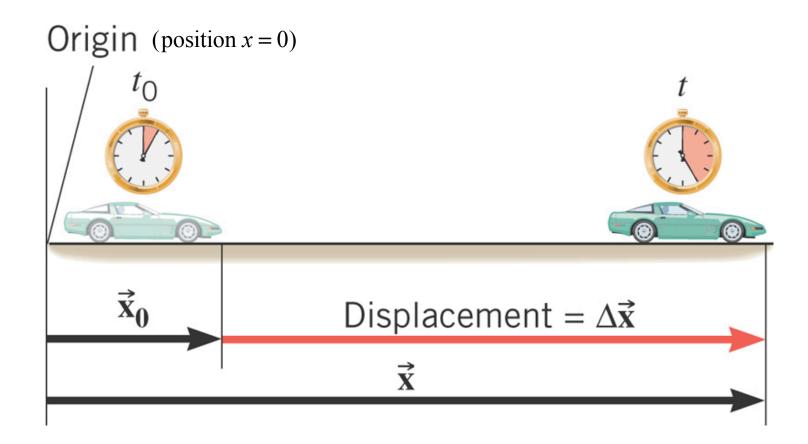
Moving: How can one tell if an object is moving at time, t?

Look a little bitty time ( $\varepsilon$ ) earlier,  $t' = t - \varepsilon$ ,

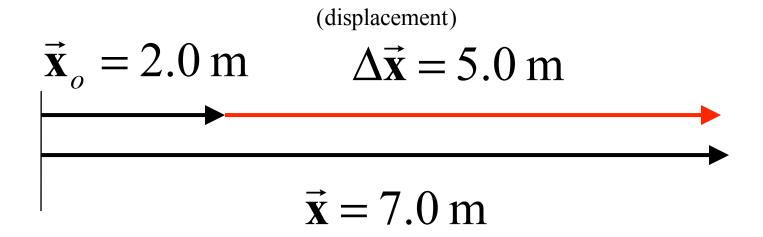
or look a little bitty time ( $\varepsilon$ ) later,  $t' = t + \varepsilon$ and see if the object is at the same place.

If object is at the same place, it is not moving (stationary). If object is NOT at the same place --- it is MOVING.

If an object is thrown upward, at the highest point v = 0, instantaneously, but the object IS MOVING! Turning around is motion, it is moving.

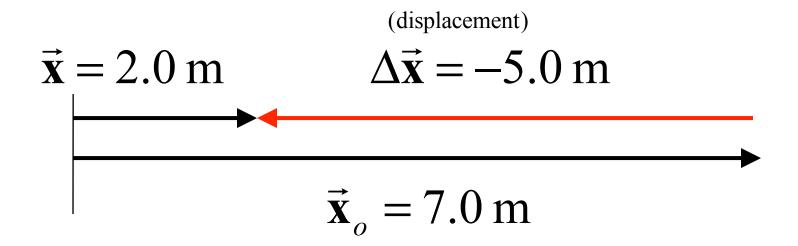


$$\vec{\mathbf{x}}_o = \text{initial position (at } t = 0)$$
  $\vec{\mathbf{x}} = \text{final position}$  
$$\Delta \vec{\mathbf{x}} = \vec{\mathbf{x}} - \vec{\mathbf{x}}_o = \text{displacement}$$



$$\Delta \vec{x} = \vec{x} - \vec{x}_o = 7.0 \text{ m} - 2.0 \text{ m} = 5.0 \text{ m}$$

(Note:  $\vec{x}_0 + \Delta \vec{x} = \vec{x}$  initial position + displacement = final position)



$$\Delta \vec{x} = \vec{x} - \vec{x}_o = 2.0 \text{ m} - 7.0 \text{ m} = -5.0 \text{ m}$$

$$\vec{\mathbf{x}}_o = -2.0 \,\mathrm{m}$$

$$\vec{\mathbf{x}} = 5.0 \,\mathrm{m}$$

$$\Delta \vec{\mathbf{x}} = 7.0 \,\mathrm{m}$$

(displacement)

$$\Delta \vec{\mathbf{x}} = \vec{\mathbf{x}} - \vec{\mathbf{x}}_o = 5.0 \text{ m} - (-2.0) \text{m} = 7.0 \text{ m}$$

**Average speed** is the distance traveled divided by the time required to cover the distance.

Average speed = 
$$\frac{\text{Distance}}{\text{Elapsed time}}$$

SI units for speed: meters per second (m/s)

## **Example 1** Distance Run by a Jogger

How far does a jogger run in 1.5 hours (5400 s) if his average speed is 2.22 m/s?

Average speed = 
$$\frac{\text{Distance}}{\text{Elapsed time}}$$

Distance = (Average speed)(Elapsed time)  
= 
$$(2.22 \text{ m/s})(5400 \text{ s}) = 12000 \text{ m}$$

## Clicker Question 2.1

A jogger travels 1500 m at an average speed of 2.00 m/s. How long did it take to cover the distance ?

- a) 300 seconds
- b) 750 seconds
- c) 3000 seconds
- d) 1700 seconds
- e) 10 minutes

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Average speed

$$\overline{v} = \frac{d \text{ (distance)}}{t \text{ (elapsed time)}}$$

$$t = \frac{d}{\overline{v}} = \frac{1500 \text{ m}}{2.00 \text{ m/s}} = 750 \text{ s}$$

Average velocity is the displacement divided by the elapsed time.

Average velocity = 
$$\frac{\text{Displacement}}{\text{Elapsed time}}$$

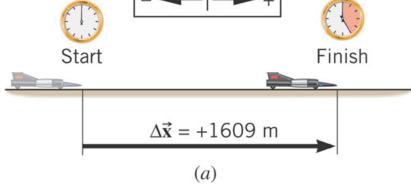
$$\frac{\vec{\mathbf{v}}}{\vec{\mathbf{v}}} = \frac{\vec{\mathbf{x}} - \vec{\mathbf{x}}_o}{t - t_o} = \frac{\Delta \vec{\mathbf{x}}}{\Delta t}$$

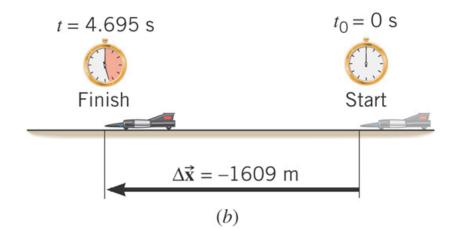
A vector divided by a scalar is another vector Note: division by a 2D or 3D vector is not allowed

#### **Example 2** The World's Fastest Jet-Engine Car

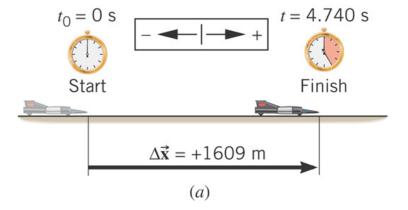
Andy Green in the car *ThrustSSC* set a world record of 341.1 m/s in 1997. To establish such a record, the driver makes two runs through the course, one in each direction, to nullify wind effects. From the data, determine the average

velocity for each run.  $t_0 = 0 \text{ s}$ 

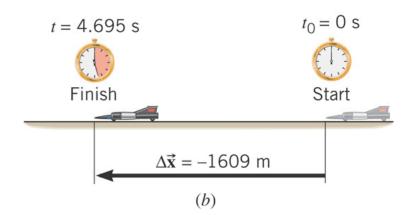




$$\vec{\mathbf{v}} = \frac{\Delta \vec{\mathbf{x}}}{\Delta t} = \frac{+1609 \text{ m}}{4.740 \text{ s}} = +339.5 \text{ m/s}$$



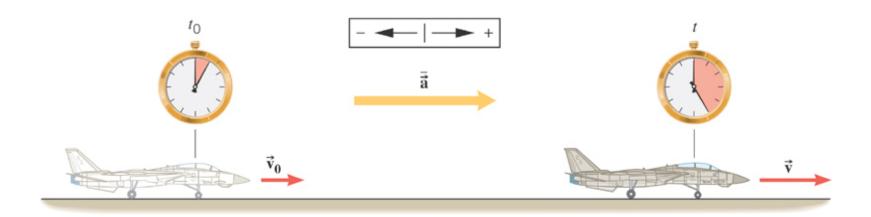
$$\overline{\mathbf{v}} = \frac{\Delta \overline{\mathbf{x}}}{\Delta t} = \frac{-1609 \text{ m}}{4.695 \text{ s}} = -342.7 \text{ m/s}$$

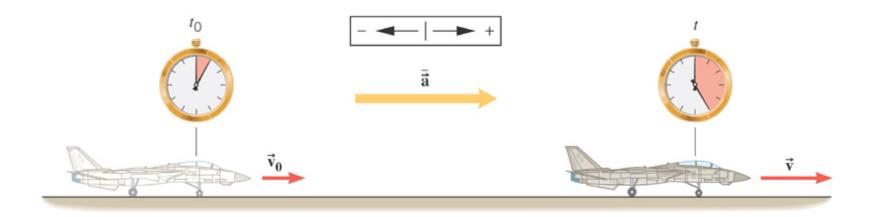


The *instantaneous velocity* indicates how fast the car moves and the direction of motion at each instant of time.

$$\vec{\mathbf{v}} = \lim_{\Delta t \to 0} \frac{\Delta \vec{\mathbf{x}}}{\Delta t}$$

The notion of *acceleration* emerges when a change in velocity is combined with the time during which the change occurs.

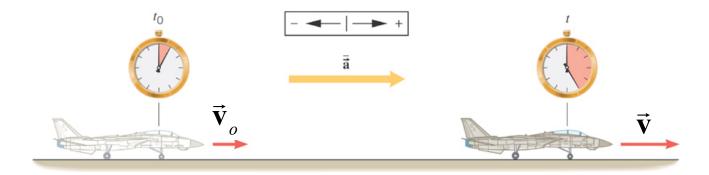




#### **DEFINITION OF AVERAGE ACCELERATION**

$$\overline{\vec{\mathbf{a}}} = \frac{\vec{\mathbf{v}} - \vec{\mathbf{v}}_o}{t - t_o} = \frac{\Delta \vec{\mathbf{v}}}{\Delta t}$$

 $\overline{\overline{\mathbf{a}}} = \frac{\overline{\mathbf{v}} - \overline{\mathbf{v}}_o}{t - t_o} = \frac{\Delta \overline{\mathbf{v}}}{\Delta t}$  (rate that velocity is changing in time)



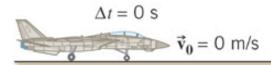
#### **Example 3** Acceleration and Increasing Velocity

Determine the average acceleration of the plane.

$$\vec{\mathbf{v}}_o = 0 \,\mathrm{m/s}$$
  $\vec{\mathbf{v}} = 260 \,\mathrm{km/h}$   $t_o = 0 \,\mathrm{s}$   $t = 29 \,\mathrm{s}$ 

$$\bar{\mathbf{a}} = \frac{\vec{\mathbf{v}} - \vec{\mathbf{v}}_o}{t - t_o} = \frac{260 \,\text{km/h} - 0 \,\text{km/h}}{29 \,\text{s} - 0 \,\text{s}} = +9.0 \,\frac{\text{km/h}}{\text{s}}$$





$$\Delta t = 1.0 \text{ s}$$

$$\vec{\mathbf{v}} = +9.0 \text{ km/h}$$

$$\Delta t = 2.0 \text{ s}$$
 $\vec{\mathbf{v}} = +18 \text{ km/h}$ 

Example 3 Acceleration and Decreasing

Velocity

$$\overline{\vec{a}} = \frac{\vec{v} - \vec{v}_o}{t - t_o} = \frac{13 \text{ m/s} - 28 \text{ m/s}}{12 \text{ s} - 9 \text{ s}} = -5.0 \text{ m/s}^2$$

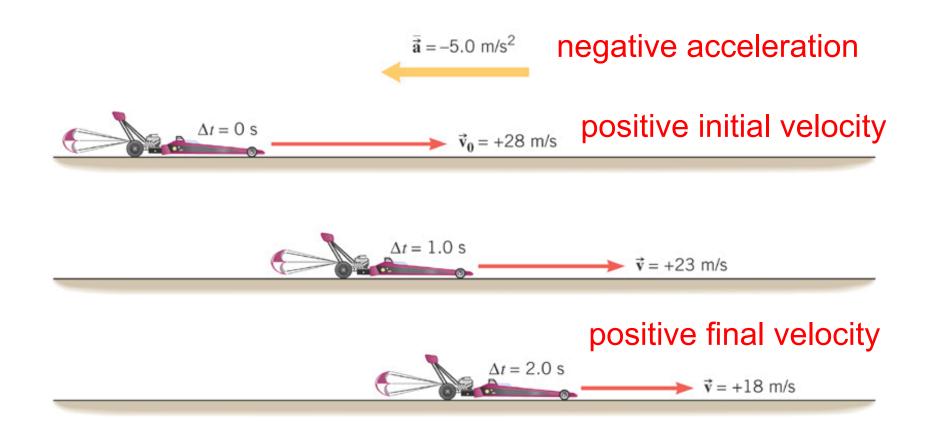






$$\overline{\vec{\mathbf{a}}} = -5.0 \text{ m/s}^2$$





Acceleration was  $\vec{a} = -5.0 \,\mathrm{m/s^2}$  throughout the motion

$$\vec{\mathbf{v}} = \frac{\vec{\mathbf{x}} - \vec{\mathbf{x}}_o}{t - t_o} \qquad \qquad \vec{\mathbf{a}} = \frac{\vec{\mathbf{v}} - \vec{\mathbf{v}}_o}{t - t_o}$$

## For motion along a straight line

it is customary to dispense with the use of boldface symbols overdrawn with arrows for the displacement, velocity, and acceleration vectors. We will, however, continue to convey the directions with a plus or minus sign.

$$v = \frac{x - x_o}{t - t_o} \qquad a = \frac{v - v_o}{t - t_o}$$

a, v and  $v_o$  are STILL vectors (values will have + or – for direction)

#### From now on unless stated otherwise

Let the object be at the origin when the clock starts.

$$x_o = 0 \quad \left(t_o = 0\right)$$

#### Simplifies things a great deal

$$\overline{v} = \frac{x - x_o}{t - t_o} \qquad \overline{v} = \frac{x}{t}$$



Note: average is (initial + final)/2

$$x = \overline{v}t = \frac{1}{2}(v_o + v)t$$

# A constant acceleration can be measured at any time

$$a = \frac{v - v_o}{t - t_o}$$

$$a = \frac{v - v_o}{t}$$

$$at = v - v_o$$

$$v = v_o + at$$

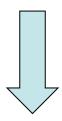
Five kinematic variables:

- 1. displacement, x
- 2. acceleration (constant), a
- 3. final velocity (at time t), v
- 4. initial velocity,  $v_0$
- 5. elapsed time, t

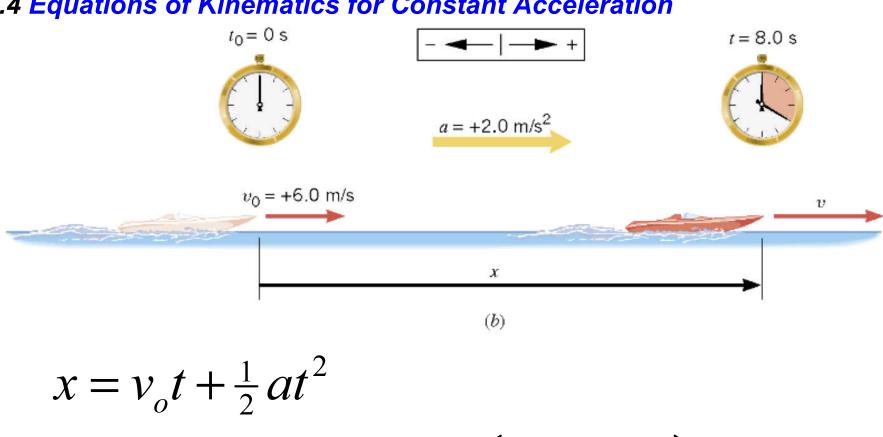
$$v = v_o + at$$

$$\downarrow$$

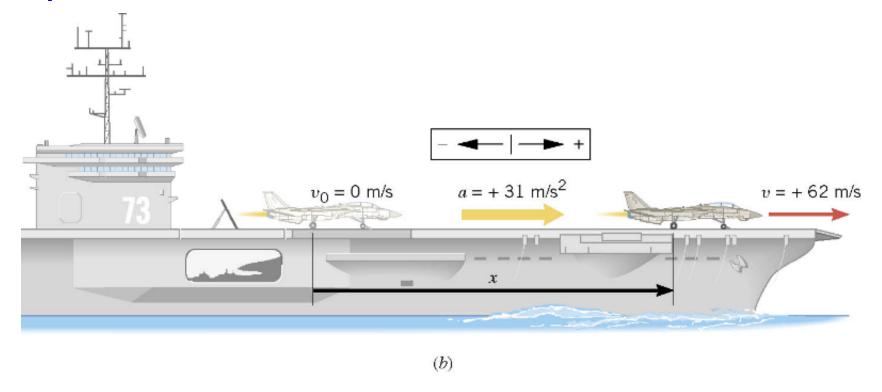
$$x = \frac{1}{2} (v_o + v)t = \frac{1}{2} (v_o + v_o + at)t$$



$$x = v_o t + \frac{1}{2}at^2$$



$$x = v_o t + \frac{1}{2} at$$
=  $(6.0 \text{ m/s})(8.0 \text{ s}) + \frac{1}{2} (2.0 \text{ m/s}^2)(8.0 \text{ s})^2$ 
=  $+110 \text{ m}$ 



## **Example 6** Catapulting a Jet

Find its displacement.

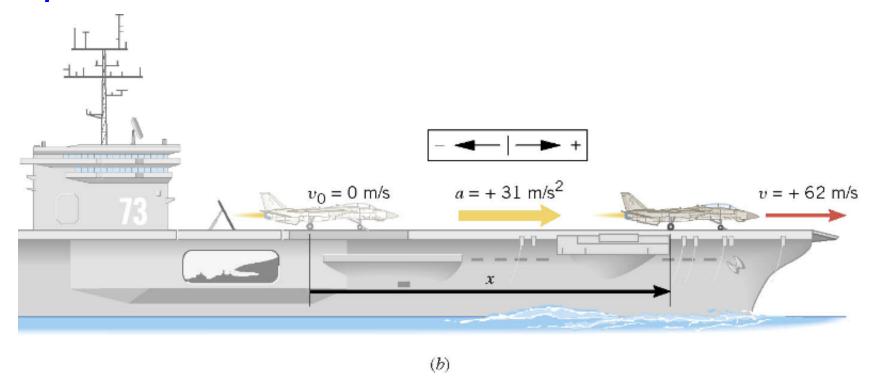
$$v_o = 0 \text{ m/s}$$
  $a = +31 \text{ m/s}^2$   
 $x = ??$   $v = +62 \text{ m/s}$ 

$$a = \frac{v - v_o}{t}$$

$$\Rightarrow t = \frac{v - v_o}{a}$$

$$x = \frac{1}{2} (v_o + v) t = \frac{1}{2} (v_o + v) \frac{(v - v_o)}{a}$$

$$x = \frac{v^2 - v_o^2}{2a}$$



$$x = \frac{v^2 - v_o^2}{2a} = \frac{(62 \text{ m/s})^2 - (0 \text{ m/s})^2}{2(31 \text{ m/s}^2)} = +62 \text{ m}$$

## **Equations of Kinematics for Constant Acceleration**

$$v = v_o + at$$

$$v = v_o + at$$
$$x = \frac{1}{2} (v_o + v)t$$

$$v^2 = v_o^2 + 2ax$$

$$v^2 = v_o^2 + 2ax$$
$$x = v_o t + \frac{1}{2}at^2$$

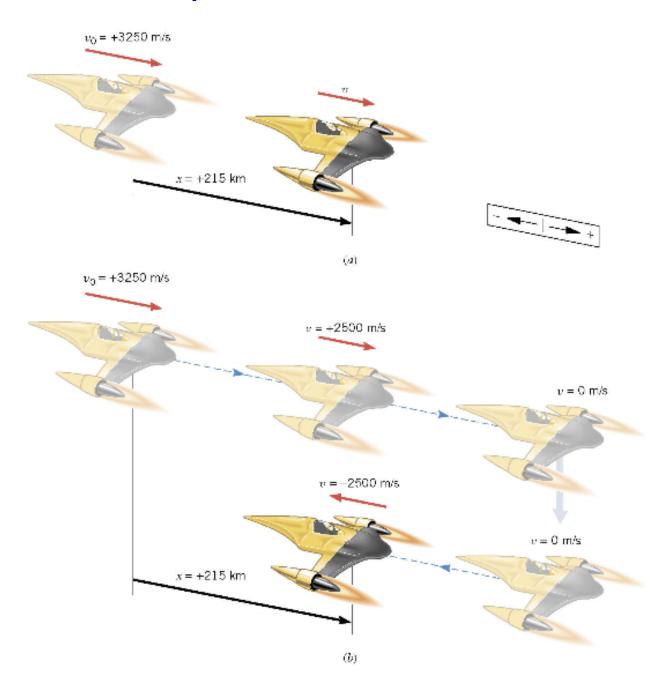
## Reasoning Strategy

- 1. Make a drawing.
- 2. Decide which directions are to be called positive (+) and negative (-).
- 3. Write down the values that are given for any of the five kinematic variables.
- 4. Verify that the information contains values for at least three of the five kinematic variables. Select the appropriate equation.
- 5. When the motion is divided into segments, remember that the final velocity of one segment is the initial velocity for the next.
- 6. Keep in mind that there may be two possible answers to a kinematics problem.

## **Example 8** An Accelerating Spacecraft

A spacecraft is traveling with a velocity of +3250 m/s. Suddenly the retrorockets are fired, and the spacecraft begins to slow down with an acceleration whose magnitude is 10.0 m/s². What is the velocity of the spacecraft when the displacement of the craft is +215 km, relative to the point where the retrorockets began firing?

X	а	V	V <sub>o</sub>	t
+215000 m	-10.0 m/s <sup>2</sup>	?	+3250 m/s	



X	а	V	V <sub>o</sub>	t
+215000 m	-10.0 m/s <sup>2</sup>	?	+3250 m/s	

$$v^2 = v_o^2 + 2ax$$
  $\Rightarrow v = \sqrt{v_o^2 + 2ax}$ 

$$v = \pm \sqrt{(3250 \,\text{m/s})^2 + 2(10.0 \,\text{m/s}^2)(215000 \,\text{m})}$$
  
=  $\pm 2500 \,\text{m/s}$ 

#### 2.6 Freely Falling Bodies

In the absence of air resistance, it is found that all bodies at the same location above the Earth fall vertically with the same acceleration. If the distance of the fall is small compared to the radius of the Earth, then the acceleration remains essentially constant throughout the descent.

This idealized motion is called *free-fall* and the acceleration of a freely falling body is called the *acceleration due to gravity*.

$$g = 9.80 \,\mathrm{m/s^2}$$
 or  $32.2 \,\mathrm{ft/s^2}$ 

## 2.6 Freely Falling Bodies



Air-filled tube (a)



Evacuated tube (b)

acceleration due to gravity.

$$g = 9.80 \,\mathrm{m/s^2}$$