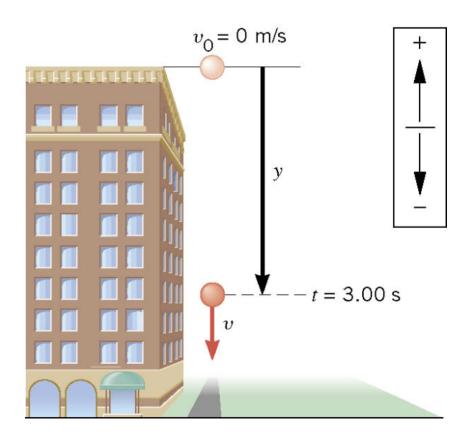
# Chapter 2

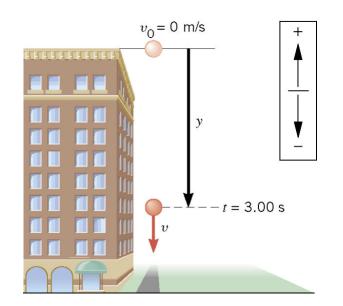
## Kinematics in One Dimension

continued

## **Example 10** A Falling Stone

A stone is dropped from the top of a tall building. After 3.00s of free fall, what is the displacement *y* of the stone?





У	а	V	V <sub>o</sub>	t
?	-9.80 m/s <sup>2</sup>		0 m/s	3.00 s

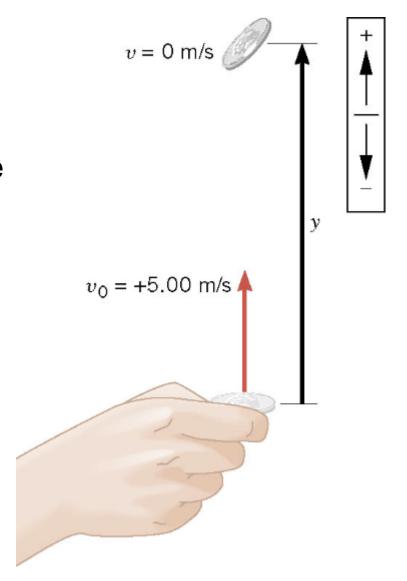
$$y = v_o t + \frac{1}{2} a t^2$$

$$= (0 \text{ m/s})(3.00 \text{ s}) + \frac{1}{2} (-9.80 \text{ m/s}^2)(3.00 \text{ s})^2$$

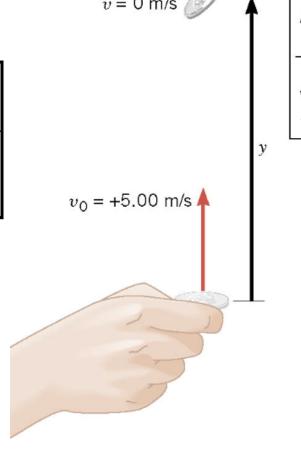
$$= -44.1 \text{ m}$$

## **Example 12** How High Does it Go?

The referee tosses the coin up with an initial speed of 5.00m/s. In the absence if air resistance, how high does the coin go above its point of release?



У	а	V	V <sub>o</sub>	t
?	-9.80 m/s <sup>2</sup>	0 m/s	+5.00 m/s	



$$v^2 = v_o^2 + 2ay \qquad \Longrightarrow \qquad y = \frac{v^2 - v_o^2}{2a}$$

$$y = \frac{v^2 - v_o^2}{2a} = \frac{(0 \text{ m/s})^2 - (5.00 \text{ m/s})^2}{2(-9.80 \text{ m/s}^2)} = 1.28 \text{ m}$$

## Conceptual Example 14 Acceleration Versus Velocity

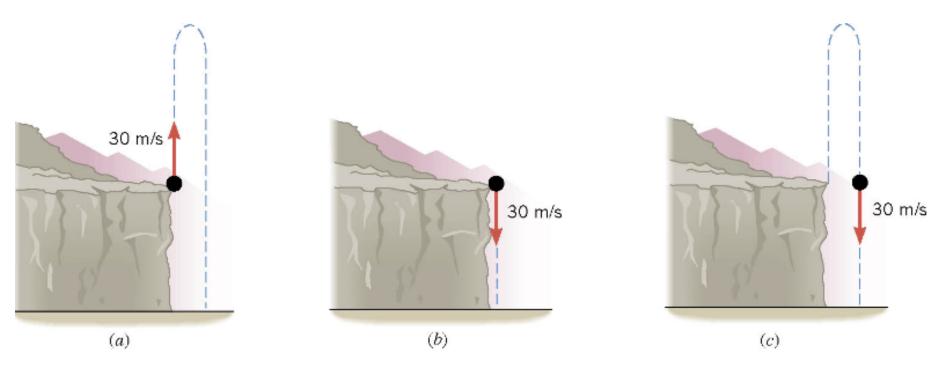
There are three parts to the motion of the coin.

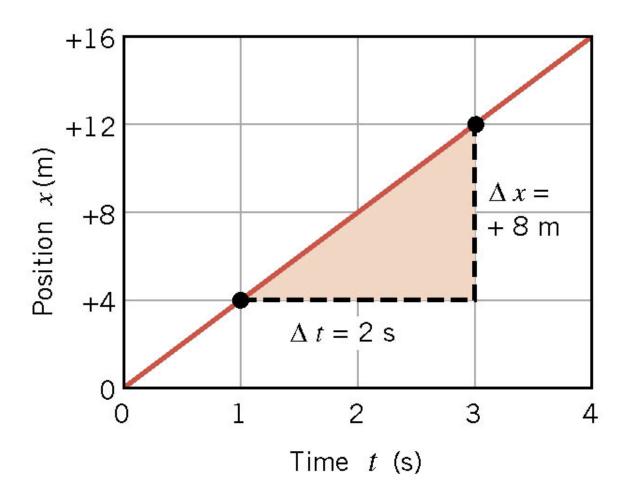
- 1) On the way up, the coin has an upward-pointing velocity with a decreasing magnitude.
- 2) At that time the coin reaches the top of its path, the coin has an instantaneously zero velocity.
- 3) On the way down, the coin has a downward-pointing velocity with an increasing magnitude.

In the absence of air resistance, does the acceleration vector of the coin, like the velocity, change from one part to another?

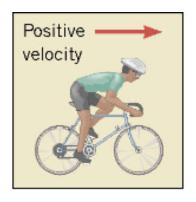
## Conceptual Example 15 Taking Advantage of Symmetry

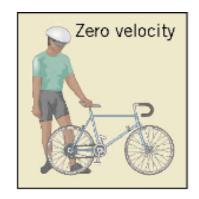
Does the pellet in part b strike the ground beneath the cliff with a smaller, greater, or the same speed as the pellet in part a?

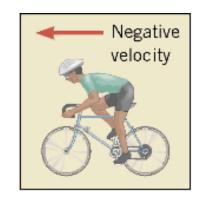


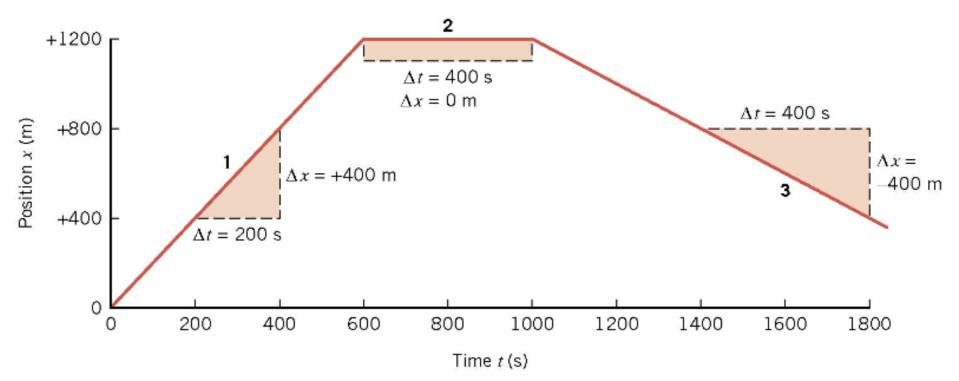


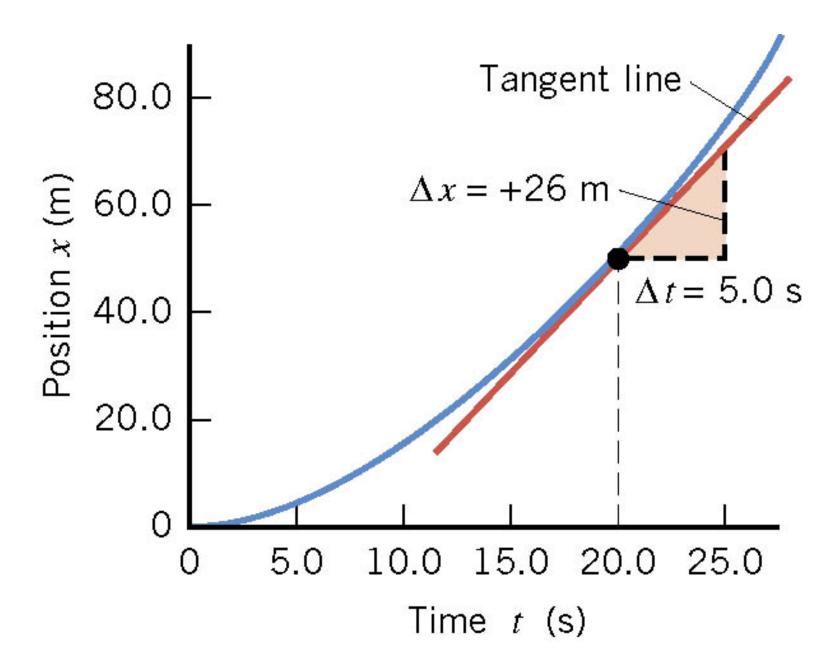
Slope = 
$$\frac{\Delta x}{\Delta t}$$
 =  $\frac{+8 \text{ m}}{2 \text{ s}}$  =  $+4 \text{ m/s}$ 

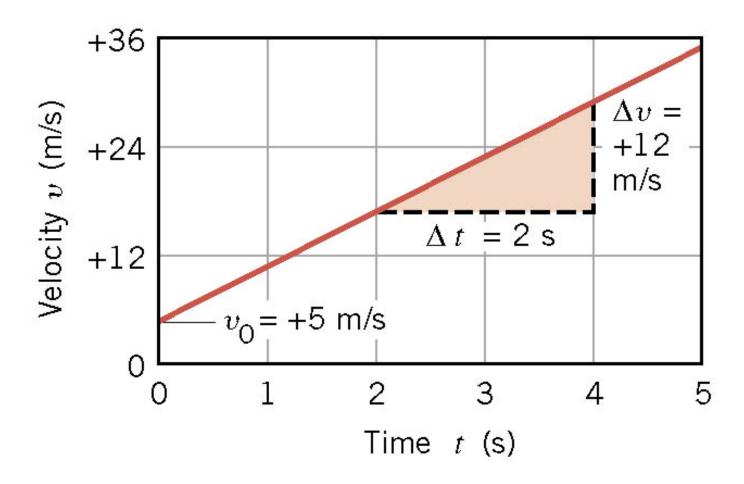












Slope = 
$$\frac{\Delta v}{\Delta t}$$
 =  $\frac{+12 \text{ m/s}}{2 \text{ s}}$  =  $+6 \text{ m/s}^2$ 

# Chapter 3

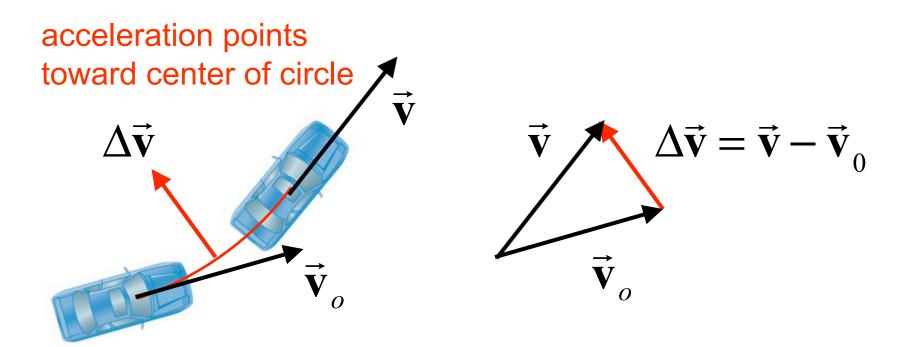
## Kinematics in Two Dimensions

### 3.1 Displacement, Velocity, and Acceleration

#### DEFINITION OF AVERAGE ACCELERATION

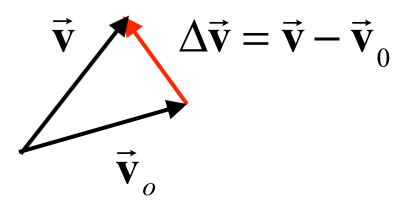
$$\overline{\mathbf{a}} = \frac{\overrightarrow{\mathbf{v}} - \overrightarrow{\mathbf{v}}_o}{t - t_o} = \frac{\Delta \overrightarrow{\mathbf{v}}}{\Delta t}$$

Consider a velocity that keeps the <u>same magnitude (speed)</u> but changes its direction, e.g., car going around a curve.



How to see this:

$$\Delta \vec{\mathbf{v}} = \vec{\mathbf{v}} - \vec{\mathbf{v}}_0$$



$$= \vec{\mathbf{v}} + \left(-\vec{\mathbf{v}}_0\right)$$

acceleration points toward center of circle  $\Delta \vec{\mathbf{v}} = \vec{\mathbf{v}} - \vec{\mathbf{v}}_0$ 

$$\Delta \vec{\mathbf{v}} = \vec{\mathbf{v}} - \vec{\mathbf{v}}_0$$

Need in Chapter 5 when uniform circular motion is discussed.

**Equations of 1D Kinematics** 

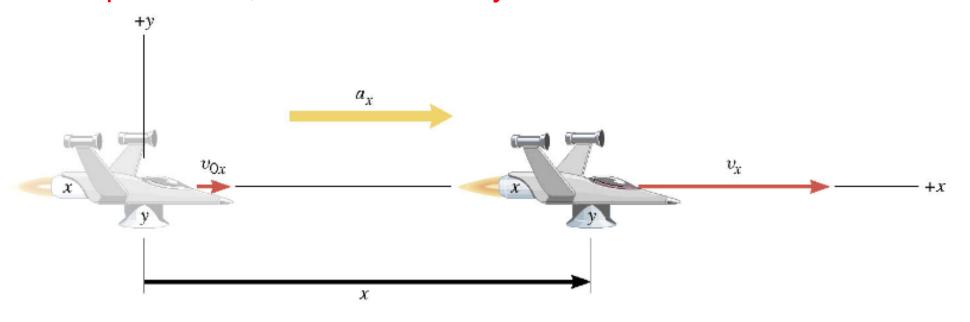
$$v = v_0 + at$$

$$x = \frac{1}{2} \left( v_0 + v \right) t$$

$$v^2 = v_0^2 + 2ax$$

$$x = v_0 t + \frac{1}{2} a t^2$$

Except for time, motion in x and y directions are INDEPENDENT.

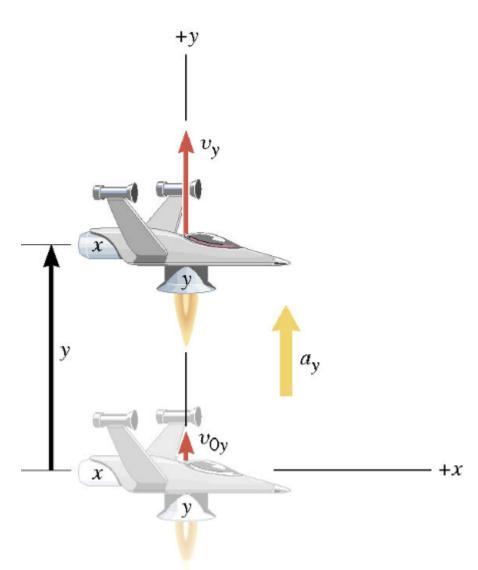


## Motion in x direction.

$$v_x = v_{0x} + a_x t$$
  $x = \frac{1}{2} (v_{0x} + v_x) t$ 

$$x = v_{0x}t + \frac{1}{2}a_xt^2$$
  $v_x^2 = v_{0x}^2 + 2a_xx$ 

Except for time, motion in x and y directions are INDEPENDENT.



## Motion in y direction.

$$v_{y} = v_{0y} + a_{y}t$$

$$y = v_{0y}t + \frac{1}{2}a_{y}t^{2}$$

$$y = \frac{1}{2} \left( v_{0y} + v_y \right) t$$

$$v_y^2 = v_{0y}^2 + 2a_y y$$

## Reasoning Strategy

- 1. Make a drawing.
- 2. Decide which directions are to be called positive (+) and negative (-).
- 3. Write down the values that are given for any of the five kinematic variables associated with each direction.

## **Example 1** A Moving Spacecraft

In the x direction, the spacecraft has an initial velocity component of +22 m/s and an acceleration of +24 m/s<sup>2</sup>. In the y direction, the analogous quantities are +14 m/s and an acceleration of +12 m/s<sup>2</sup>. Find (a) x and  $v_x$ , (b) y and  $v_y$ , and (c) the final velocity of the spacecraft at time 7.0 s.

Want final values:  $v_{0x} = +22 \text{ m/s}$   $v_{0y} = +14 \text{ m/s}$   $v_{0y} = +12 \text{ m/s}$ 

## Reasoning Strategy

- 1. Make a drawing.
- 2. Decide which directions are to be called positive (+) and negative (-).
- 3. Write down the values that are given for any of the five kinematic variables associated with each direction.
- 4. Verify that the information contains values for at least three of the kinematic variables. Do this for *x* and *y*. Select the appropriate equation.
- 5. When the motion is divided into segments, remember that the final velocity of one segment is the initial velocity for the next.
- 6. Keep in mind that there may be two possible answers to a kinematics problem.

## **Example 1** A Moving Spacecraft:

#### x direction motion

X	$a_{x}$	V <sub>X</sub>	V <sub>ox</sub>	t
?	+24.0 m/s <sup>2</sup>	?	+22 m/s	7.0 s

$$x = v_{ox}t + \frac{1}{2}a_xt^2$$

$$= (22 \text{ m/s})(7.0 \text{ s}) + \frac{1}{2}(24 \text{ m/s}^2)(7.0 \text{ s})^2 = +740 \text{ m}$$

$$v_x = v_{ox} + a_x t$$
  
=  $(22 \text{ m/s}) + (24 \text{ m/s}^2)(7.0 \text{ s}) = +190 \text{ m/s}$ 

## **Example 1** A Moving Spacecraft:

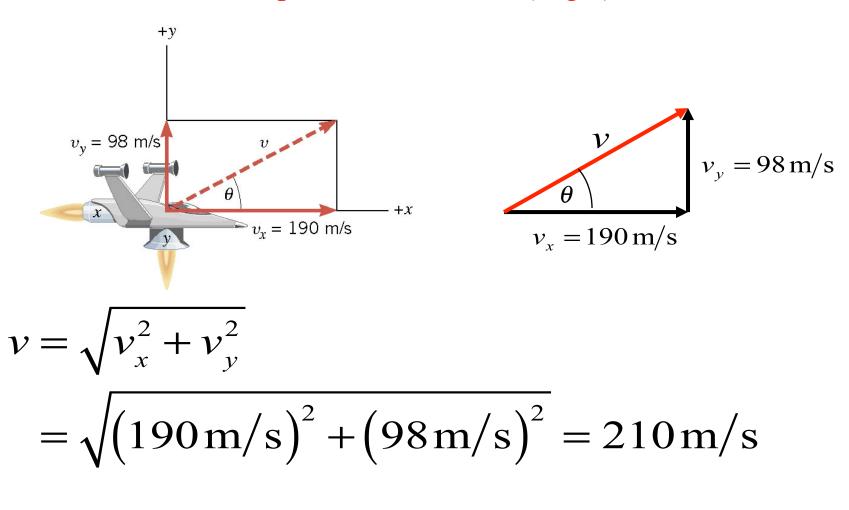
## y direction motion

У	$a_y$	$V_y$	V <sub>oy</sub>	t
?	+12.0 m/s <sup>2</sup>	?	+14 m/s	7.0 s

$$y = v_{oy}t + \frac{1}{2}a_yt^2$$
  
=  $(14 \text{ m/s})(7.0 \text{ s}) + \frac{1}{2}(12 \text{ m/s}^2)(7.0 \text{ s})^2 = +390 \text{ m}$ 

$$v_y = v_{oy} + a_y t$$
  
=  $(14 \text{ m/s}) + (12 \text{ m/s}^2)(7.0 \text{ s}) = +98 \text{ m/s}$ 

Can also find final speed and direction (angle) at t = 7s.



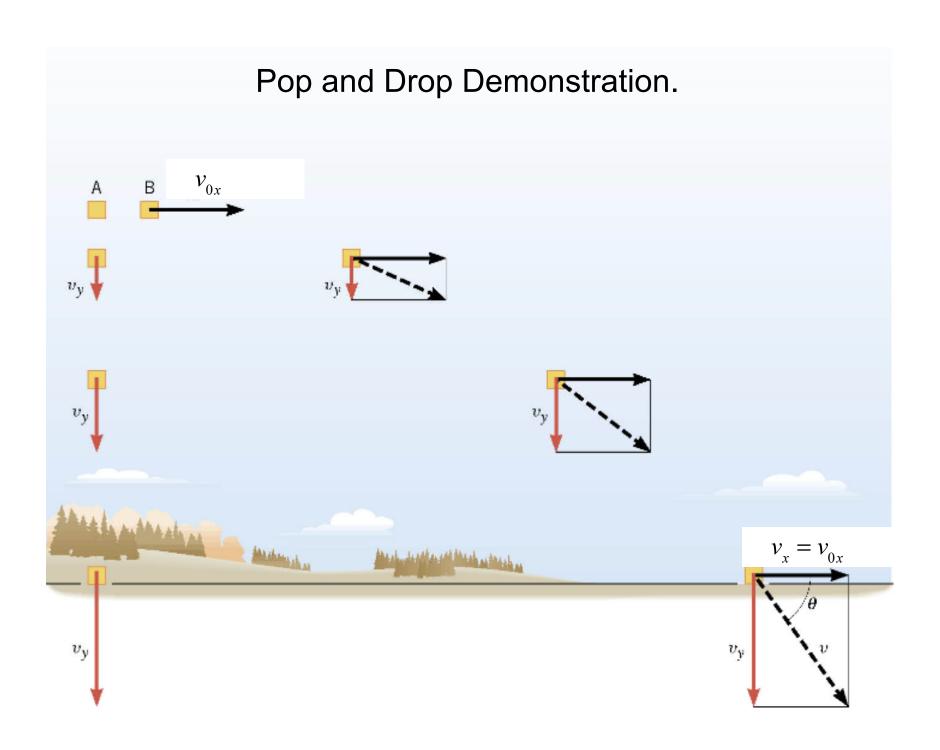
$$\theta = \tan^{-1}(98/190) = 27^{\circ}$$

Under the influence of gravity alone, an object near the surface of the Earth will accelerate downwards at 9.80m/s<sup>2</sup>.

$$a_y = -9.80 \,\mathrm{m/s^2}$$
  $a_x = 0$ 

Great simplification for projectiles!

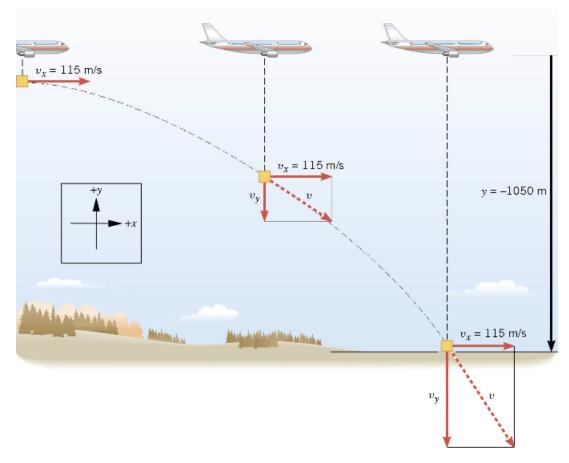
$$v_x = v_{ox} = \text{constant}$$



## **Example 3** A Falling Care Package

The airplane is moving horizontally with a constant velocity of +115 m/s at an altitude of 1050m. Determine the time required for the care package to hit the ground.

# Time to hit the ground depends ONLY on vertical motion



$$v_{oy} = 0$$

$$a_y = -9.8 \text{ m/s}^2$$

$$y = 1050 \text{ m}$$

У	$a_y$	$V_y$	<b>V</b> <sub>oy</sub>	t
-1050 m	-9.80 m/s <sup>2</sup>		0 m/s	

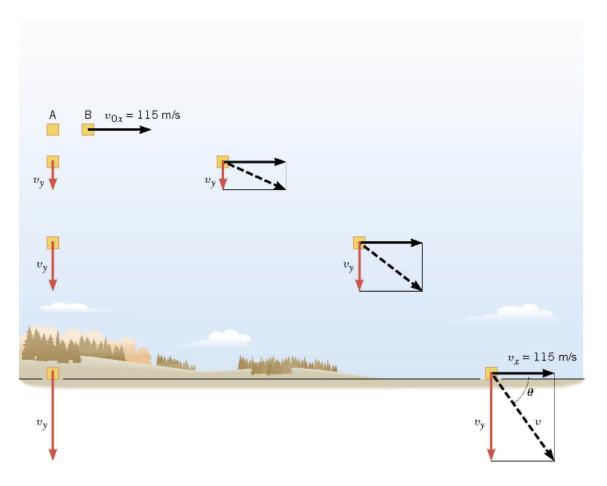
$$y = v_{oy}t + \frac{1}{2}a_yt^2$$
  $\implies$   $y = \frac{1}{2}a_yt^2$ 

$$t = \sqrt{\frac{2y}{a_y}} = \sqrt{\frac{2(-1050 \text{ m})}{-9.80 \text{ m/s}^2}} = 14.6 \text{ s}$$

## Example 4 The Velocity of the Care Package

What are the magnitude and direction of the final velocity of

the care package?



$$v_{0y} = 0$$
 $a_y = -9.8 \text{ m/s}^2$ 
 $y = 1050 \text{ m}$ 
 $t = 14.6 \text{ s}$ 
 $v_{0x} = +115 \text{ m/s}$ 
 $a_x = 0$ 
 $v_x = v_{0x} = +115 \text{ m/s}$ 

x-component does not change

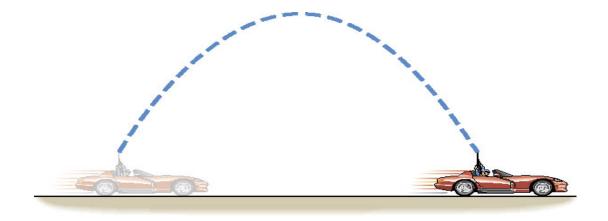
У	$a_y$	$V_y$	V <sub>oy</sub>	t
-1050 m	-9.80 m/s <sup>2</sup>	?	0 m/s	14.6 s

$$v_y = v_{oy} + a_y t = 0 + (-9.80 \text{ m/s}^2)(14.6 \text{ s})$$
  
= -143 m/s y-component of final velocity.

$$v_x = v_{ox} = +115 \text{ m/s}$$
  $v = \sqrt{v_x^2 + v_y^2} = 184 \text{ m/s}$   $\theta = \tan^{-1} \left(\frac{v_y}{v_x}\right) = \tan^{-1} \left(\frac{-143}{+115}\right) = -51^\circ$ 

## Conceptual Example 5 I Shot a Bullet into the Air...

Suppose you are driving a convertible with the top down. The car is moving to the right at constant velocity. You point a rifle straight up into the air and fire it. In the absence of air resistance, where would the bullet land – behind you, ahead of you, or in the barrel of the rifle?

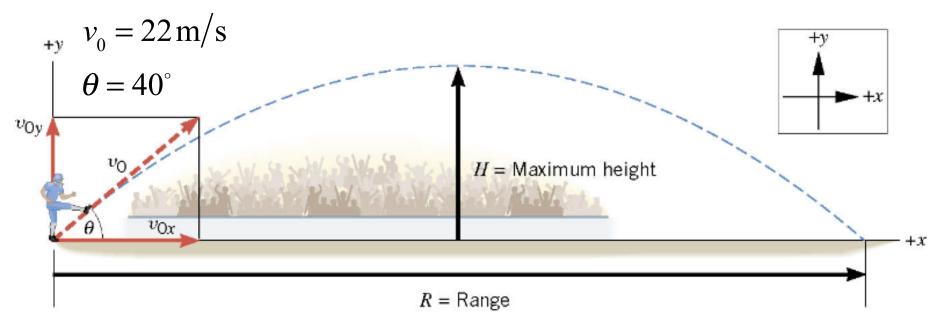


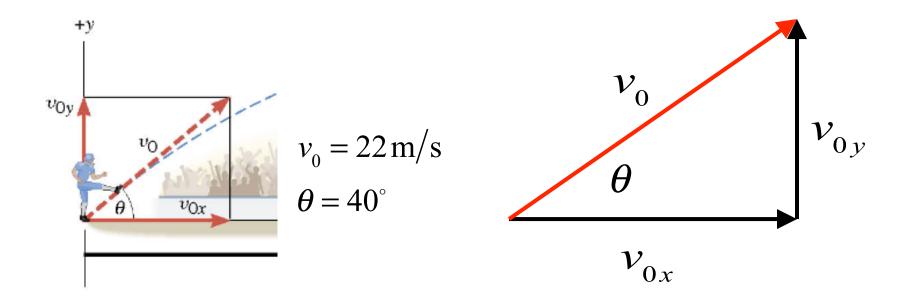
**Ballistic Cart Demonstration** 

## **Example 6** The Height of a Kickoff

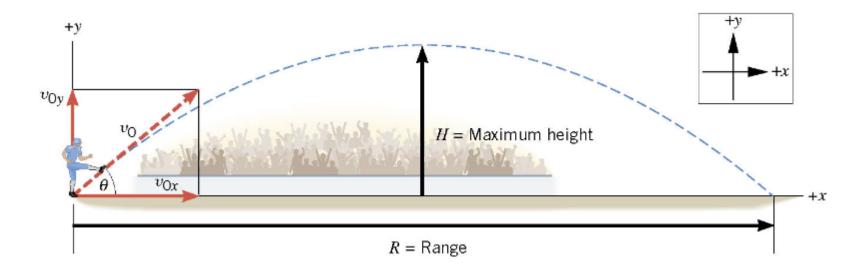
A placekicker kicks a football at and angle of 40.0 degrees and the initial speed of the ball is 22 m/s. Ignoring air resistance, determine the maximum height that the ball attains.

maximum height and "hang time" depend only on the y-component of initial velocity





$$v_{0y} = v_0 \sin \theta = (22 \text{ m/s}) \sin 40^\circ = 14 \text{ m/s}$$
  
 $v_{0x} = v_0 \cos \theta = (22 \text{ m/s}) \cos 40^\circ = 17 \text{ m/s}$ 

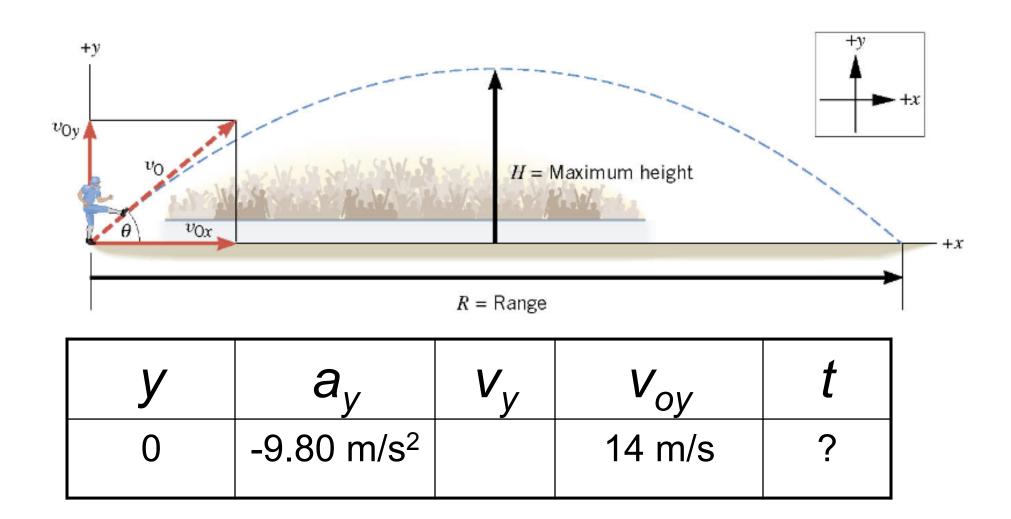


У	$a_y$	$V_y$	V <sub>oy</sub>	t
?	-9.80 m/s <sup>2</sup>	0	14 m/s	

$$v_y^2 = v_{0y}^2 + 2a_y y \qquad y = \frac{v_y^2 - v_{0y}^2}{2a_y}$$
$$y = \frac{0 - (14 \text{ m/s})^2}{2(-9.8 \text{ m/s}^2)} = +10 \text{ m}$$

## **Example 7** The Time of Flight of a Kickoff

What is the time of flight between kickoff and landing?



У	$a_y$	$V_y$	V <sub>oy</sub>	t
0	-9.80 m/s <sup>2</sup>		14 m/s	?

$$y = v_{0y}t + \frac{1}{2}a_{y}t^{2}$$

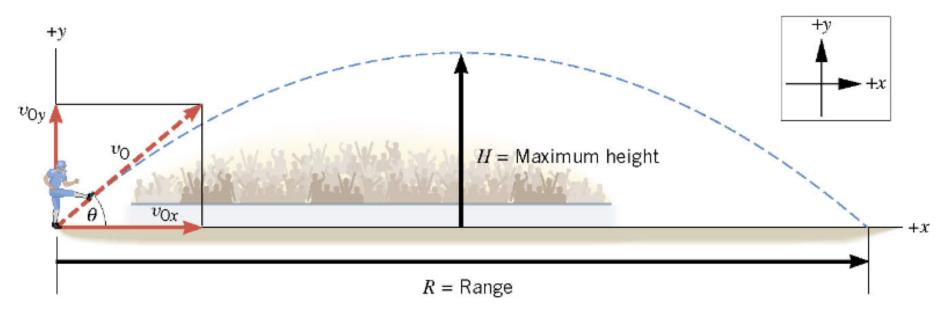
$$0 = (14 \,\mathrm{m/s})t + \frac{1}{2}(-9.80 \,\mathrm{m/s^2})t^2$$

$$0 = 2(14 \,\mathrm{m/s}) + (-9.80 \,\mathrm{m/s^2})t$$

$$t = 2.9 \, \mathrm{s}$$

**Example 8** The Range of a Kickoff Calculate the range R of the projectile.

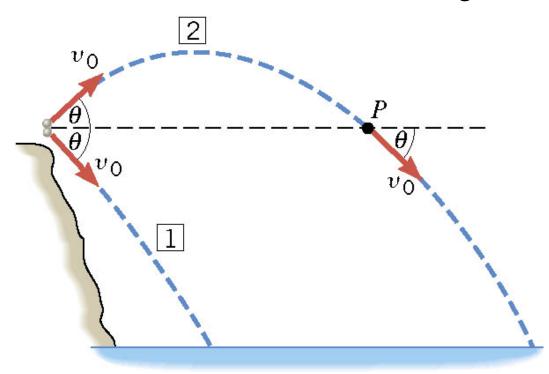
Range depends on the hang time and x-component of initial velocity



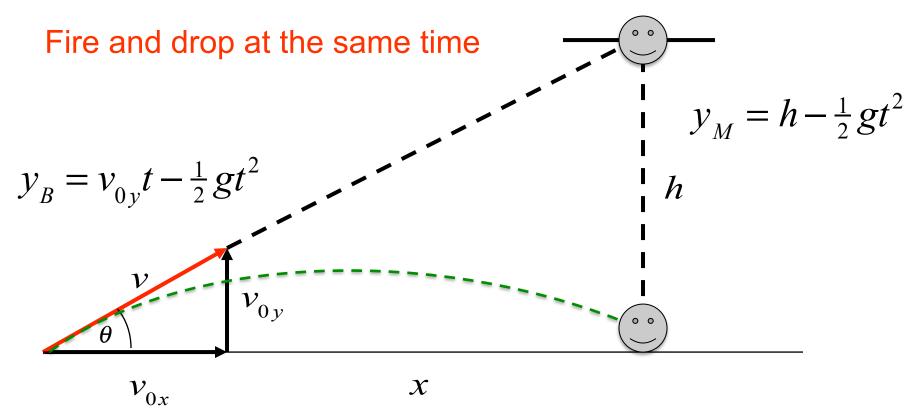
$$x = v_{ox}t + \frac{1}{2}a_xt^2 = v_{ox}t$$
  
=  $(17 \text{ m/s})(2.9 \text{ s}) = +49 \text{ m}$ 

## Conceptual Example 10 Two Ways to Throw a Stone

From the top of a cliff, a person throws two stones. The stones have identical initial speeds, but stone 1 is thrown downward at some angle above the horizontal and stone 2 is thrown at the same angle below the horizontal. Neglecting air resistance, which stone, if either, strikes the water with greater velocity?



## **Shoot the Monkey Demonstration**



Hit height: 
$$y_B = y_M \implies v_{0y}t = h$$

Hit time: 
$$t = \frac{x}{v_{0x}}$$
 
$$\frac{v_{0y}}{v_{0x}} x = h$$

## Shoot at the Monkey!

$$\frac{v_{0y}}{v_{0x}} = \frac{h}{x} = \tan \theta$$