Chapter 11



11.2 Pressure

Pressure is the amount of force acting on an area:

$$P = \frac{F}{A}$$

SI unit:
$$N/m^2$$

(1 Pa = 1 N/m²)

Example 2 The Force on a Swimmer

Suppose the pressure acting on the back of a swimmer's hand is $1.2x10^5$ Pa. The surface area of the back of the hand is $8.4x10^{-3}m^2$.

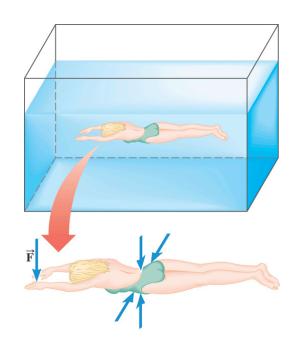
(a) Determine the magnitude of the force that acts on it.

(b) Discuss the direction of the force.

$$F = PA = (1.2 \times 10^5 \text{ N/m}^2)(8.4 \times 10^{-3} \text{ m}^2)$$
$$= 1.0 \times 10^3 \text{ N}$$

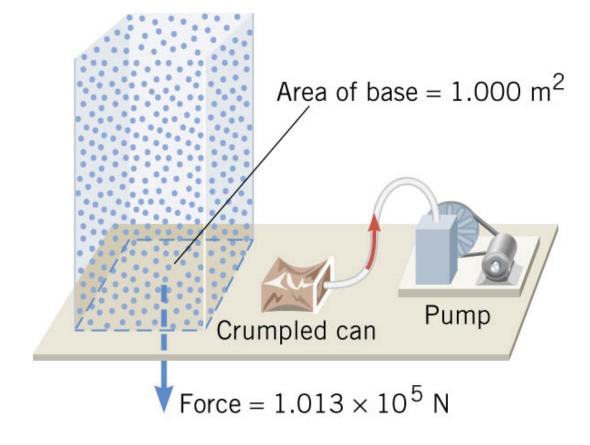
Since the water pushes perpendicularly against the back of the hand, the force is directed downward in the drawing.

Pressure on the underside of the hand is somewhat greater (greater depth). So force upward is somewhat greater - bouyancy

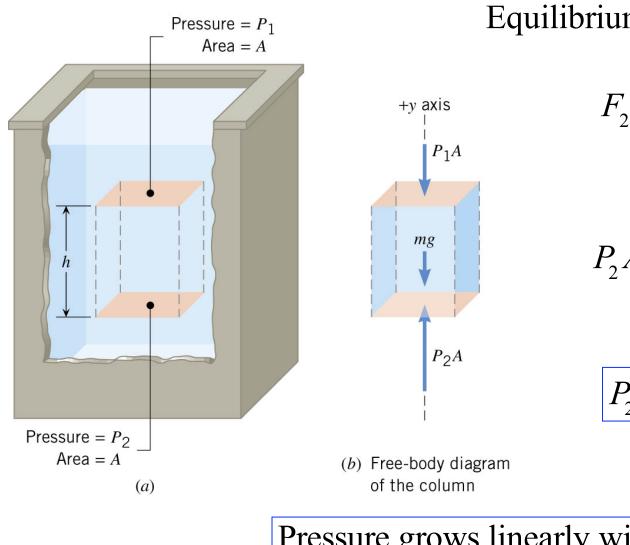


11.2 Pressure

Atmospheric Pressure at Sea Level: 1.013x10⁵ Pa = 1 atmosphere



11.3 Pressure and Depth in a Static Fluid



Fluid density is ρ Equilibrium of a volume of fluid

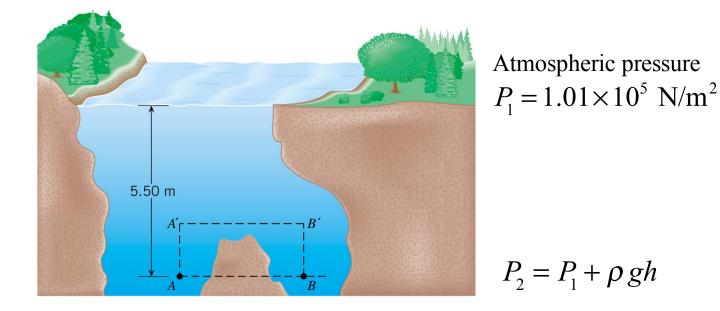
 $F_{\gamma} = F_1 + mg$ with F = PA, $m = \rho V$ $P_2 A = P_1 A + \rho V g$ with V = Ah $P_2 = P_1 + \rho gh$

Pressure grows linearly with depth (h)

11.3 Pressure and Depth in a Static Fluid

Example 4 The Swimming Hole

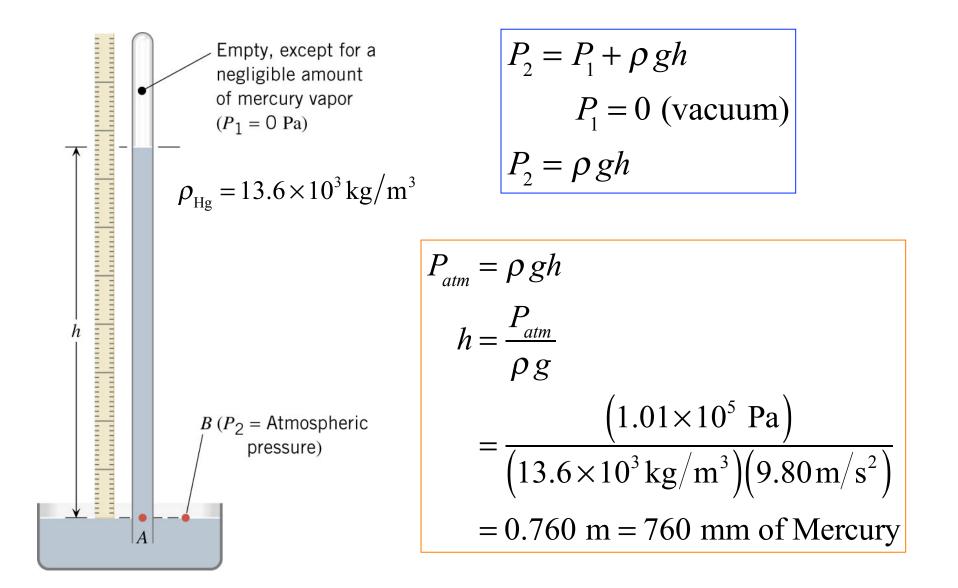
Points A and B are located a distance of 5.50 m beneath the surface of the water. Find the pressure at each of these two locations.



$$P_{2} = P_{1} + \rho gh$$

= $(1.01 \times 10^{5} \text{ Pa}) + (1.00 \times 10^{3} \text{ kg/m}^{3})(9.80 \text{ m/s}^{2})(5.50 \text{ m})$
= $1.55 \times 10^{5} \text{ Pa}$

11.4 Pressure Gauges



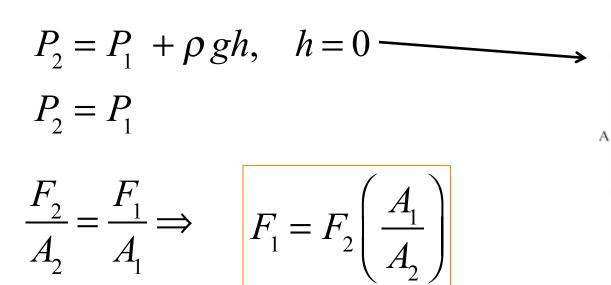
11.5 Pascal's Principle

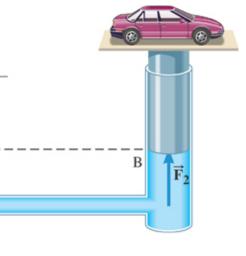
PASCAL'S PRINCIPLE

Any change in the pressure applied to a completely enclosed fluid is transmitted undiminished to all parts of the fluid and enclosing walls.

$$P_2 = \frac{F_2}{A_2}; \quad P_1 = \frac{F_1}{A_1}$$

(*a*)





(b)

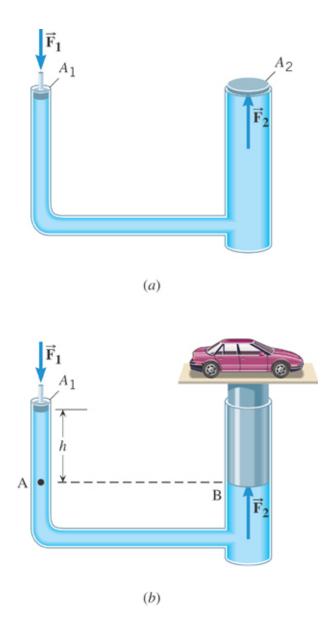
11.5 Pascal's Principle

Example 7 A Car Lift

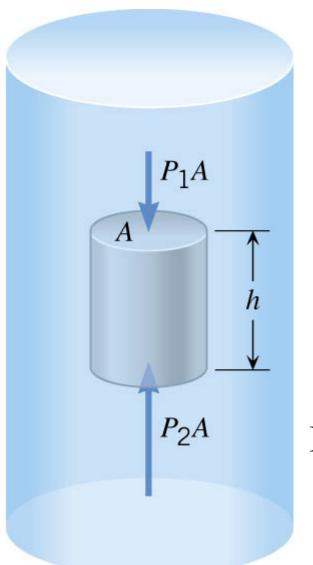
The input piston has a radius of 0.0120 m and the output plunger has a radius of 0.150 m.

The combined weight of the car and the plunger is 20500 N. Suppose that the input piston has a negligible weight and the bottom surfaces of the piston and plunger are at the same level. What is the required input force?

$$F_{1} = F_{2} \left(\frac{A_{1}}{A_{2}}\right)$$
$$= (20500 \text{ N}) \frac{\pi (0.0120 \text{ m})^{2}}{\pi (0.150 \text{ m})^{2}} = 131 \text{ N}$$



11.6 Archimedes' Principle



Buoyant Force

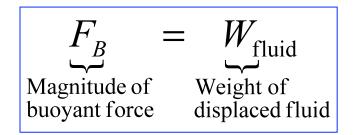
$$F_{B} = P_{2}A - P_{1}A = (P_{2} - P_{1})A$$

= ρghA $P_{2} = P_{1} + \rho gh$
= $\rho V g$ $V = hA$
mass of
displaced
fluid

Buoyant force = Weight of displaced fluid

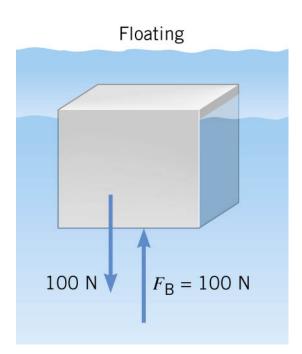
ARCHIMEDES' PRINCIPLE

Any fluid applies a buoyant force to an object that is partially or completely immersed in it; the magnitude of the buoyant force equals the weight of the fluid that the object displaces:



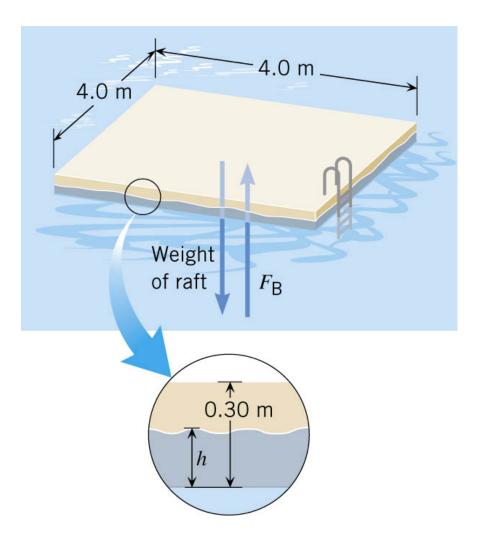
CORROLARY

If an object is floating then the magnitude of the buoyant force is equal to the magnitude of its weight.



Example 9 A Swimming Raft

The raft is made of solid square pinewood. Determine whether the raft floats in water and if so, how much of the raft is beneath the surface.



11.6 Archimedes' Principle

$$W_{raft} = m_{raft}g = \rho_{pine}V_{raft}g$$

= $(550 \text{ kg/m}^3)(4.8 \text{m}^3)(9.80 \text{ m/s}^2)$
= 26000 N

If
$$W_{\rm raft} < F_{\rm B}^{\rm max}$$
, raft floats

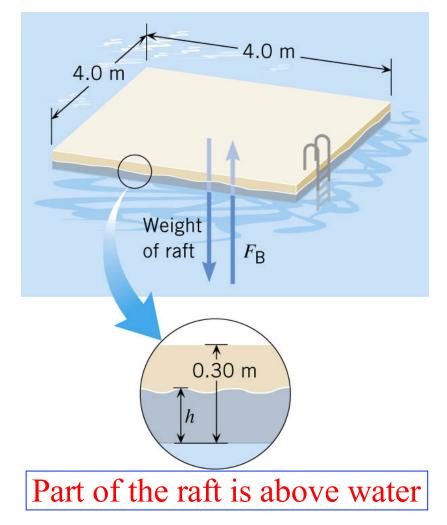
$$F_{\rm B}^{\rm max} = W_{\rm fluid}$$
 (full volume)

$$F_{B}^{\max} = \rho V g = \rho_{water} V_{water} g$$

= (1000 kg/m³)(4.8m³)(9.80 m/s²)
= 47000 N

$$W_{raft} < F_B^{\max}$$
 Raft floats

$\frac{\text{Raft properties}}{V_{raft}} = (4.0)(4.0)(0.30)\text{m}^3 = 4.8 \text{ m}^3$ $\rho_{pine} = 550 \text{ kg/m}^3$



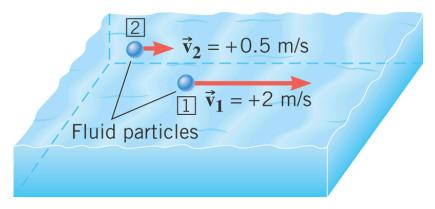
11.6 Archimedes' Principle

How much of raft below water? 4.0 m_ 4.0 m Floating object $F_{\rm B} = W_{\rm raft}$ Weight of raft F_{B} $F_{B} = \rho_{\text{water}} g V_{\text{water}}$ $= \rho_{\text{water}} g(A_{\text{water}} h)$ ↑ 0.30 m $\frac{W_{\rm raft}}{\rho_{\rm water}gA_{\rm water}}$ h $W_{raft} = 26000 \text{ N}$ h = -26000N $(1000 \text{ kg/m}^3)(9.80 \text{ m/s}^2)(16.0 \text{ m}^2)$ = 0.17 m

11.7 Fluids in Motion

In *steady flow* the velocity of the fluid particles at any point is constant as time passes.

Unsteady flow exists whenever the velocity of the fluid particles at a point changes as time passes.



Turbulent flow is an extreme kind of unsteady flow in which the velocity of the fluid particles at a point change erratically in both magnitude and direction.

Fluid flow can be *compressible* or *incompressible*. Most liquids are nearly incompressible.

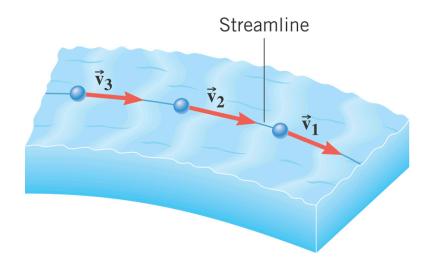
Fluid flow can be *viscous* or *nonviscous*.

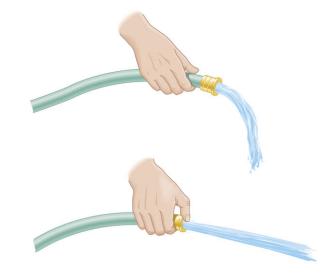
An incompressible, nonviscous fluid is called an *ideal fluid*.

11.7 Fluids in Motion

When the flow is steady, *streamlines* are often used to represent the trajectories of the fluid particles.

The mass of fluid per second that flows through a tube is called the *mass flow rate*.





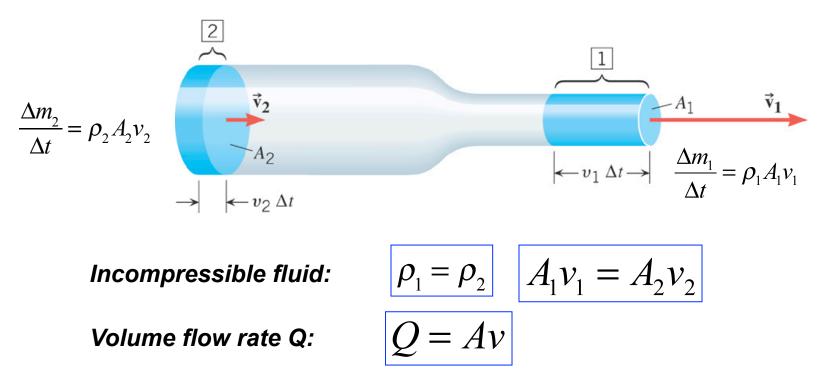
11.8 The Equation of Continuity

EQUATION OF CONTINUITY

The mass flow rate has the same value at every position along a tube that has a single entry and a single exit for fluid flow.

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

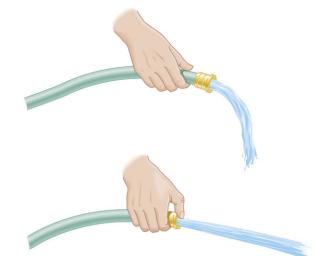
SI Unit of Mass Flow Rate: kg/s



11.8 The Equation of Continuity

Example 12 A Garden Hose

A garden hose has an unobstructed opening with a cross sectional area of $2.85 \times 10^{-4} \text{m}^2$. It fills a bucket with a volume of $8.00 \times 10^{-3} \text{m}^3$ in 30 seconds.



Find the speed of the water that leaves the hose through (a) the unobstructed opening and (b) an obstructed opening with half as much area.

a)
$$Q = Av$$

 $v = \frac{Q}{A} = \frac{\left(\frac{8.00 \times 10^{-3} \text{ m}^3}{2.85 \times 10^{-4} \text{ m}^2}\right) = 0.936 \text{ m/s}$

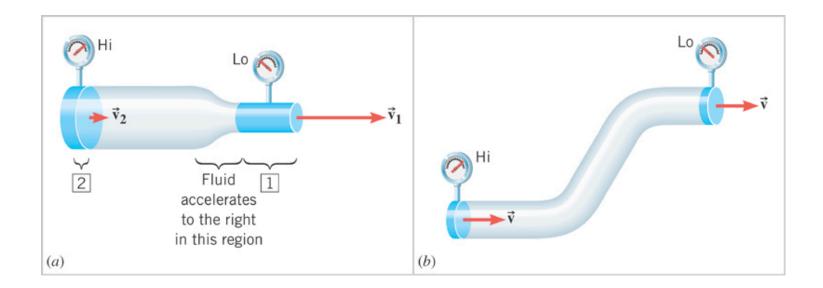
b)
$$A_1 v_1 = A_2 v_2$$

 $v_2 = \frac{A_1}{A_2} v_1 = (2)(0.936 \text{ m/s}) = 1.87 \text{ m/s}$

11.9 Bernoulli's Equation

The fluid accelerates toward the lower pressure regions.

According to the pressure-depth relationship, the pressure is lower at higher levels, provided the area of the pipe does not change.



Apply Work-Energy theorem to determine relationship between pressure, height, velocity, of the fluid.

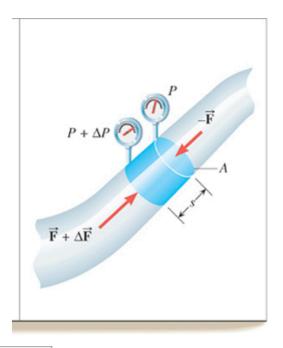
11.9 Bernoulli's Equation

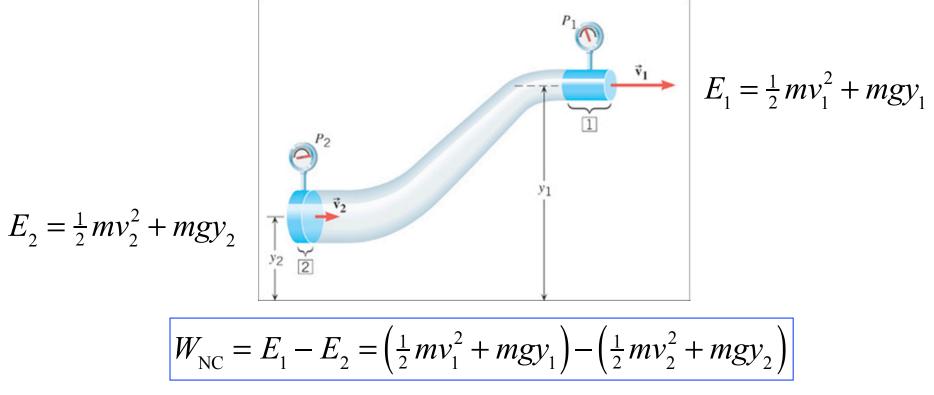
Work done by tiny pressure "piston"

$$W_{\Delta P} = \left(\sum F\right)s = \left(\Delta F\right)s = \left(\Delta PA\right)s; \quad V = As$$

Work (NC) done by pressure difference from 2 to 1

$$W_{\rm NC} = \left(P_2 - P_1\right)V$$





11.9 Bernoulli's Equation

$$\begin{split} W_{\rm NC} &= \left(P_2 - P_1\right) V \\ W_{\rm NC} &= E_1 - E_2 = \left(\frac{1}{2}mv_1^2 + mgy_1\right) - \left(\frac{1}{2}mv_2^2 + mgy_2\right) & \begin{array}{l} {\rm NC} \ {\rm Work \ yields \ a} \\ {\rm total \ Energy \ change.} \end{split}$$

Equating the two expressions for the work done,

$$(P_2 - P_1)V = (\frac{1}{2}mv_1^2 + mgy_1) - (\frac{1}{2}mv_2^2 + mgy_2)$$
 $m = \rho V$

$$(P_2 - P_1) = (\frac{1}{2}\rho v_1^2 + \rho g y_1) - (\frac{1}{2}\rho v_2^2 + \rho g y_2)$$

Rearrange to obtain Bernoulli's Equation BERNOULLI'S EQUATION

In steady flow of a nonviscous, incompressible fluid, the pressure, the fluid speed, and the elevation at two points are related by:

$$P_1 + \frac{1}{2}\rho v_1^2 + \rho g y_1 = P_2 + \frac{1}{2}\rho v_2^2 + \rho g y_2$$

11.10 Applications of Bernoulli's Equation

Conceptual Example 14 Tarpaulins and Bernoulli's Equation

When the truck is stationary, the tarpaulin lies flat, but it bulges outward when the truck is speeding down the highway.

Account for this behavior.

Bernoulli's Equation

$$P_1 + \frac{1}{2}\rho v_1^2 + \rho g y_1 = P_2 + \frac{1}{2}\rho v_2^2 + \rho g y_2$$

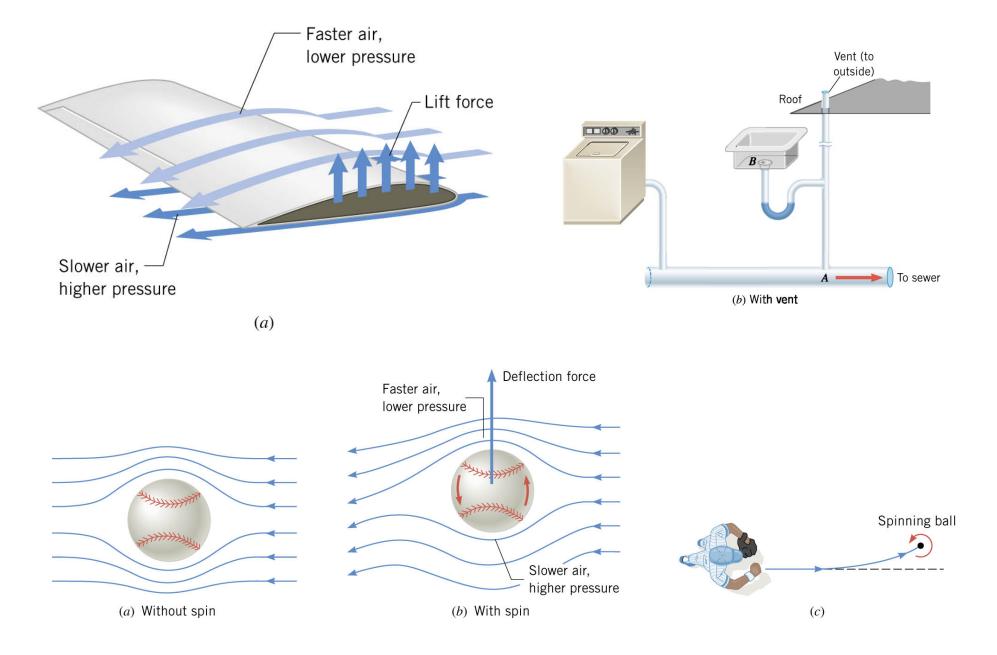
$$P_1 = P_2 + \frac{1}{2}\rho v_2^2$$

 $P_{1} > P_{2}$

Tarpaulin is flat

Moving

11.10 Applications of Bernoulli's Equation



11.10 Applications of Bernoulli's Equation

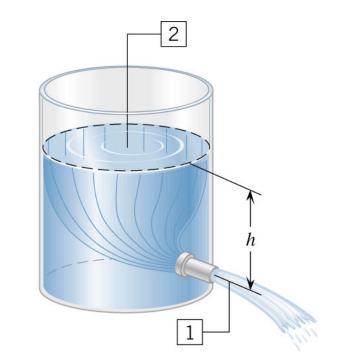
Example 16 Efflux Speed

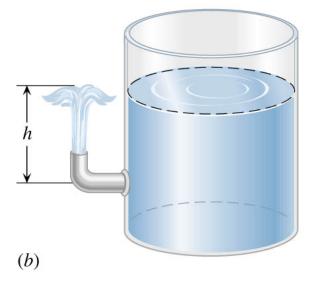
The tank is open to the atmosphere at the top. Find and expression for the speed of the liquid leaving the pipe at the bottom.

$$P_1 = P_2 = P_{atmosphere} (1 \times 10^5 \text{ N/m}^2)$$

 $v_2 = 0, \quad y_2 = h, \quad y_1 = 0$

$$P_{1} + \frac{1}{2}\rho v_{1}^{2} + \rho g y_{1} = P_{2} + \frac{1}{2}\rho v_{2}^{2} + \rho g y_{2}$$
$$\frac{1}{2}\rho v_{1}^{2} = \rho g h$$
$$v_{1} = \sqrt{2gh}$$



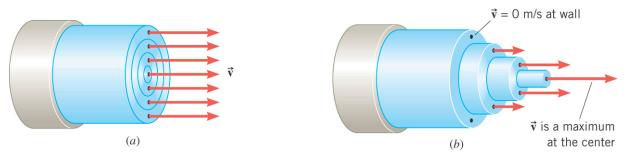


(a)

11.11 Viscous Flow

Flow of an ideal fluid.

Flow of a viscous fluid.



FORCE NEEDED TO MOVE A LAYER OF VISCOUS FLUID WITH CONSTANT VELOCITY

The magnitude of the tangential force required to move a fluid layer at a constant speed is given by:

$$F = \frac{\eta A v}{y}$$

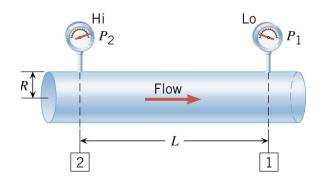
 η , is the coefficient of viscosity SI Unit: Pa · s; 1 poise (P) = 0.1 Pa · s

POISEUILLE'S LAW (flow of viscous fluid)

The volume flow rate is given by:

$$Q = \frac{\pi R^4 \left(P_2 - P_1 \right)}{8\eta L}$$

Pressure drop in a straight uniform diamater pipe.

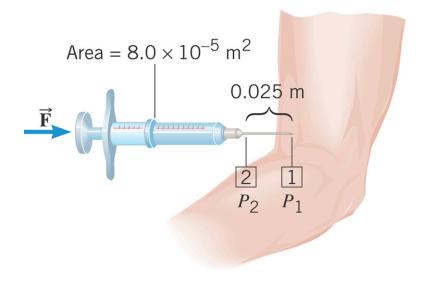


11.11 Viscous Flow

Example 17 Giving and Injection

A syringe is filled with a solution whose viscosity is 1.5×10^{-3} Pa·s. The internal radius of the needle is 4.0×10^{-4} m.

The gauge pressure in the vein is 1900 Pa. What force must be applied to the plunger, so that $1.0x10^{-6}m^3$ of fluid can be injected in 3.0 s?



$$P_{2} - P_{1} = \frac{8\eta LQ}{\pi R^{4}}$$

= $\frac{8(1.5 \times 10^{-3} \text{ Pa} \cdot \text{s})(0.025 \text{ m})(1.0 \times 10^{-6} \text{ m}^{3}/3.0 \text{ s})}{\pi (4.0 \times 10^{-4} \text{m})^{4}}$ = 1200 Pa
 $P_{2} = (1200 + P_{1}) \text{ Pa} = (1200 + 1900) \text{ Pa} = 3100 \text{ Pa}$
 $F = P_{2}A = (3100 \text{ Pa})(8.0 \times 10^{-5} \text{ m}^{2}) = 0.25 \text{ N}$