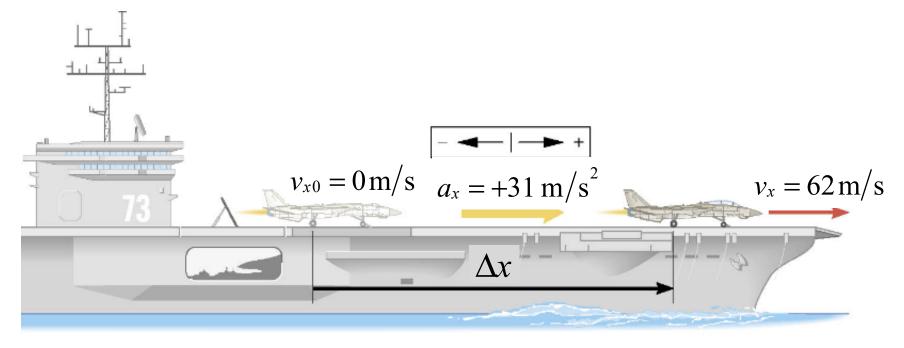
Chapter 2

Kinematics in One Dimension

continued



(b)

Example: Catapulting a Jet

Find its displacement.

$$v_{x0} = 0 \text{ m/s}$$
 $v_x = +62 \text{ m/s}$ $a_x = +31 \text{ m/s}^2$
 $\Delta x = ??$

definition of acceleration

$$a_{x} = \frac{v_{x} - v_{x0}}{t} \qquad \qquad t = \frac{v_{x} - v_{x0}}{a_{x}} \qquad \text{time velocity is changing}$$

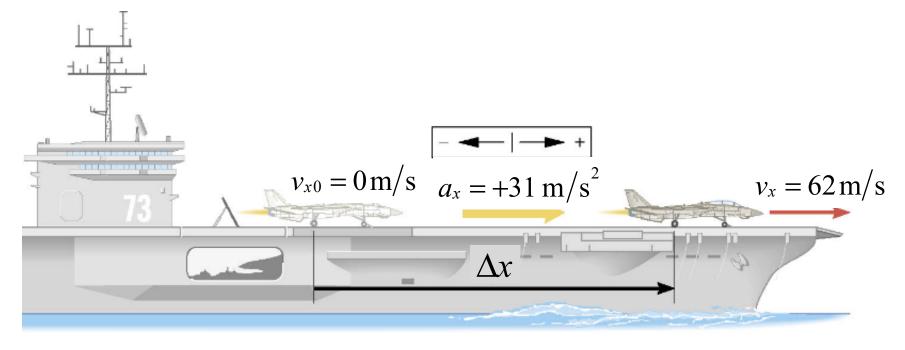
$$\Delta x = \frac{1}{2} \left(v_{x0} + v_{x} \right) t = \frac{1}{2} \left(v_{x0} + v_{x} \right) \frac{\left(v_{x} - v_{x0} \right)}{a_{x}}$$

$$displacement = \frac{average}{velocity} \times time$$

$$Solve for$$

$$final velocity$$

$$v_{x}^{2} = v_{x0}^{2} + 2a_{x}\Delta x \qquad \Delta x = \frac{v_{x}^{2} - v_{x0}^{2}}{2a_{x}}$$



(b)

$$\Delta x = \frac{v_x^2 - v_{x0}^2}{2a_x} = \frac{\left(62 \,\mathrm{m/s}\right)^2 - \left(0 \,\mathrm{m/s}\right)^2}{2\left(31 \,\mathrm{m/s}^2\right)} = +62 \,\mathrm{m}$$

Equations of Kinematics for Constant Acceleration

$$v_x = v_{x0} + a_x t$$
$$\Delta x = \frac{1}{2} \left(v_{x0} + v_x \right) t$$
$$v_x^2 = v_{x0}^2 + 2a_x \Delta x$$
$$\Delta x = v_{x0} t + \frac{1}{2} a_x t^2$$

Except for *t*, every variable has a direction and thus can have a positive or negative value. 2.4 Applications of the Equations of Kinematics

Reasoning Strategy

1. Make a drawing.

2. Decide which directions are to be called positive (+) and negative (-).

3. Write down the values that are given for any of the five kinematic variables.

4. Verify that the information contains values for at least three of the five kinematic variables. Select the appropriate equation.

5. When the motion is divided into segments, remember that the final velocity of one segment is the initial velocity for the next.

6. Keep in mind that there may be two possible answers to a kinematics problem.

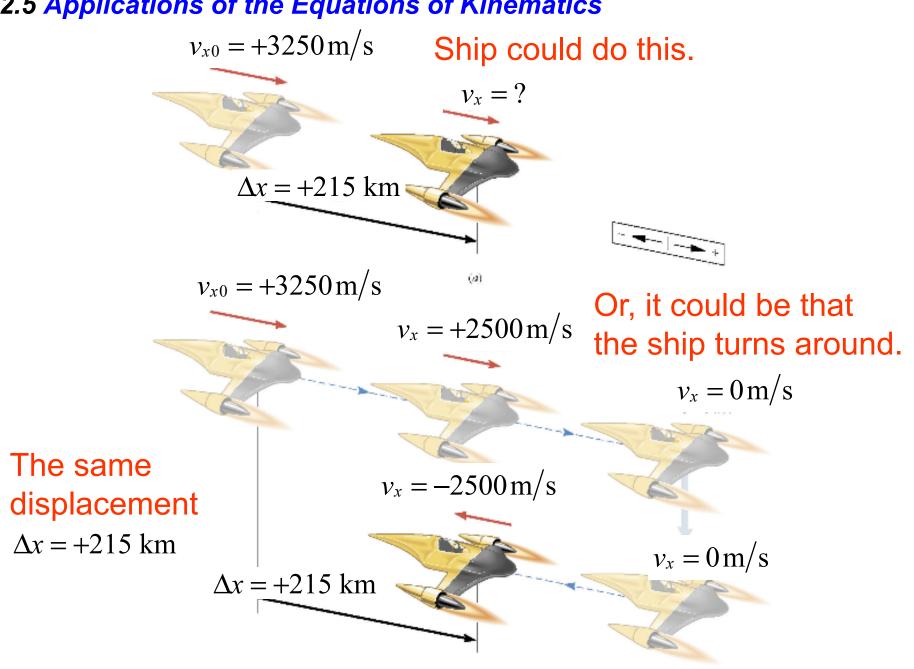
2.5 Applications of the Equations of Kinematics

Example: An Accelerating Spacecraft

initial velocity

A spacecraft is traveling with a velocity of +3250 m/s. Suddenly the retrorockets are fired, and the spacecraft begins to <u>slow down</u> with an acceleration whose magnitude is 10.0 m/s². What is the <u>velocity of the spacecraft when</u> the displacement of the craft is +215 km, relative to the point where the retrorockets began firing?

ΔX	a _x	V _X	V _{x0}	t
+215000 m	-10.0 m/s ²	?	+3250 m/s	
	acceleration			
	is negative			



2.5 Applications of the Equations of Kinematics

2.5 Applications of the Equations of Kinematics

ΔX	a _x	V _x	V _{x0}	t
+215000 m	-10.0 m/s ²	?	+3250 m/s	

$$v_x^2 = v_{x0}^2 + 2a_x \Delta x = \sqrt{v_{x0}^2 + 2a_x \Delta x}$$

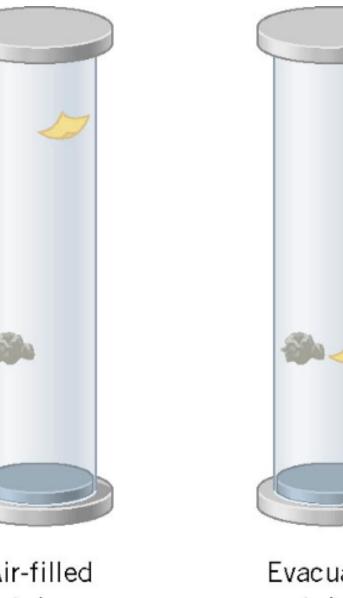
$$v_x = \pm \sqrt{(3250 \,\mathrm{m/s})^2 + 2(-10.0 \,\mathrm{m/s^2})(215000 \,\mathrm{m})}$$
$$= \pm 2500 \,\mathrm{m/s}$$

For vertical motion, we will replace the *x* label with *y* in all kinematic equations, and use upward as positive.

In the absence of air resistance, it is found that all bodies at the same location above the Earth fall vertically with the same acceleration. If the distance of the fall is small compared to the radius of the Earth, then the acceleration remains essentially constant throughout the descent.

This idealized motion is called <u>free-fall</u> and the acceleration of a freely falling body is called the <u>acceleration due to</u> <u>gravity</u>, and the acceleration is downward or negative.

$$a_y = -g = -9.81 \,\mathrm{m/s^2}$$
 or $-32.2 \,\mathrm{ft/s^2}$



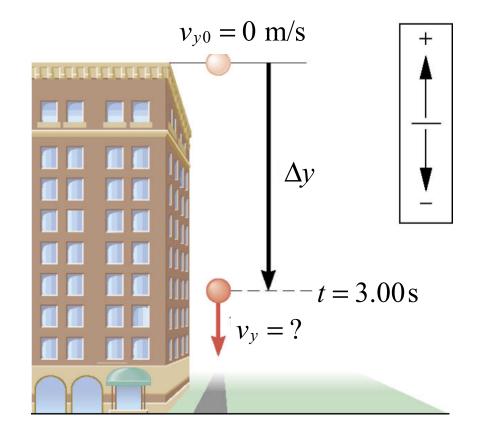
acceleration due to gravity.

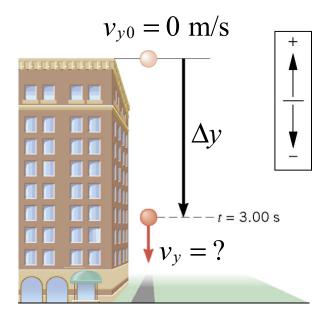
$$a_y = -g = -9.80 \,\mathrm{m/s^2}$$

Air-filled tube (a) Evacuated tube (b)

Example: A Falling Stone

A stone is dropped from the top of a tall building. After 3.00s of free fall, what is the displacement, Δy of the stone?





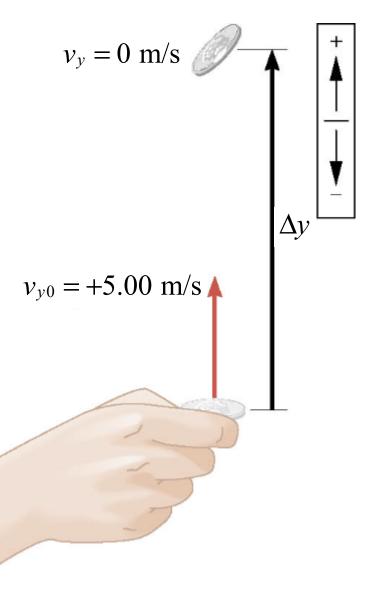
Δγ	a _y	Vy	V _{y0}	t
?	–9.80 m/s²		0 m/s	3.00 s

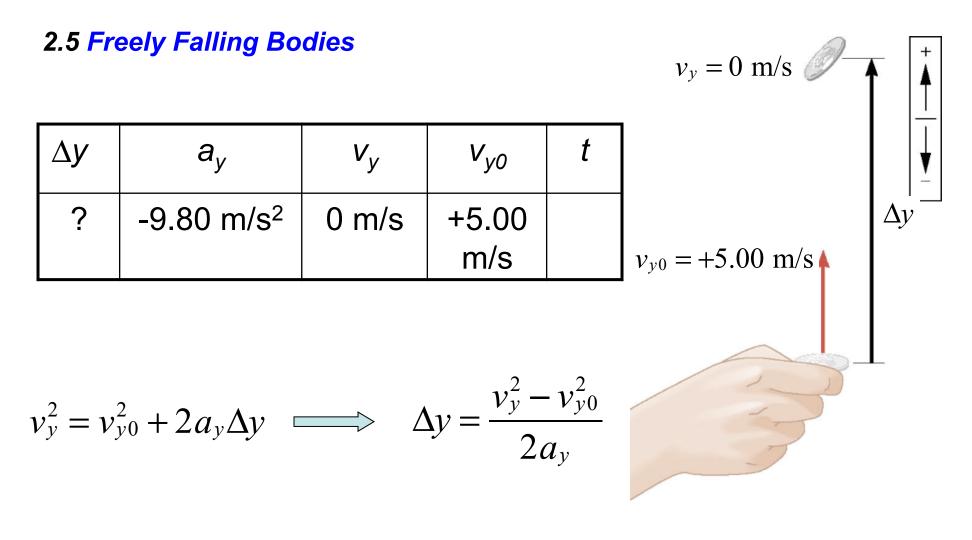
$$\Delta y = v_{y0}t + \frac{1}{2}a_yt^2$$

= $(0 \text{ m/s})(3.00 \text{ s}) + \frac{1}{2}(-9.80 \text{ m/s}^2)(3.00 \text{ s})^2$
= -44.1 m

Example: How High Does it Go?

The referee tosses the coin up with an initial speed of 5.00m/s. In the absence if air resistance, how high does the coin go above its point of release?





$$\Delta y = \frac{v_y^2 - v_{y0}^2}{2a_y} = \frac{\left(0 \,\mathrm{m/s}\right)^2 - \left(5.00 \,\mathrm{m/s}\right)^2}{2\left(-9.80 \,\mathrm{m/s}^2\right)} = 1.28 \,\mathrm{m}$$

Conceptual Example 14 Acceleration Versus Velocity

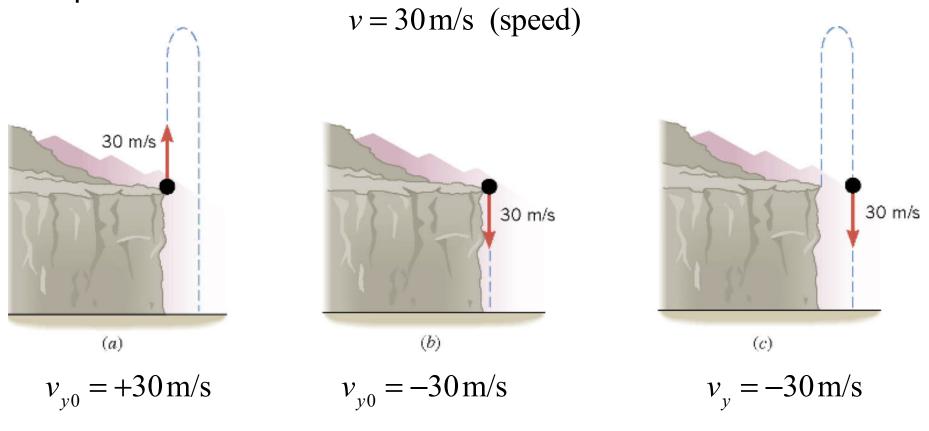
There are three parts to the motion of the coin.

- 1) On the way up, the coin has an upward-pointing velocity with a decreasing magnitude.
- 2) At that time the coin reaches the top of its path, the coin has an instantaneously zero velocity.
- 3) On the way down, the coin has a downward-pointing velocity with an increasing magnitude.

In the absence of air resistance, does the acceleration vector of the coin, like the velocity, change from one part to another?

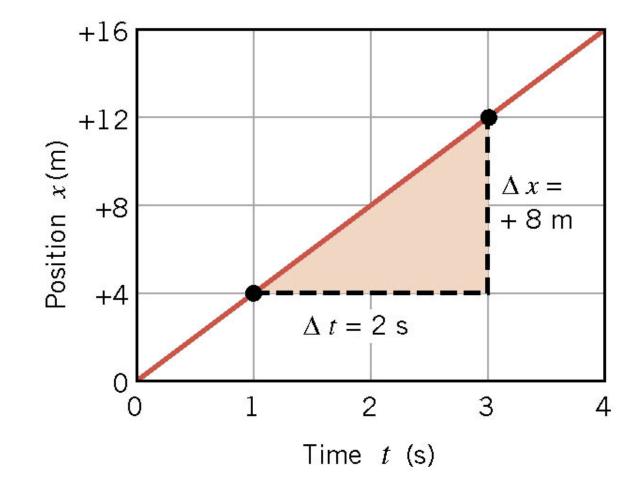
Conceptual Example: Taking Advantage of Symmetry

Does the pellet in part *b* strike the ground beneath the cliff with a smaller, greater, or the same speed as the pellet in part *a*?



2.5 Graphical Analysis of Velocity and Acceleration

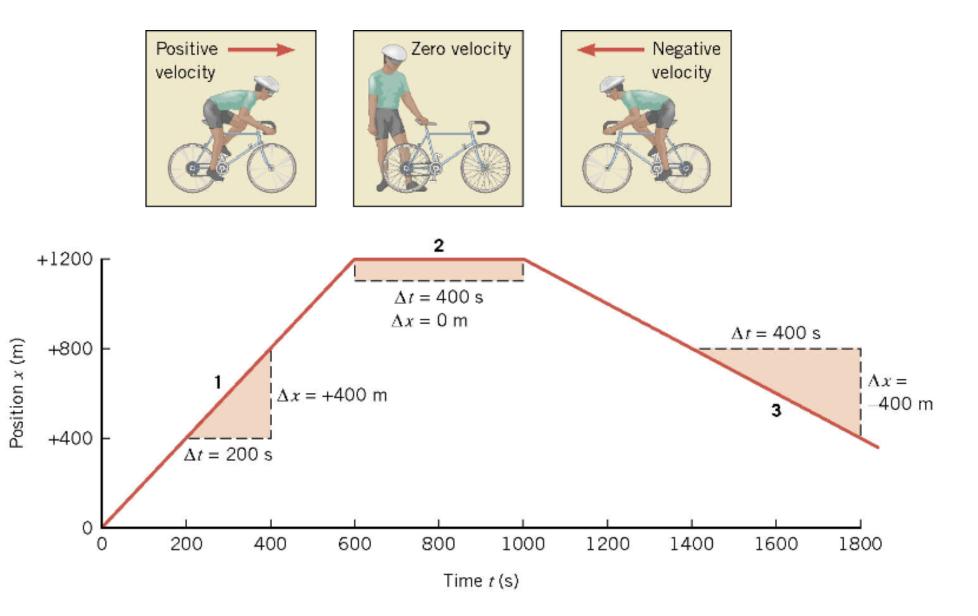
Graph of position vs. time.

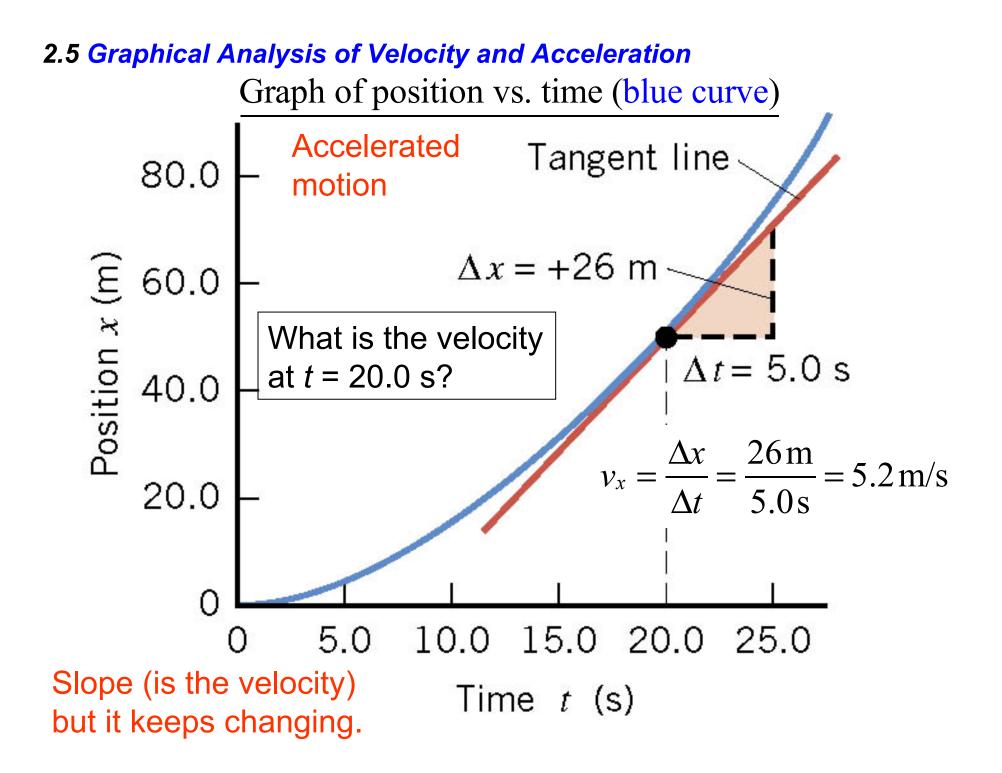


Slope $=\frac{\Delta x}{\Delta t} = \frac{+8 \text{ m}}{2 \text{ s}} = +4 \text{ m/s}$

The same slope at all times. This means constant velocity!

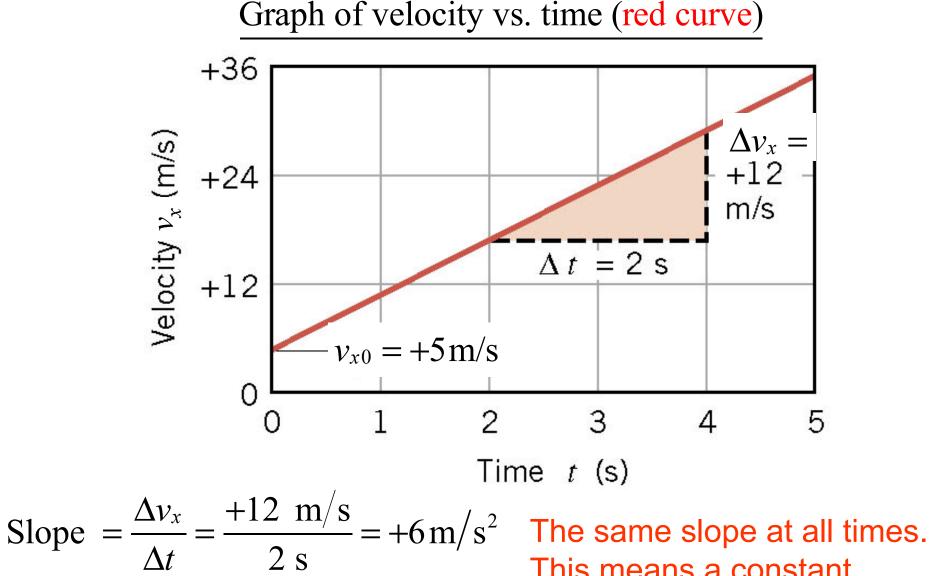
2.5 Graphical Analysis of Velocity and Acceleration





2.5 Graphical Analysis of Velocity and Acceleration

 $a_x = +6 \,\mathrm{m/s^2}$



This means a constant acceleration!

2.5 Summary equations of kinematics in one dimension

Equations of Kinematics for Constant Acceleration

$$v_x = v_{x0} + a_x t$$
$$\Delta x = \frac{1}{2} \left(v_{x0} + v_x \right) t$$
$$v_x^2 = v_{x0}^2 + 2a_x \Delta x$$
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Except for *t*, every variable has a direction and thus can have a positive or negative value.

For vertical motion replace x with y