

Chapter 12

Temperature and Heat

continued

12.3 The Ideal Gas Law

THE IDEAL GAS LAW

The absolute pressure of an ideal gas is directly proportional to the Kelvin temperature and the number of moles (n) of the gas and is inversely proportional to the volume of the gas.

$$P = \frac{nRT}{V}$$

$$PV = nRT$$

$$R = 8.31 \text{ J}/(\text{mol} \cdot \text{K})$$

Another form for the Ideal Gas Law using the number of atoms (N)

$$PV = nRT$$

$$= N \left(\frac{R}{N_A} \right) T$$

$$N = nN_A$$

Boltzmann's constant

$$PV = Nk_B T$$

$$k_B = \frac{R}{N_A} = \frac{8.31 \text{ J}/(\text{mol} \cdot \text{K})}{6.022 \times 10^{23} \text{ mol}^{-1}} = 1.38 \times 10^{-23} \text{ J/K}$$

When temperature is involved, a letter $k = k_B$, Boltzmann's constant

Clicker Question 12.2

An ideal gas is enclosed within a container by a moveable piston. If the final temperature is two times the initial temperature and the volume is reduced to one-fourth of its initial value, what will the final pressure of the gas be relative to its initial pressure, P_1 ?

- a) $8P_1$
- b) $4P_1$
- c) $2P_1$
- d) $P_1/2$
- e) $P_1/4$

Clicker Question 12.2

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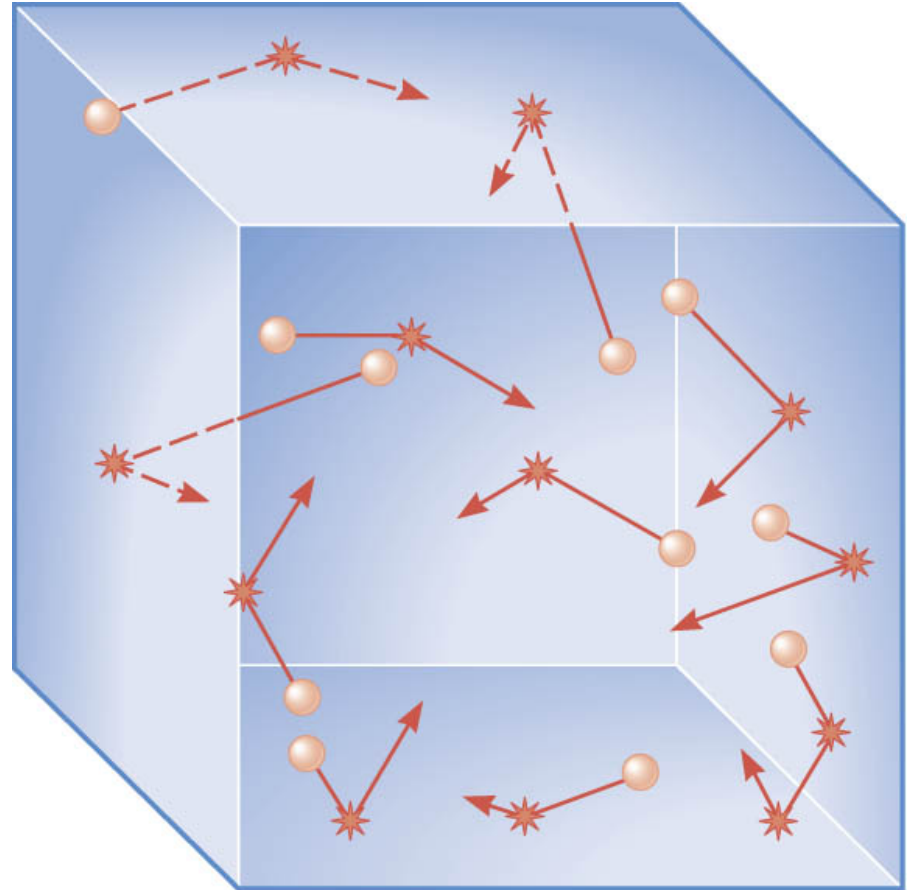
$$P_1 V_1 = nRT_1; \quad V_2 = V_1/4; \quad T_2 = 2T_1$$
$$P_2 = \frac{nRT_2}{V_2} = \frac{nR(2T_1)}{V_1/4} = 8 \frac{nRT_1}{V_1} = 8P_1$$

12.4 *Kinetic Theory of Gases*

The particles are in constant, random motion, colliding with each other and with the walls of the container.

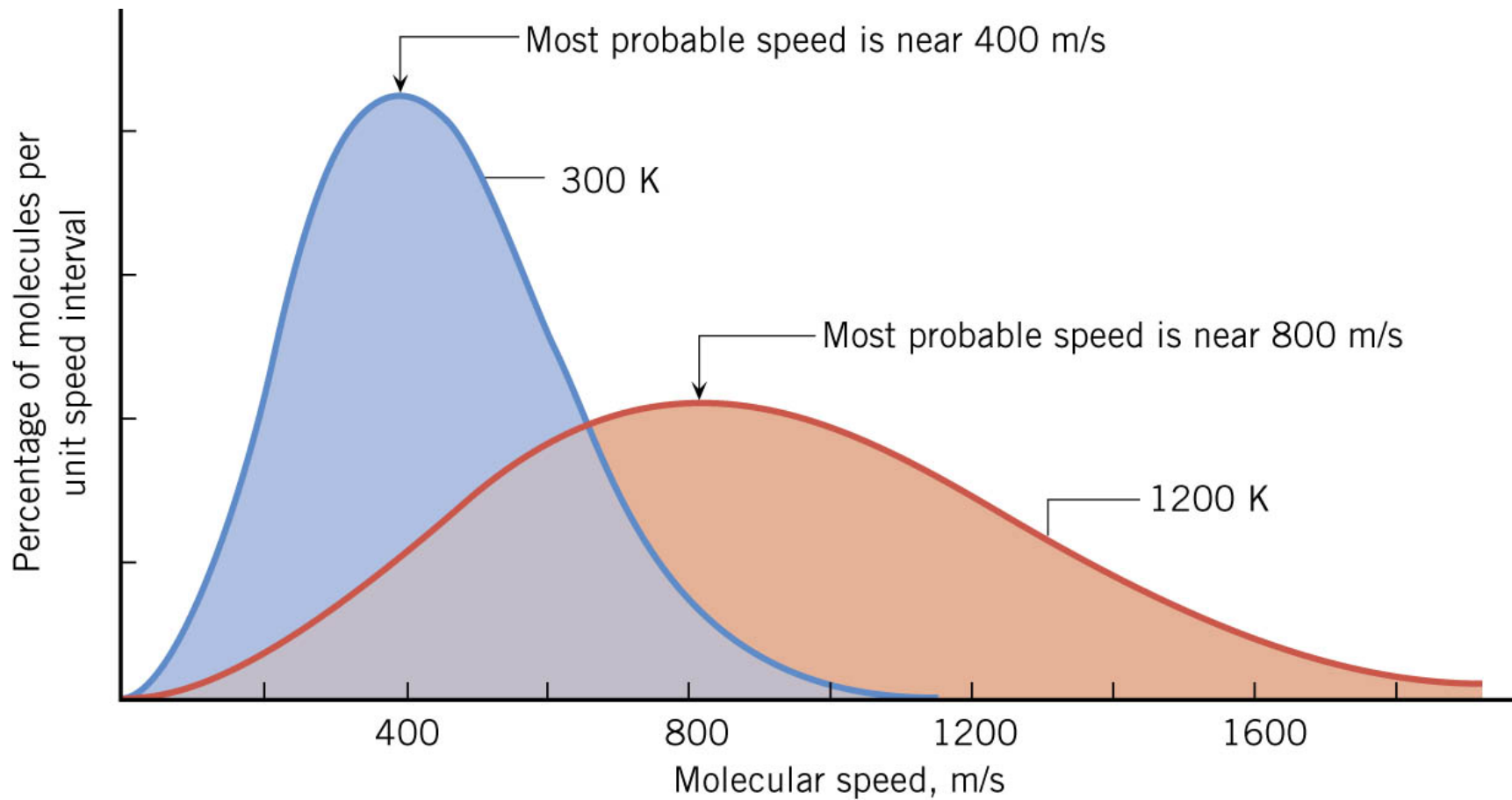
Each collision changes the particle's speed.

As a result, the atoms and molecules have different speeds.



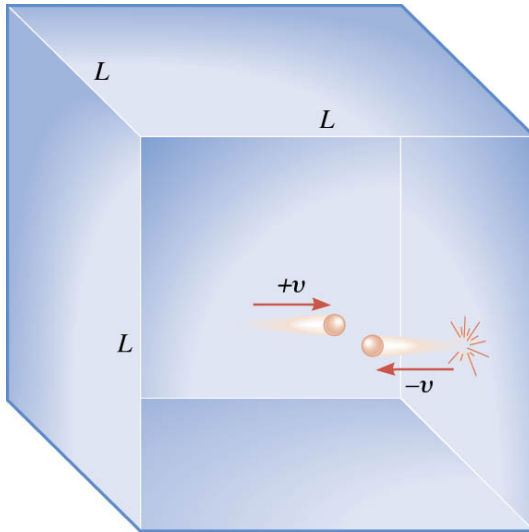
12.4 Kinetic Theory of Gases

THE DISTRIBUTION OF MOLECULAR SPEEDS



12.4 Kinetic Theory of Gases

KINETIC THEORY



$$\sum F = ma = m \frac{\Delta v}{\Delta t} = \frac{\Delta(mv)}{\Delta t}$$

$$\begin{aligned} \text{Average force on each gas molecule when hitting the wall} &= \frac{\text{Final momentum} - \text{Initial momentum}}{\text{Time between successive collisions}} \\ &= \frac{(-mv) - (+mv)}{2L/v} = \frac{-mv^2}{L} \end{aligned}$$

Average force
on a wall

$$\bar{F} = \left(\frac{N}{3} \right) \left(\frac{mv^2}{L} \right) \Rightarrow P = \frac{\bar{F}}{A} = \frac{\bar{F}}{L^2} = \left(\frac{N}{3} \right) \left(\frac{mv^2}{L^3} \right)$$

$$PV = \left(\frac{N}{3} \right) mv^2 = \frac{2}{3} N \left(\frac{1}{2} mv^2 \right)$$

$$PV = NkT$$

$$\overline{KE} = \frac{1}{2} mv^2$$

$$v_{rms} = \sqrt{\overline{v^2}}$$

root mean
square speed

Temperature reflects the average
Kinetic Energy of the molecules

$$\frac{3}{2} kT = \frac{1}{2} mv_{rms}^2 = \overline{KE}$$

$$k = 1.38 \times 10^{-23} \text{ J/K}$$

12.4 Kinetic Theory of Gases

Example: The Speed of Molecules in Air

Air is primarily a mixture of nitrogen N_2 molecules (molecular mass 28.0u) and oxygen O_2 molecules (molecular mass 32.0u). Assume that each behaves as an ideal gas and determine the rms speeds of the nitrogen and oxygen molecules when the temperature of the air is 293K.

$$\frac{1}{2} m v_{rms}^2 = \frac{3}{2} kT$$

$$v_{rms} = \sqrt{\frac{3kT}{m}}$$

T must be in Kelvin
($K = C^\circ + 273$)

$$\begin{aligned} &\text{Nitrogen molecule} \\ m &= \frac{28.0 \text{ g/mol}}{6.022 \times 10^{23} \text{ mol}^{-1}} \\ &= 4.65 \times 10^{-26} \text{ kg} \end{aligned}$$

$$\begin{aligned} v_{rms} &= \sqrt{\frac{3kT}{m}} \\ &= \sqrt{\frac{3(1.38 \times 10^{-23} \text{ J/K})(293 \text{ K})}{4.65 \times 10^{-26} \text{ kg}}} = 511 \text{ m/s} \end{aligned}$$

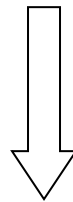
Molecules are moving really fast
but do not go very far before hitting
another molecule.

12.4 Kinetic Theory of Gases

THE INTERNAL ENERGY OF A MONO-ATOMIC IDEAL GAS

$$\overline{\text{KE}} = \frac{1}{2} m v_{rms}^2 = \frac{3}{2} kT$$

Average KE per atom



multiply by the number of atoms

$$U = N \frac{3}{2} kT = \frac{3}{2} nRT$$

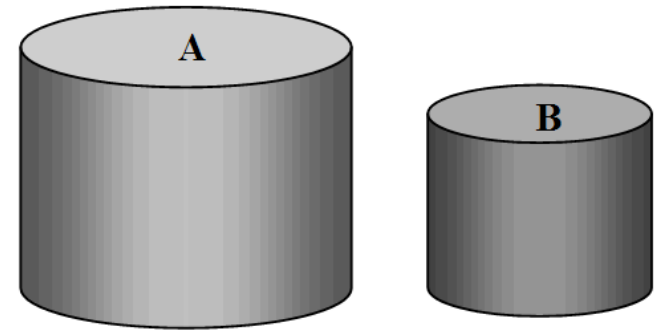
Total Internal Energy

THE INTERNAL ENERGY OF A MOLECULAR GAS
MUST INCLUDE MOLECULAR VIBRATIONS!

$\text{H}_2, \text{N}_2, \text{H}_2\text{O}, \text{SO}_2, \text{CO}_2, \dots$ (most gases except Nobel gases)

Clicker Question 12.3

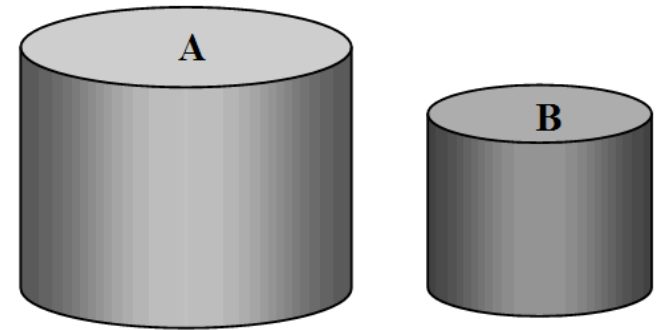
Two sealed containers, labeled A and B as shown, are at the same temperature and each contain the same number of moles of an ideal monatomic gas. Which one of the following statements concerning these containers is true?



- a) The rms speed of the atoms in the gas is greater in B than in A
- b) The frequency of collisions of the atoms with the walls of container B are greater than that for container A
- c) The kinetic energy of the atoms in the gas is greater in B than in A.
- d) The pressure within container B is less than the pressure inside container A.
- e) The force that each atom exerts on a hit wall of container B is greater than for those in container A.

Clicker Question 12.3

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- a) The rms speed of the atoms in the gas is greater in B than in A
- b) The frequency of collisions of the atoms with the walls of container B are greater than that for container A**
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Chapter 13

Heat

13.1 Heat and Internal Energy

DEFINITION OF HEAT

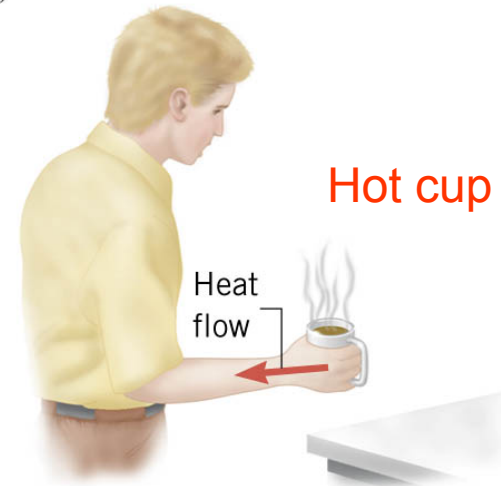
Heat is energy that flows from a higher-temperature object to a lower-temperature object because of a difference in temperatures.

SI Unit of Heat: joule (J)

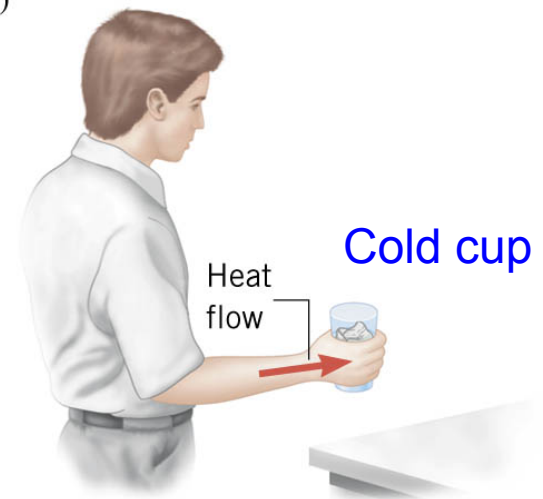
The heat that flows from hot to cold originates in the *internal energy* of the hot substance.

It is not correct to say that a substance contains heat. You must use the word *energy* or *internal energy*.

(a)



(b)



13.2 Heat and Temperature Change: Specific Heat Capacity

Temperature of an object reflects the amount of internal energy within it. But objects with the same temperature and mass can have DIFFERENT amounts of internal energy!

SOLIDS AND LIQUIDS (GASES ARE DIFFERENT)

HEAT SUPPLIED OR REMOVED IN CHANGING THE TEMPERATURE OF A SUBSTANCE.

The heat that must be supplied or removed to change the temperature of a substance is

$$Q = mc\Delta T$$

c , is the specific heat capacity of the substance

Common Unit for Specific Heat Capacity: $\text{J}/(\text{kg}\cdot\text{C}^\circ)$

$$\Delta T > 0, \text{ Heat added}$$

$$\Delta T < 0, \text{ Heat removed}$$

GASES

The value of the specific heat of a gas depends on whether the pressure or volume is held constant.

This distinction is not important for solids.

13.2 Heat and Temperature Change: Specific Heat Capacity

Example: A Hot Jogger

In a half-hour, a 65-kg jogger produces 8.0×10^5 J of heat. This heat is removed from the body by a variety of means, including sweating, one of the body's own temperature-regulating mechanisms. If the heat were not removed, how much would the body temperature increase?

$$Q = mc\Delta T$$
$$\Delta T = \frac{Q}{mc} = \frac{8.0 \times 10^5 \text{ J}}{(65 \text{ kg})[3500 \text{ J}/(\text{kg} \cdot \text{C}^\circ)]} = 3.5 \text{ C}^\circ$$

OTHER UNITS for heat production

1 cal = 4.186 joules (calorie)

1 kcal = 4186 joules ([kilo]calories for food)

Specific means per unit mass

Specific Heat Capacities^a of Some Solids and Liquids

Substance	Specific Heat Capacity, c $\text{J}/(\text{kg} \cdot \text{C}^\circ)$
Solids	
Aluminum	9.00×10^2
Copper	387
Glass	840
Human body (37 °C, average)	3500
Ice (−15 °C)	2.00×10^3
Iron or steel	452
Lead	128
Silver	235
Liquids	
Benzene	1740
Ethyl alcohol	2450
Glycerin	2410
Mercury	139
Water (15 °C)	4186

^aExcept as noted, the values are for 25 °C and 1 atm of pressure.

Clicker Question 13.1

Four 1-kg cylinders are heated to 100 C° and placed on top of a block of paraffin wax, which melts at 63 C°. There is one cylinder made from lead, one of copper, one of aluminum, and one of iron. After a few minutes, it is observed that the cylinders have sunk into the paraffin to differing depths. Rank the depths of the cylinders from deepest to shallowest..

$$Q = mc\Delta T$$

- a) lead > iron > copper > aluminum
- b) aluminum > copper > lead > iron
- c) aluminum > iron > copper > lead
- d) copper > aluminum > iron > lead
- e) iron > copper > lead > aluminum

Specific Heat Capacities^a of Some Solids and Liquids

Substance	Specific Heat Capacity, c J/(kg · C°)
Solids	
Aluminum	9.00×10^2
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Iron or steel	452
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$$Q = mc\Delta T$$

- a) lead > iron > copper > aluminum
- b) aluminum > copper > lead > iron
- c) aluminum > iron > copper > lead**
- d) copper > aluminum > iron > lead
- e) iron > copper > lead > aluminum

Specific Heat Capacities^a of Some Solids and Liquids

Substance	Specific Heat Capacity, c J/(kg · C°)
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Iron or steel	452 2
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13.2 Specific Heat Capacities (Gases)

To relate heat and temperature change in **solids and liquids (mass in kg)**, use:

$$Q = mc\Delta T \quad \text{specific heat capacity, } c \left[\text{J}/(\text{kg} \cdot ^\circ\text{C}) \right]$$

For **gases**, the amount of gas is given in moles, use molar heat capacities:

$$Q = nC\Delta T \quad \text{molar heat capacity, } C \left[\text{J}/(\text{mole} \cdot ^\circ\text{C}) \right]$$

$$C = (m/n)c = m_u c; \quad m_u = \text{mass/mole (kg)}$$

ALSO, for gases it is necessary to distinguish between the molar specific heat capacities at constant pressure and at constant volume:

$$C_P, C_V$$

**Constant pressure
for a monatomic ideal gas**

$$Q_P = nC_P\Delta T$$
$$C_P = \frac{5}{2}R$$

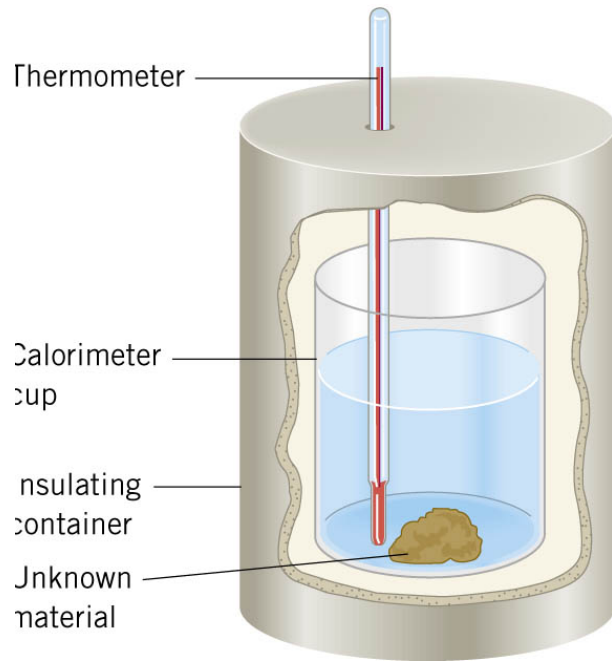
**Constant volume
for a monatomic ideal gas**

$$Q_V = nC_V\Delta T$$
$$C_V = \frac{3}{2}R$$

any ideal gas

$$C_P - C_V = R$$

13.2 Heat and Temperature Change: Specific Heat Capacity



CALORIMETRY

If there is no heat loss to the surroundings, the heat lost by the hotter object equals the heat gained by the cooler ones. **Net heat change equals zero.**

A calorimeter is made of 0.15 kg of aluminum and contains 0.20 kg of water, both at 18.0 C°. A mass, 0.040 kg at 97.0 C° is added to the water, causing the water temperature to rise to 22.0 C°. What is the specific heat capacity of the mass?

Water and Al rise in temperature ($\Delta T > 0$)

Unknown stuff drops in temperature ($\Delta T < 0$)

$$\Delta T_w = \Delta T_{Al} = +4^\circ\text{C}; \quad \Delta T_{Unk} = -75^\circ\text{C}$$

$$c_{Al} = 900 \text{ J/kg} \cdot \text{C}^\circ$$

$$c_w = 4190 \text{ J/kg} \cdot \text{C}^\circ$$

Al $\equiv$ Aluminum, W $\equiv$ water, Unk $\equiv$ unknown

Net heat change equals zero.

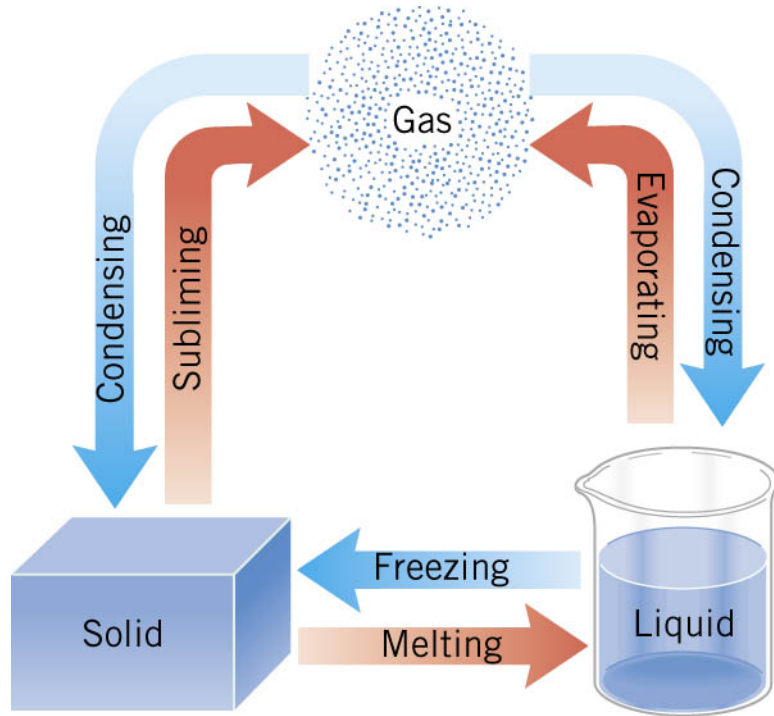
$$\sum Q = m_{Al} c_{Al} \Delta T_{Al} + m_w c_w \Delta T_w + m_{Unk} c_{Unk} \Delta T_{Unk} = 0$$

Three heat changes must sum to zero

$$c_{Unk} = 1.3 \times 10^3 \text{ J/(kg} \cdot \text{C}^\circ)$$

13.3 Heat and Phase Change: Latent Heat

THE PHASES OF MATTER



There is internal energy added or removed in a change of phase.

Typically, solid $\rightarrow$ liquid (melt) or liquid $\rightarrow$ gas (evaporate) requires heat energy to be **ADDED**.

Typically, gas $\rightarrow$ liquid (condense), or liquid $\rightarrow$ solid (freeze) requires heat energy to be **REMOVED**.

HEAT ADDED OR REMOVED IN CHANGING THE PHASE OF A SUBSTANCE

The heat that must be supplied or removed to change the phase of a mass m of a substance is the “latent heat”, L :

$$Q = mL$$

SI Units of Latent Heat: J/kg

13.3 Heat and Phase Change: Latent Heat

Latent Heats^a of Fusion and Vaporization

Substance	Melting Point (°C)	Latent Heat of Fusion, L_f (J/kg)	Boiling Point (°C)	Latent Heat of Vaporization, L_v (J/kg)
Ammonia	-77.8	33.2×10^4	-33.4	13.7×10^5
Benzene	5.5	12.6×10^4	80.1	3.94×10^5
Copper	1083	20.7×10^4	2566	47.3×10^5
Ethyl alcohol	-114.4	10.8×10^4	78.3	8.55×10^5
Gold	1063	6.28×10^4	2808	17.2×10^5
Lead	327.3	2.32×10^4	1750	8.59×10^5
Mercury	-38.9	1.14×10^4	356.6	2.96×10^5
Nitrogen	-210.0	2.57×10^4	-195.8	2.00×10^5
Oxygen	-218.8	1.39×10^4	-183.0	2.13×10^5
Water	0.0	33.5×10^4	100.0	22.6×10^5

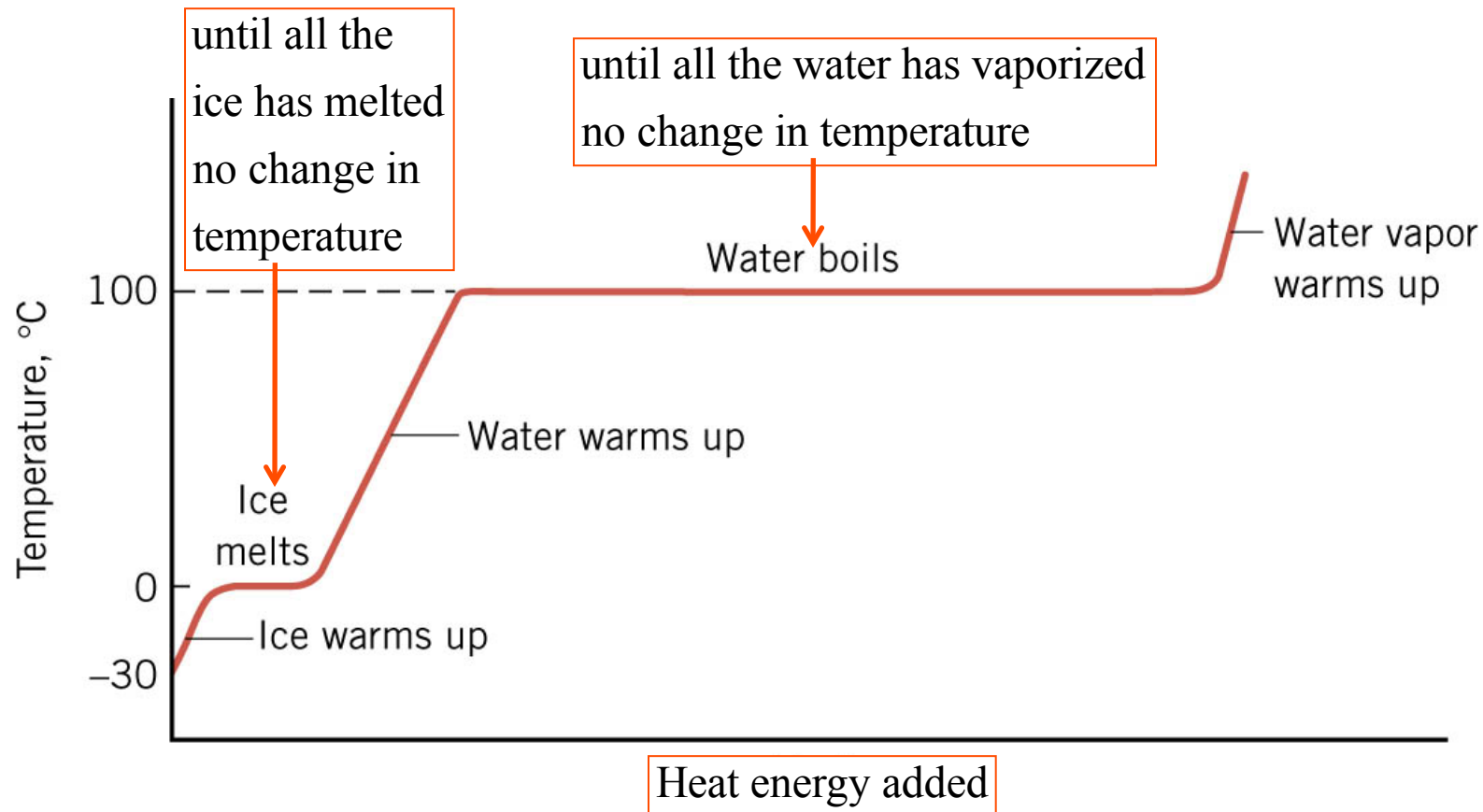
^aThe values pertain to 1 atm pressure.

Add heat: Ice $\rightarrow$ Water $L_f > 0$
Remove heat: Water $\rightarrow$ Ice $L_f < 0$

Add heat: Water $\rightarrow$ Vapor $L_v > 0$
Remove heat: Vapor $\rightarrow$ Water $L_v < 0$

13.3 Heat and Phase Change: Latent Heat

During a phase change, the temperature of the mixture does not change (provided the system is in thermal equilibrium).



13.3 Heat and Phase Change: Latent Heat

Example Ice-cold Lemonade

Ice at 0°C is placed in a Styrofoam cup containing 0.32 kg of lemonade at 27°C. Assume that mass of the cup is very small and lemonade behaves like water.

After ice is added, the ice and lemonade reach an equilibrium temperature ($T = 0\text{ }^{\circ}\text{C}$) with some ice remaining. How much ice melted?

Heat redistributes.
No heat added or lost.

$$\sum Q = \underbrace{m_I L_I}_{\text{Heat for Ice} \rightarrow \text{Water}} + \underbrace{m_W c_W \Delta T_W}_{\text{Heat change of lemonade}} = 0$$

$$\Delta T_W = -27\text{ }^{\circ}\text{C}$$

$$m_I L_I + m_W c_W \Delta T_W = 0$$

$$m_I = \frac{-m_W c_W \Delta T_W}{L_I}$$

$$= \frac{-(0.32\text{ kg})(4.19 \times 10^3 \text{ J/kg} \cdot ^{\circ}\text{C})(-27^{\circ}\text{C})}{33.5 \times 10^4 \text{ J/kg}} = 0.110 \text{ kg}$$

Clicker Question 13.2

A 10.0 kg block of ice has a temperature of 0 C°. How much heat must be added to melt half the ice? Latent heat of fusion for water is 33.5×10^4 J/kg .

$$Q = mL_f$$

- a) 167 J
- b) 1.67×10^6 J
- c) 33.5×10^5 J
- d) 33.5×10^3 J
- e) 33.5 J

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$$Q = mL_f$$

a) 167 J

b) $1.67 \times 10^6 \text{ J}$

c) $3.35 \times 10^5 \text{ J}$

d) $3.35 \times 10^6 \text{ J}$

e) 33.5 J

$$\begin{aligned} Q &= mL_f \\ &= (5.00 \text{ kg})(33.5 \times 10^4 \text{ J/kg}) \\ &= 1.67 \times 10^6 \text{ J} \end{aligned}$$

Chapter 13

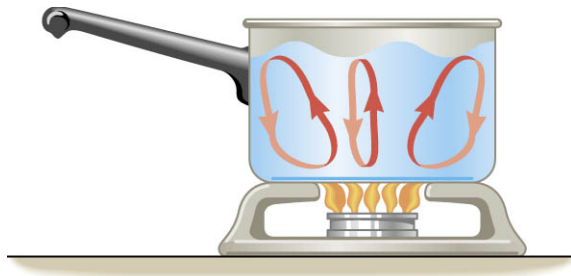
The Transfer of Heat

CONVECTION, CONDUCTION, RADIATION

13.4 Convection

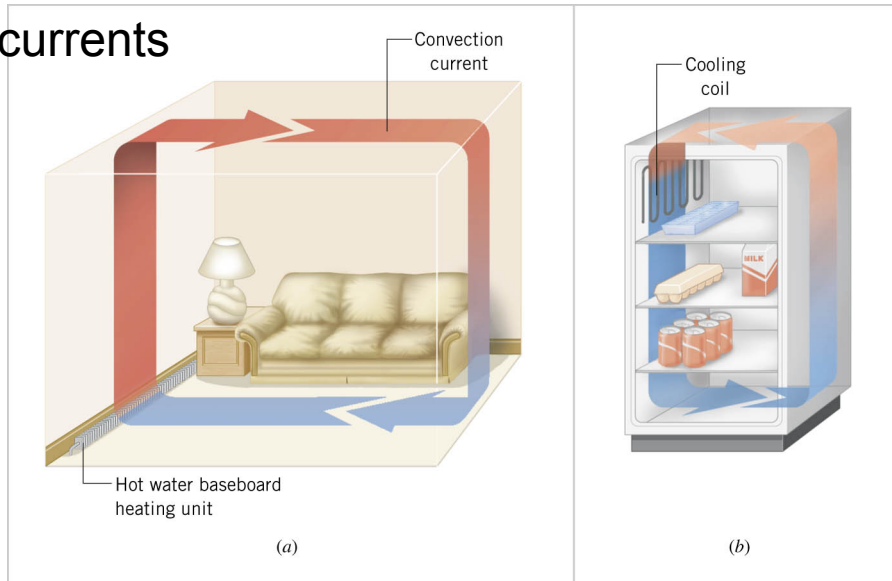
CONVECTION

Heat carried by the bulk movement of a fluid.

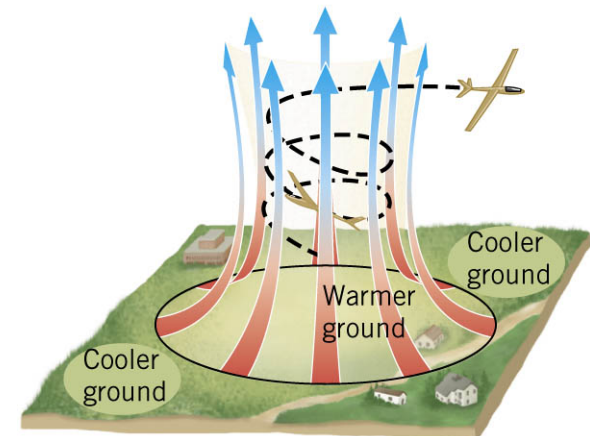


Convection
fluid currents

Convection
air currents



Convection
air currents

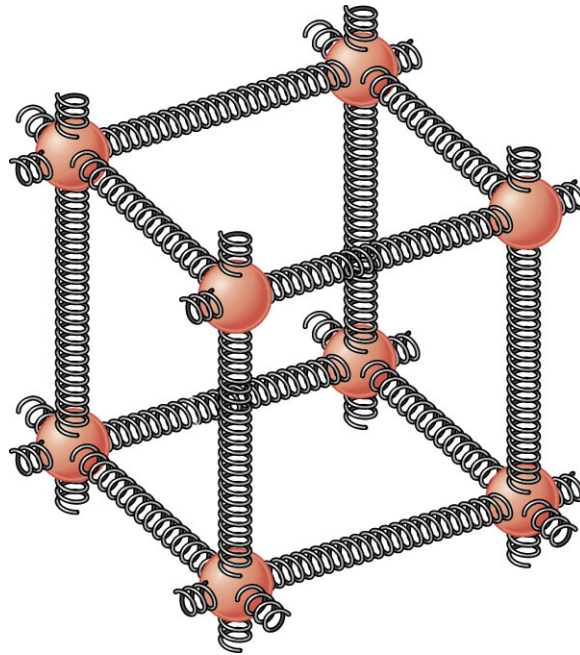


13.4 Conduction

CONDUCTION

Heat transferred directly through a material, but not via bulk motion.

One mechanism for conduction occurs when the atoms or molecules in a hotter part of the material vibrate with greater energy than those in a cooler part. Though the atomic forces, the more energetic molecules pass on some of their energy to their less energetic neighbors.

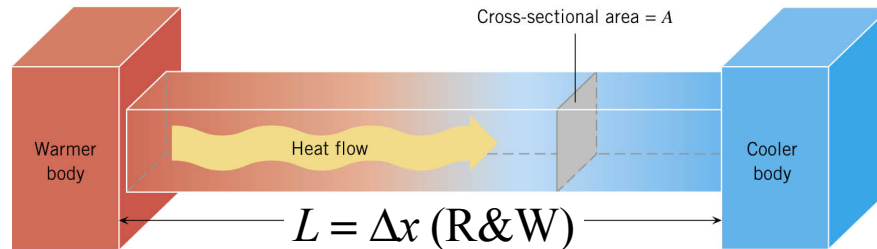


Model of solid materials.
Atoms connected by atomic
spring-like forces.

Materials that conduct heat well are called ***thermal conductors***, and those that conduct heat poorly are called ***thermal insulators***.

13.4 Conduction

CONDUCTION OF HEAT THROUGH A MATERIAL



The heat Q conducted during a time t through a bar of length L and cross-sectional area A is

$$Q = \frac{(kA\Delta T)t}{L}$$

k , is the thermal conductivity

SI Units of Thermal Conductivity:

$\text{J}/(\text{s} \cdot \text{m} \cdot ^\circ\text{C})$ (joule per second-meter- $^\circ\text{C}$)

$$H = \frac{Q}{t}$$

Thermal Conductivities^a of Selected Materials

Substance	Thermal Conductivity, k [$\text{J}/(\text{s} \cdot \text{m} \cdot ^\circ\text{C})$]
Metals	
Aluminum	240
Brass	110
Copper	390
Iron	79
Lead	35
Silver	420
Steel (stainless)	14
Gases	
Air	0.0256
Hydrogen (H_2)	0.180
Nitrogen (N_2)	0.0258
Oxygen (O_2)	0.0265
Other Materials	
Asbestos	0.090
Body fat	0.20
Concrete	1.1
Diamond	2450
Glass	0.80
Goose down	0.025
Ice (0°C)	2.2
Styrofoam	0.010
Water	0.60
Wood (oak)	0.15
Wool	0.040

^a Except as noted, the values pertain to temperatures near 20°C .

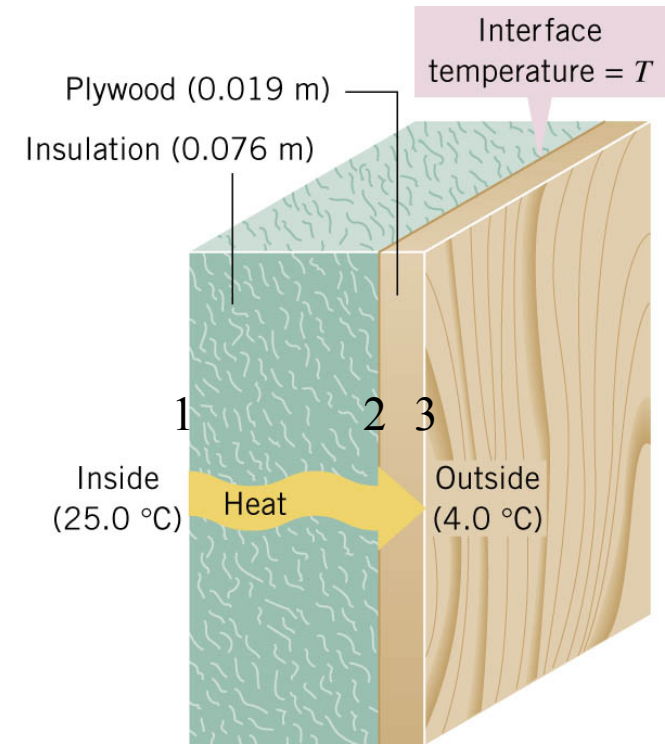
13.2 Conduction

Example Layered insulation

One wall of a house consists of plywood backed by insulation. The thermal conductivities of the insulation and plywood are, respectively, 0.030 and 0.080 J/(s·m·C°), and the area of the wall is 35m².

Find the amount of heat conducted through the wall in one hour.

Note: Heat passing through insulation is the same heat passing through plywood.



$$Q_{\text{insulation}} = Q_{12}; \quad Q_{\text{plywood}} = Q_{23}$$

$$T_1 = 25\text{C}^\circ, T_3 = 4\text{C}^\circ, T_2 \text{ is unknown}$$

First solve for the interface temperature using:

$$\begin{aligned} Q_{12} &= Q_{23} \\ T_2 &= 5.8\text{C}^\circ \\ \Delta T_{12} &= (25 - 5.8)\text{C}^\circ = 19.2\text{C}^\circ \end{aligned}$$

$$\begin{aligned} Q_{12} &= \frac{(k_{12} A \Delta T_{12}) t}{L_{12}} = \frac{.03(35)(19.2)3600}{.076} \text{ J} \\ &= 9.5 \times 10^5 \text{ J} \end{aligned}$$

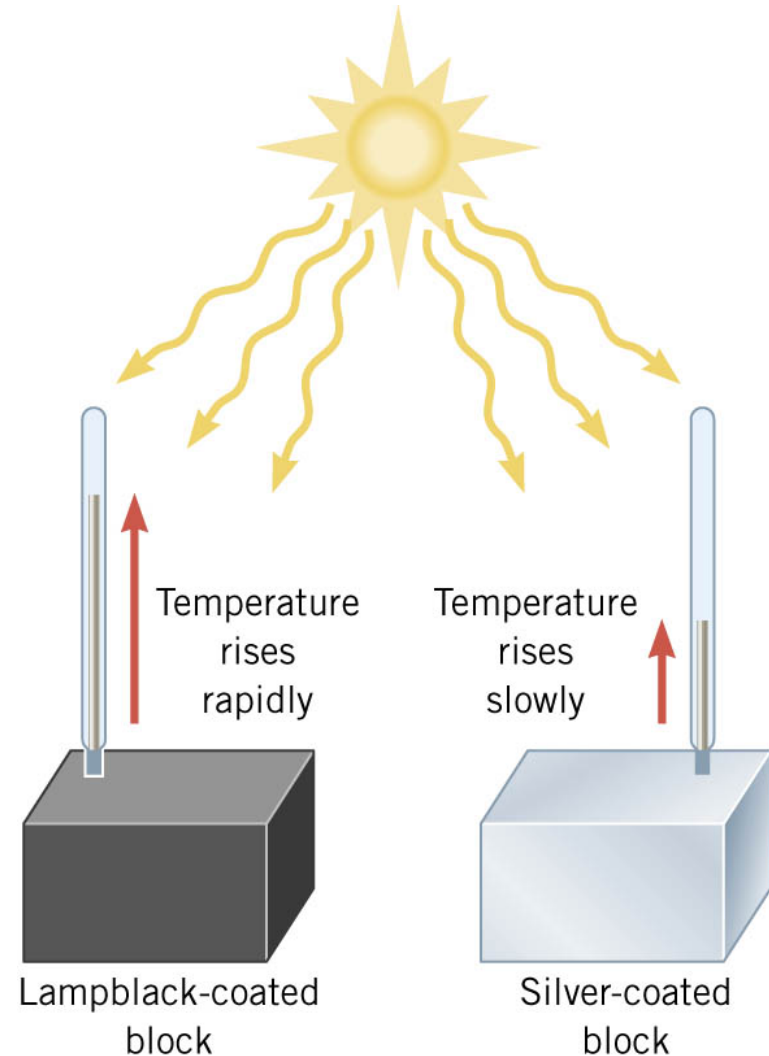
13.3 Radiation

RADIATION

Radiation is the process in which energy is transferred by means of electromagnetic waves.

A material that is a good absorber is also a good emitter.

A material that absorbs completely is called a ***perfect blackbody***.



13.3 Radiation

THE STEFAN-BOLTZMANN LAW OF RADIATION

The radiant energy Q , emitted in a time t by an object that has a Kelvin temperature T , a surface area A , and an emissivity e , is given by

$$Q = e\sigma T^4 At$$

emissivity e = constant between 0 to 1
 $e = 1$ (perfect black body emitter)

Stefan-Boltzmann constant
 $\sigma = 5.67 \times 10^{-8} \text{ J}/(\text{s} \cdot \text{m}^2 \cdot \text{K}^4)$

Example A Supergiant Star

The supergiant star Betelgeuse has a surface temperature of about 2900 K and emits a power of approximately $4 \times 10^{30} \text{ W}$. Assuming Betelgeuse is a perfect emitter and spherical, find its radius.

$$\text{power, } P = \frac{Q}{t}$$

with $A = 4\pi r^2$ (surface area of sphere with radius r)

$$\begin{aligned} r &= \sqrt{\frac{Q/t}{4\pi e\sigma T^4}} = \sqrt{\frac{4 \times 10^{30} \text{ W}}{4\pi(1)[5.67 \times 10^{-8} \text{ J}/(\text{s} \cdot \text{m}^2 \cdot \text{K}^4)](2900 \text{ K})^4}} \\ &= 3 \times 10^{11} \text{ m} \end{aligned}$$