

H. Assignment #9 Problem 9-1

In[1284]:= Show[Import["9-1.png", "png"], ImageSize -> 640]

Homework Assignment 9

9-1 (a) Plot $\frac{dP}{ds}$ versus θ , for $\beta = 0$,
0.5, and 0.9, if \vec{u} is parallel to \vec{v} .

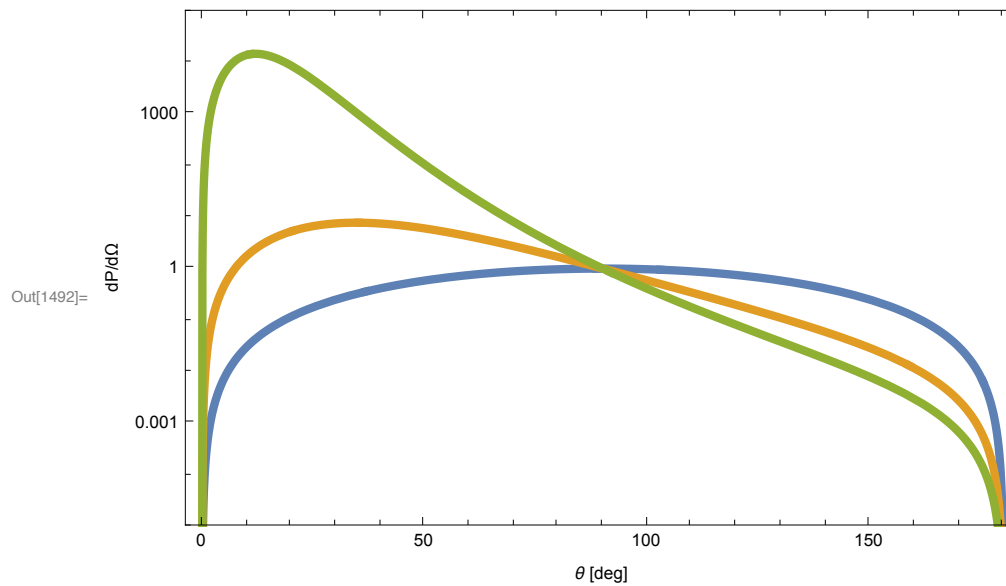
(b) Plot $\frac{dP}{ds}$ versus θ , for $\phi = 0$, for
 $\beta = 0, 0.5, \text{ and } 0.9$, if \vec{u} is perpendicular to \vec{v} .

Out[1284]=

Part (a); use EQ (11.161)

```
In[1489]:= Remove[β, α, f, f1]
f = Sin[θ]^2 / (1 - β * Cos[θ])^6
f1[β_, α_] = f /. {θ → α / 180 * Pi};
LogPlot[{f1[0, α], f1[0.5, α], f1[0.9, α]}, {α, 0, 180},
PlotRange → {All, {1*^-5, 1*^5}}, Frame → True,
FrameLabel → {"θ [deg]", "dP/dΩ"},
PlotStyle → Thickness[0.01], ImageSize → 480]
```

Out[1490]=
$$\frac{\text{Sin}[\theta]^2}{(1 - \beta \text{Cos}[\theta])^6}$$

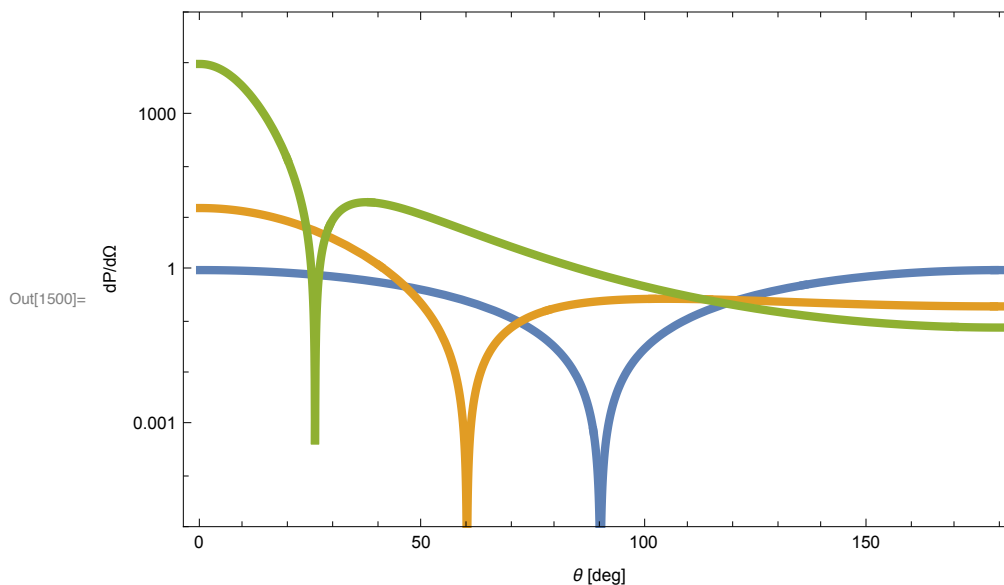


Part (b); use EQ (11.168) with $\phi = 0$

```
In[1497]:= Remove[β, α, g, g1]
g = ( (1 - β * Cos[θ]) ^ 2 - (1 - β ^ 2) * Sin[θ] ^ 2 ) *
  Power[1 - β * Cos[θ], -6]
g1[β_, α_] = g /. {θ → α / 180 * Pi};
LogPlot[{g1[0, α], g1[0.5, α], g1[0.9, α]}, {α, 0, 180},
  PlotRange → {All, {1*^-5, 1*^5}}, Frame → True,
  FrameLabel → {"θ [deg]", "dP/dΩ"},
  PlotStyle → Thickness[0.01], ImageSize → 480]
```

```
Out[1498]= 
$$\frac{(1 - \beta \cos[\theta])^2 - (1 - \beta^2) \sin[\theta]^2}{(1 - \beta \cos[\theta])^6}$$

```

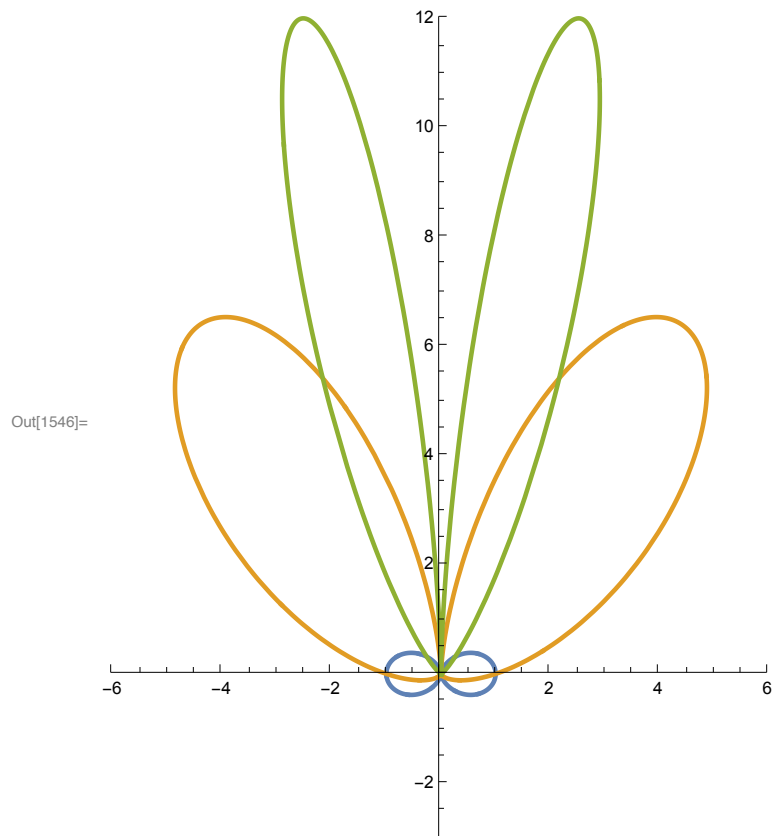


Polar plots

```
(* a parallel v *)
r[β_, α_] = f1[β, α]
ParametricPlot[
  {{r[0., α] * Sin[α / 180 * Pi], r[0., α] * Cos[α / 180 * Pi]},
   {r[0.5, α] * Sin[α / 180 * Pi], r[0.5, α] * Cos[α / 180 * Pi]},
   {r[0.9, α] / 1200 * Sin[α / 180 * Pi], r[0.9, α] / 1200 * Cos[α / 180 * Pi]}},
  {α, 0, 360}, PlotStyle → Thickness[0.007],
  PlotRange → {{-6, 6}, {-3, 12}}, AspectRatio → 15 / 12]
```

Out[1545]=

$$\frac{\sin\left[\frac{\pi\alpha}{180}\right]^2}{\left(1 - \beta \cos\left[\frac{\pi\alpha}{180}\right]\right)^6}$$



```
In[1549]:= (* a perp v *)
r[β_, α_] = g1[β, α]
ParametricPlot[
  {{r[0., α] * Sin[α / 180 * Pi], r[0., α] * Cos[α / 180 * Pi]},
   {r[0.5, α] / 5 * Sin[α / 180 * Pi], r[0.5, α] / 5 * Cos[α / 180 * Pi]},
   {r[0.9, α] / 1000 * Sin[α / 180 * Pi], r[0.9, α] / 1000 * Cos[α / 180 * Pi]}},
  {α, 0, 360}, PlotStyle → Thickness[0.007],
  PlotRange → {{-2, 2}, {-3, 12}}, AspectRatio → 1]
```

Out[1549]=

$$\frac{(1 - \beta \cos[\frac{\pi \alpha}{180}])^2 - (1 - \beta^2) \sin[\frac{\pi \alpha}{180}]^2}{(1 - \beta \cos[\frac{\pi \alpha}{180}])^6}$$

Out[1550]=

