

Homework Assignment #4 = magnetostatics  
 due Monday Sept 30 [ ANNOUNCEMENT: NO CLASS FRIDAY SEPT 27]

To aid in grading, for each problem draw a box around your final answers using red pencil.

- 4-1. A doughnut-shaped soft iron ring (radii  $a$  and  $R \gg a$ ) with a small gap has a toroidal winding ( $N$  turns with current  $I$ ). Assume the permeability is  $3000 \mu_0$ . Calculate  $\vec{B}$  and  $\vec{H}$  in the iron and in the air gap. You may make reasonable approximations.
- 4-2. (A) A long straight wire (radius  $a$  and length  $L \gg a$  and permeability  $\mu$ ) is placed in a uniform magnetic field  $\vec{B}_0$  perpendicular to the wire. Calculate the magnetic induction inside the wire.
- (B) Two long straight parallel wires ( one copper and one iron ) carry small equal currents  $I$  in a uniform magnetic field  $\vec{B}_0$  perpendicular to the wires. The wires are far apart. Compare the strengths of the forces on the wires, numerically and accurately.
- 4.3. Prove: If two magnetic media are separated by a planar interface, then the angles between the normal to the interface and the B-fields on either side obey  $\mu_2 \tan\theta_1 = \mu_1 \tan\theta_2$ .
- 4-4. A straight wire in air, carrying current  $I$ , is parallel to a planar boundary of a medium with permeability  $\mu$ , at distance  $d$  from the plane. The permeability of the medium is  $\mu$ .
- (A) Assume  $\mu = \infty$  (ferromagnetic material). Find an image current that produces the correct B-field in the air.
- (B) Assume  $\mu = 0$  (superconductor). Find an image current that produces the correct B-field in the air.
- 4-5. Why is a superconductor a perfect diamagnet?
- 4-6. Calculate the diamagnetic susceptibility of neon at STP. Use this theoretical model: assume the 8 outer electrons travel on circular orbits with mean radius  $R = 0.4 \times 10^{-10}$  m.
- 4-7. Jackson Problem 5-21.
- 4-8. The figure shows two identical permanent magnets. Calculate the force on either magnet. HINT: You will need elliptic integral functions.

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