

Physics 472 - 2020

Quantum Mechanics

Quiz 2

Your name:

Consider a smooth function $f(\phi)$ of the azimuthal angle ϕ . Find $\exp(-i\epsilon\hat{L}_z/\hbar)f(\phi)$ ¹

¹for experts in the theory of complex variables: assume that the radius of convergence of $f(\phi)$ for the considered ϕ exceeds ϵ

Your name:

Extra problem

Consider a particle of mass m in a two-dimensional potential box. The potential is

$$U(x, y) = 0 \quad \text{for } x^2 + y^2 < R^2, \quad U(x, y) \rightarrow \infty \quad \text{for } x^2 + y^2 > R^2$$

The Hamiltonian is $H = \frac{1}{2m}(p_x^2 + p_y^2) + U(x, y)$.
Estimate the energy of the lowest eigenstate.