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### Nothing Ain't What It Used to Be

### **Featured Event**

This event has been specially chosen by the Science Festival planning team! Here's what they have to say about it:



### **Nothing Ain't What It Used to Be**

Saturday, April 8th, 12:00-12:45 PM and 2:00-2:45 PM

### Biomedical and Physical Sciences Building, Room 1420

A little bit of nothing goes a long, long way since, these days, nothing is really something. In fact, our understanding of nothing has changed in just the last few years in particle physics and in cosmology.

How do we know nothing? Well, since 2010, 7,000 of us have been peering into

nothing at the CERN Large Hadron Collider in Geneva, Switzerland. We dug around in spacetime and reached an important conclusion about  $-$  wait for it  $-$  nothing!

At the same time, since 1998 hundreds of astronomers have been looking deep into the cosmos and they found...nothing as well! The nothing that we found at CERN is called the Higgs Boson...that little bit of the vacuum that makes everything...something. The nothing that astronomers uncovered is called Dark Energy, possibly the bang in the Big Bang.

Nothing is a very strange place and in this presentation, we'll talk about it.

Type: Talk or Demonstration

### Description:

A little bit of nothing goes a long, long way, since, these days, nothing is really something. In fact, our understanding of nothing has changed in just the last few years in particle physics and in cosmology. How do

### **Times and Locations**

Date/Time: 4/8/2017 12:00 - 12:45 PM

Location: Biomedical and Physical Sciences Building, Room 1420 **III** View on MSU Campus Map

Date/Time: 4/8/2017 2:00 - 2:45 PM

Location: Biomedical and Physical Sciences Building, Room 1420 **III** View on MSU Campus Map

Ages: All Ages

**Scientific Disciplines:** 

• Physics or Astronomy



# **hi**

## Lecture 24, 04.06.2017

Quantum Mechanics 4

2

# **housekeeping**

Question about anything?

*I'll make a movie for you:* 

Poster selection:

*April 13, outline due April 20…read the instructions.*  Homework:

*For month of April, I've shifted due dates to Saturdays.*





# **a problem**

with my website as I've described in Facebook.

*It's still unavailable from a university computer* 

*It is available everywhere else* 

This week you should be reading:

*The Theory of Everything, Chapters 4 and 5 Physics, Concepts & Connections, Chapter 13* 



# **Honors Project**

Data due April 22. Paper due on May 4 (final day).

Read the Second of two sets of instructions:

MinervaInstructions2\_2017.pdf in

[www.pa.msu.edu/~brock/file\\_sharing/QSandBB/2017homework/honors\\_project\\_2017/](http://www.pa.msu.edu/~brock/file_sharing/QSandBB/2017homework/honors_project_2017/)

# **Quantum Mechanics, so far:**

Light has both wave and particle-like properties

### Bohr Model:

electrons are in atomic orbits

fixed in radius and energy

electrons make transitions - spectra

### Electrons have both wave and particle-like properties

for both light and electrons,  $\,p=$ *h*  $\lambda$ 

standing wave patterns at Bohr radii worked

### Electrons are represented by imaginary wavefunctions, *ψ*

the square of the wavefunctions represent the probability of finding an electron at a point at a time

### Heisenberg Uncertainty Principle:

measuring a precision location of a quantum makes momentum imprecise

measuring a precision time interval of a quantum makes energy imprecise



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## **slice through the probability density of Hydrogen** Square these:







### **there is**

NO WAY to beat it in any of these measurement scenarios the inverse relation between p and λ messes with you every time  $p =$ *h*  $\lambda$ 

### **but here's the hard part**

the inability to determine position or momentum to arbitrary precision

is not about poor instruments

It. Is. About. Nature.

### **Heisenberg Uncertainty Relation** relation alert:

refers to:

example:

objects to not possess precise same time.

# $\Delta x \Delta p \geq h$  &  $\Delta t \Delta E \geq h$ an inherent property of Nature position and precise velocity at the

# 1932 Nobel

### 31 years old

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**Werner Karl** Heisenberg

The Nobel Prize in Physics 1932 was awarde creation of quantum mechanics, the applicat discovery of the allotropic forms of hydrogen

Werner Heisenberg received his Nobel Prize selection process in 1932, the Nobel Commit the year's nominations met the criteria as out According to the Nobel Foundation's statutes be reserved until the following year, and this Heisenberg therefore received his Nobel Priz

Photos: Copyright @ The Nobel Foundation

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a classical particle (dot) and its wavefunction

the contract of the contract o<br>The contract of the contract o

Heisenberg Uncertainty Relation at work again



all of the wave combinations means all of the momenta contribute: an spread in p.

called "wavepackets"

### the wave combinations localize the state...with some spread in  $x$



different momenta **waves of different wavelengths?**

### **The Schroedinger Equation is precisely, predictive**

There is no ambiguity in how the quantum field evolves the only measurable is its probabilistic feature... Is the quantum field function - the wavefunction - real? I don't know. It cannot be observed…so moot. Does it work as a description of Nature?

**absolutely...to exquisite precision**

# **Nature's little joke**

is encapsulated in a famous Feynman-description

a Gedankenexperiment...



Like the "classical" situation of asking what is the probability of getting heads or tails in a coin flip...you'd add 0.5 and 0.5.

## Two slit experiment with classical baseballs

 $P_A(D) + P_B(D) = P_{A+B}(D)$ 



## **two slit experiment**  $2 + 1$  ways

**MARKARAN** 

## Two slit experiment with waves





# $P_A(D) + P_B(D) \neq P_{A+B}(D)$

Interference causes the characteristic diffraction pattern



## Two slit experiment with **electrons?**





**Maybe not a surprise** *given what's come*  before, eh?

### A B **D** bang bang bang bang bang bang<br>Bang bang bang

# $P_A(D) + P_B(D) \neq P_{A+B}(D)$

Interference causes the characteristic diffraction pattern

# for waves.





### probabilities don't add

it's the **quantum fields** that do the wavy-ness!



 $P_A(D) + P_B(D) \neq P_{A+B}(D)$ 

**D**

 $P_D = |\psi_A + \psi_B|$ 





### which gap did any electron come through?

okay... let's trick it

rig an alarm that sounds when an electron goes through a slit.





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## Two slit experiment with **electrons** and an alarm?

Interference has gone away!!



So the sequence "S-A-A\*-D occurred. Every time  $A^*$  rings - red curve.  $B^*$  rings, blue curve.

## Same result as for baseballs.

Now:  $A^*$  is a DISTINGUISHABLE event from  $B^*$ 

We specified the path...

and that changed the reality.





## **summarize**

### the classical situations

For macroscopic objects: outcomes add "normally": The result of whatgoesthroughA and whatgoesthroughB is the sum of whatgoesthrough(A or B) *one or the other*

For **waves**: outcomes interfere: the result of whatgoesthroughA and whatgoesthroughB is the interference of whatgoesthrough(A and B) *both at the same time* the waves interfere





# **where is the electron**

it's real only when you make a measurement

> 22 As soon as measurement is made...the superposition goes away and the potentiality becomes the actuality...according to the probabilistic prediction of the Schroedinger Equation.

### The electron is real at the screen. it's unambiguously...there. the "bang" is a measurement

and your measurement can determine how it's real



what about here?

We have to say that an electron:

- goes through both slits
- and is in a "superposition" state, *here of both the state*  $\psi_A$  and the state  $\psi_B$

*}*

### **what we can say is real**

is now very tricky

and not understood.

We know that quantum fields contain all of their potentialities

and a measurement "collapses" them into just one outcome

the concept of a "measurement" is totally not understood.



**the wavefunctions are everywhere**

### spread out and overlapping

that's how molecules stay together

but...jeez. everywhere.



doesn't go to zero.

There's a probability that the electron in one of your water molecules might spend a brief time at the Louvre

# A B

Something big...seems to have a definite trajectory Something tiny...doesn't.





## **the wavefunctions are everywhere**

### They're waves, after all.

### make a measurement....there

 $|\psi|$ the electron is there with probability

Feynman's picture was one of particles: which take all possible paths

We can calculate the wavefunction at any point, very precisely...it's completely deterministic

The trajectory of a big object?

### **Overwhelmingly probable quantum likelihood: the classical path**



### **Only then is it real.**





 $\psi$ 

 $\psi$ 

 $\psi$ 

 $\psi$ 

 $\psi$ 

 $\psi$ 

 $\psi$ 

## **so where is a quantum**

before it's measured?

anywhere? everywhere?

yeah.



### **to take it to an absurd conclusion: the dreaded Schroedinger's Cat**

proposed by Schroedinger as an absurdity

*because he too had become disgusted with this own creation - he switched to biology!*

Imagine: a radioactive source, Geiger counter, and a glass bottle of a deadly poison with a cat in a box, a weight drops on the glass, breaking it after the first radioactive decay? ...dead cat.



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Now imagine that the radioactive nucleus as a **half life of 10 sec**. 

so, after 10 s, *50-50 chance that it has decayed* 

Set it all up...wait for 10 seconds. what is the state of the cat? alive or dead? *or both?*

# **"Copenhagen Interpretation"**

### It is meaningless *to speak of reality without a measurement*

Entities have no definite reality *the cat is neither alive nor dead or it is both* 

To know you must open the box *make a measurement*



### **this is how we have to think about it:**

before measurement: alive-dead state **superposition state of both**

after measurement: is **either** alive **or** dead

## **here's our house**

just before painting last year

need to pick a color:

**SHERWIN-WILLIAMS.** *quantum paint*





*my wife says "red"* 



*I say "blue"* 



## **I expect it to be:**

### purple

### mixing red and blue





## **but the quantum mechanical paint**

that I paid extra for?

can't "exist" in a superposition, mixed state.

Only one state.

*sometimes it's red*





## **but the quantum mechanical paint**

### that I paid extra for?

*sometimes it's blue*





### **it's never the mixture**

that it potentially might be

one or the other

More red paint?

not redder...just red more often







### the cat is either alive or dead, not both.

## $\epsilon$ Richard Feynman I think I can safely say that nobody understands quantum mechanics.

But we can calculate with Quantum Mechanics very, very well.

We're all highly skilled Quantum Mechanics





**electrons are little magnets**

They behave in a magnetic field as if they are little spinning current spheres

The electron itself is like a spinning charge...

Electrons have an **intrinsic** angular momentum, "S": "spin"

But, the "spin" can only take on two values:



$$
S_z = m_s \frac{h}{2\pi}
$$

$$
m_s=+\frac{1}{2}\quad \text{ or }\quad m_s=-\frac{1}{2}
$$

We say "spin, plus  $1/2$ " or "spin up" and "spin, minus  $1/2$ " or "spin down"



### **The electron is NOT**

- a ball of spinning charge
- its outer edges would have to move >> c

This is a quantum mechanical feature with no classical analog

# **Pauli Exclusion Principle:** No two electrons can be in the same quantum state that is, have identical "quantum numbers" ...integers that characterize the atom









# **Carbon... 6 electrons, 6 protons, 6 neutrons:**









The Pauli Exclusion Principle

Explains it

& SPIN is the reason

"1s2 2p2 2p6 3s2 3p6..."



### **How come Carbon is like:**

N

 $\mathsf{F}$ 

The Pauli Exclusion Principle still works ...since spin up  $\neq$  spin down, so different quantum states

 $e$ 

e

P

P

The combination of Schroedinger, Pauli, Uhlenbeck 42 and Goudsmit - explained the Periodic Table





 

## nalf-integer spin retical work on the numbers of Fermions

neutron

 

## ct with integer spin th Bose, who worked **ultiple** boson

s Boson



symbol: charge: mass: spin: category: **electron**

*e*  –1*e me* ≠ 9.0 × 10<sup>-31</sup> kg ~ 0.0005 p 1/2 fermion, lepton

### spin is a defining quality of an electron





## 27 kg = 1 p

symbol: charge: mass: spin: category: particle: **photon** 

*γ* 0  $m'_\psi = 0$ 1 

### again, an inherent angular momentum and a defining property of photons

### boson, aka Intermediate Vector Boson

# **shifting gears**

antimatter



# here's a number:

 $\overline{0}$ 



### zero

### the # of successfully combined models of

**Quantum Mechanics and Relativity** 

prior to 1928

**remember the relativistic energy relationship**

and compare it to the nonrelativistic one

$$
E = \frac{1}{2}mv^2
$$

 $p = mv$  $v =$ *p m*

## **Relativistic**

 $E^2 = (m_0 c^2)^2 + (pc)^2$ 

that square is problematic since it suggests:

translated to Schroedinger QM: **negative energies for freely moving electrons**

 $(pc)^2$ 

$$
E = \pm \sqrt{(m_0 c^2)^2 +}
$$

### **Classical**

# negative energies for unbound systems a disaster

### any additional E is kinetic

F

 $m_0c^2$ 

 $\overline{0}$ 

## **negative energies for unbound systems**

a disaster

## negative energies for unbound systems

a disaster

# there's no bottom!

### **worse!**

Quantum Mechanics using Relativity: required not only negative energies negative probabilities!

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# **1928**



### Paul Dirac

At the question period after a Dirac lecture at the University of Toronto, somebody in the audience remarked: "Professor Dirac, I do not understand how you derived the formula on the top left side of the blackboard." "This is not a question," snapped Dirac, "it is a statement." CATAL AND

hilarious interview with the Wisconsin State Journal from 1929 on the blog.

### 1902 – 1984





# **Dirac's Mathematical Imagination**

Dirac embraced the negative energy

positive electric charge **– Energy**

*ψ*

Dirac set out to find an equation that would solve both problems

**imagination** 

The "Dirac Equation" is the correct equation for electrons: Probabilities turn out okay, but required interpretation of negative energies

*ψ*

Solved the negative probability

*ψ*

*ψ*



negative electric charge

### **Dirac's result**

required: 4 quantum fields, rather than 1  $\psi$  (μt  $E$ )  $\psi$  (HdE)  $\psi$  (+E) 2 have positive energy, 2 have negative energy

each pair is related precisely to spin

Dirac showed that spin is a wholly relativistic effect ...it just popped out of his equation.

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*ψ(–E), ψ(–E) ψup(–E), ψdown(–E)*

# **still negative energies?**

positive energy

"solved" it with Pauli's Exclusion Principle

> negative energy

 $mc<sup>2</sup>$ 

His vacuum is full of negative energy electrons



*–mc*<sup>2</sup>





0

# start with nothing

 $E_{\gamma} > 2 m_e c^2$ 



 $\begin{array}{c} \n + \n \end{array}$ 







and in cosmology



### **what is this?**

 $\psi(-E)$  a positively charged object with negative energy?

### At first, he thought: "proton"

nah. A bolder idea: an anti-electron. The Positron.



## modern intepretat

### a photon poof-disappears







**The antimatter story has a happy ending:**

1932









# **Cosmic Rays** very high energy protons from space

# **Carl Anderson**

clever...put in a lead plate to cause particles to lose energy

## Right on schedule: 1932





**B** field in



### sharper curvature at top

"antiparticle"

### symbol: charge: mass: spin: category: anti-electron, aka "positron" *e* or *e+* +1*e*  $m_e$  = 9.0 × 10<sup>-31</sup> kg ~ 0.0005 p *1/2*  anti-fermion, anti-lepton

# the bar over the top will mean

# **antimatter**

### is a fact of life

### every particle has it's anti-particle partner

same mass, different electrical charge

# Dirac Nobel

### at the age of 31

### 





 $\overline{\mathsf{N}}$ 

No<br>Me

N

N

P

N

 $\overline{\mathsf{N}}$ 

 $\frac{N}{N}$ 





# Carl Anderson and Victor Hess

### Anderson was 31

### **<sup></sub>**Mobelprize.org</sup>

The Official Web Site of the Nobel Prize

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The Nobel Prize in Physics 1936

Victor F. Hess

Carl D. Anderson



**Victor Franz Hess** 

The Nobel Prize in Physics 19: "for his discovery of cosmic ray

