

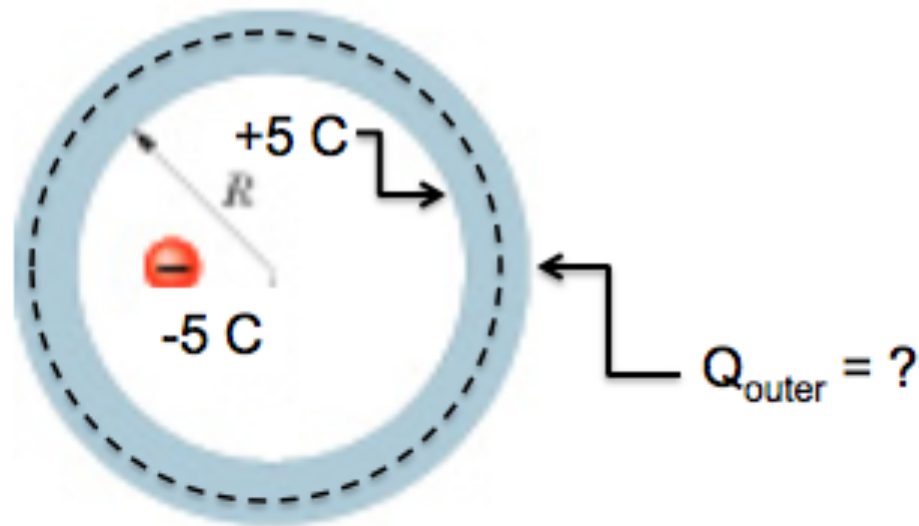
PHY294H

- Professor: Joey Huston
- email: huston@msu.edu
- office: BPS3230
- Homework will be with Mastering Physics (and an average of 1 hand-written problem per week)
 - ◆ **2nd MP assignment due Wed Jan. 27; second hand-written problem (27.51) as well**
 - ◆ **Added problem 28.68 for 3rd MP assignment due Wed Feb. 3 as a hand-in problem**
 - ◆ **Help-room hours: 12:40-2:40 Tues; 3:00-4:00 PM Friday**
- Quizzes by iclicker (sometimes hand-written)
- Course website: www.pa.msu.edu/~huston/phy294h/index.html
 - ◆ lectures will be posted frequently, mostly every day if I can remember to do so

iClicker question

A point charge of -5.0 C is off-center inside an electrically **neutral** spherical metal shell. What is the induced charge on the **outer surface** of the shell?

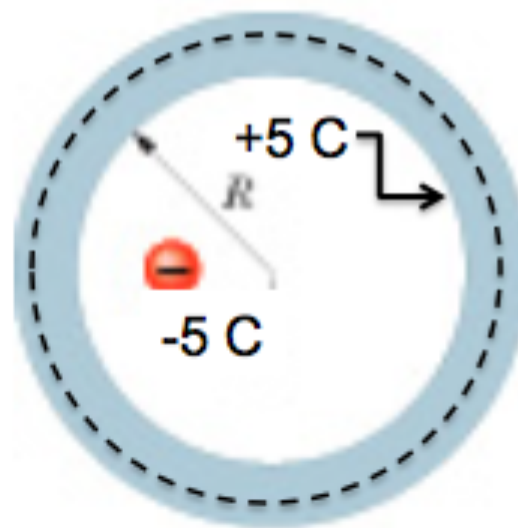
- A. 0 C
- B. $+5\text{ C}$
- C. -5 C
- D. $+10\text{ C}$
- E. -10 C



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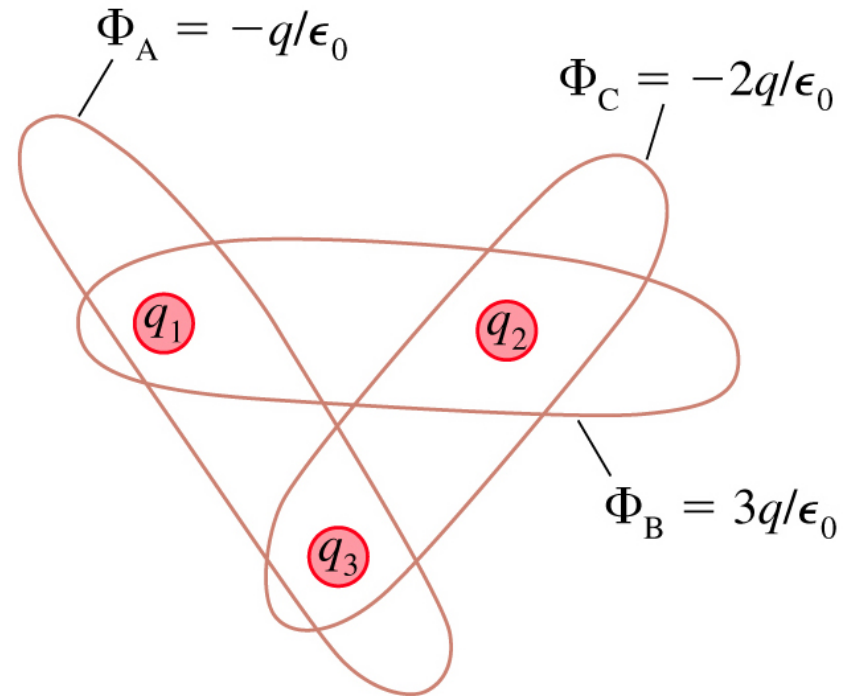


The shell is electrically neutral.

$Q_{\text{outer}} = ?$

Problem

- Given the fluxes through the Gaussian surfaces, what are the values of the charges q_1 , q_2 and q_3 ?



Step back: how well do we know Gauss' and Coulomb's law

- Gauss' law is equivalent to Coulomb's law only because Coulomb's law is an inverse square law
- How well is Coulomb's law/ Gauss' law known?
- Joseph Priestly knew that there is no gravitational field within a spherically symmetric mass distribution and speculated that a similar behavior of the gravitational and electric force laws would explain a charged cork ball placed inside the a charged metal container is not attracted to the walls of the container
 - ◆ this effect was first seen by Benjamin Franklin who told Priestly
- This is related to the styrofoam chips in the aluminum container on top of the van de Graf not feeling any electric field

Deviations from inverse square law

- John Robison did experimental tests in 1769 of the distance behavior of the forces between charges
- Robison expressed the uncertainties in his result as a deviation from Coulomb's law

◆ $F \propto 1/r^{2+\delta}$

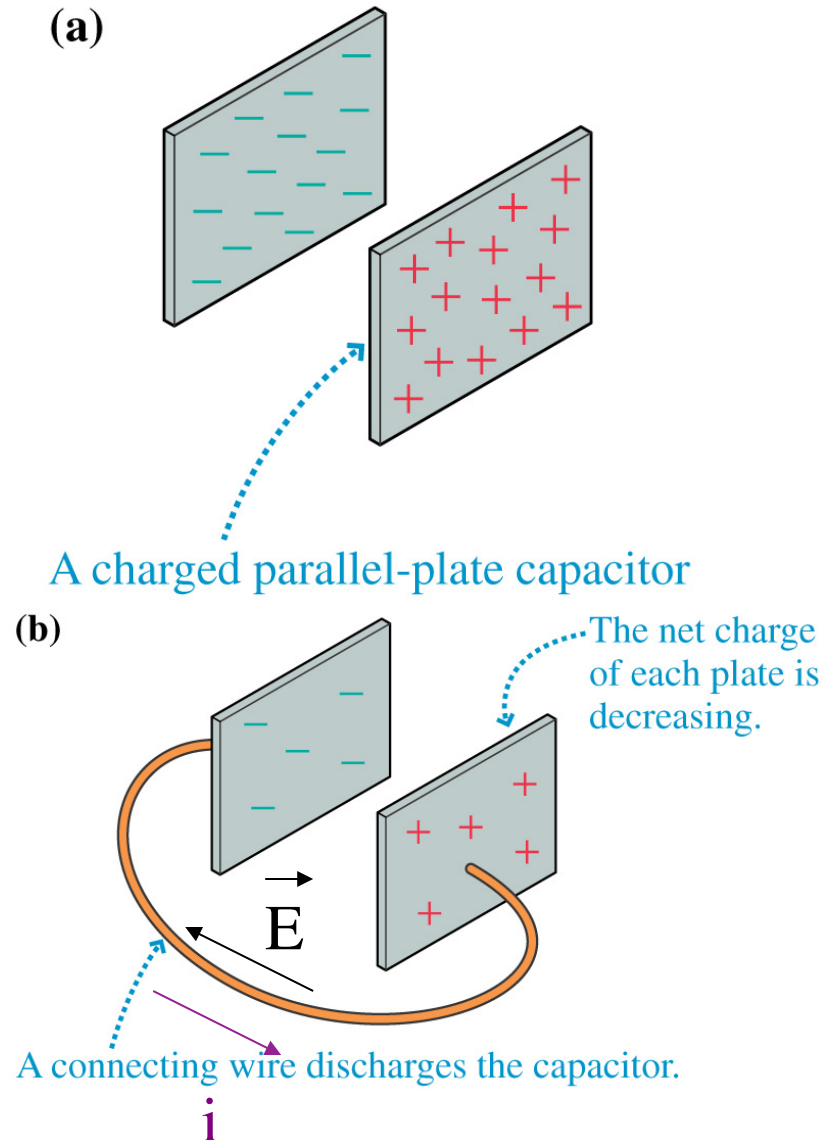
Constraints on δ have improved

Investigator	Date	Maximum δ
Robison	1769	0.06
Cavendish	1773	0.02
Coulomb	1785	0.10
Maxwell	1873	5×10^{-5}
Plimpton and Lawler	1936	2×10^{-9}
Williams, Fowler and Hill	1971	3×10^{-16}

Now verified to better than 1 part per billion from atomic scale to galactic scale.

Creating an electrical current

- Suppose I have a parallel plate capacitor in which I have equal and opposite charges on two separated plates
- If I connect the two plates by a conductor, then I know that the excess electrons will flow from the negative plate to the positive plate
- That would constitute an electrical current
- Why are the electrons moving from to the + plate?
 - ◆ there's an electric field in the conducting wire
 - ◆ the electric field provides the electrons with their motivation to move in a particular direction...but not very fast
- ...and now for something completely different



Next chapter: Electric potential

- We've discussed the similarities before between the force between two charges and the force between two masses

$$\vec{F} = \frac{q_1 q_2}{r^2} \hat{r}$$

$$\vec{F} = -G \frac{m_1 m_2}{r^2} \hat{r}$$

- Any force that is a function of position only is a conservative force which means that we can associate a potential energy with it

- ◆ $E_{\text{mech}} = K + U$

- ◆ $\Delta E_{\text{mech}} = \Delta K + \Delta U$

- $K = \sum K_i = \sum \frac{1}{2} m_i v_i^2$
 - ◆ sum of all kinetic energies in problem

- U = interaction energy of the system = potential energy

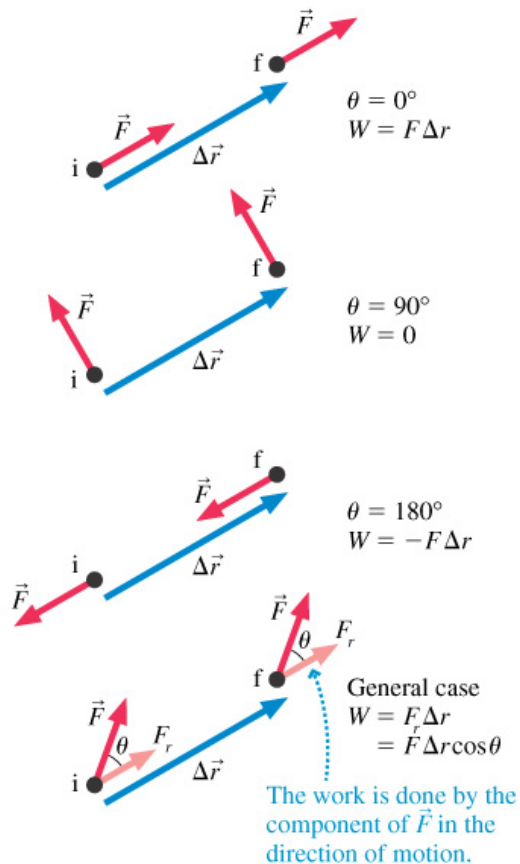
- Most often talk about change in potential energy due to work performed by conservative force

- ◆ $\Delta U = U_f - U_i = -W_{\text{force}}$

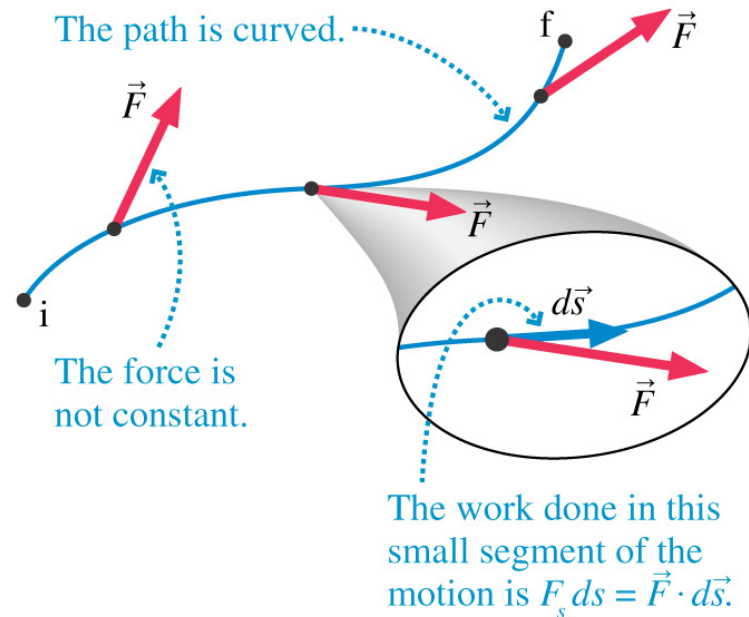
Work

- Work that a constant force does is

◆ $W = \vec{F} \cdot \vec{\Delta r} = F \Delta r \cos \theta$



- If \vec{F} or $\Delta \vec{r}$ is not constant, then have to integrate $\vec{F} \cdot d\vec{s}$ over the path travelled



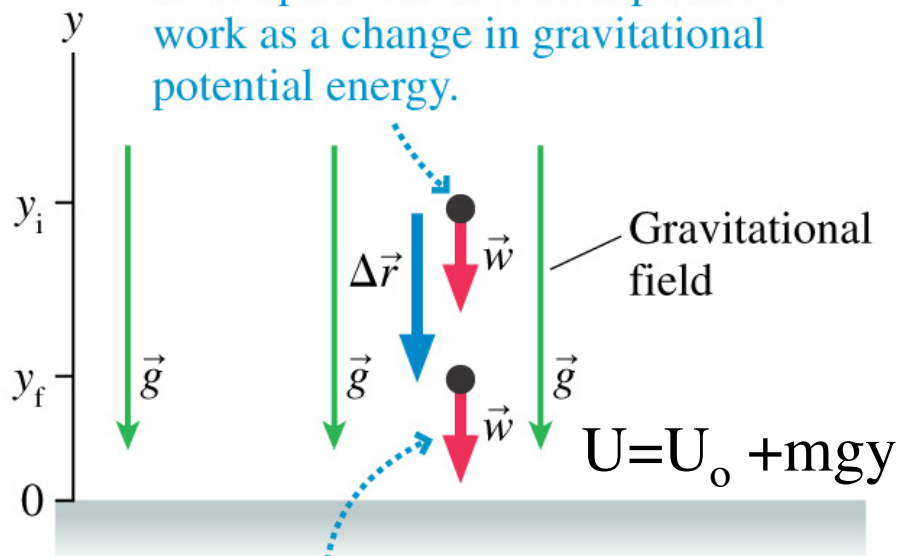
...for a conservative force, the work performed is independent of the path

Uniform fields

- $W_{\text{grav}} = mg \Delta r \cos 0^\circ = mgy_i - mgy_f$

- $\Delta U_{\text{grav}} = U_f - U_i = -W_{\text{grav}} = mgy_f - mgy_i$

The gravitational field does work on the particle. We can express the work as a change in gravitational potential energy.

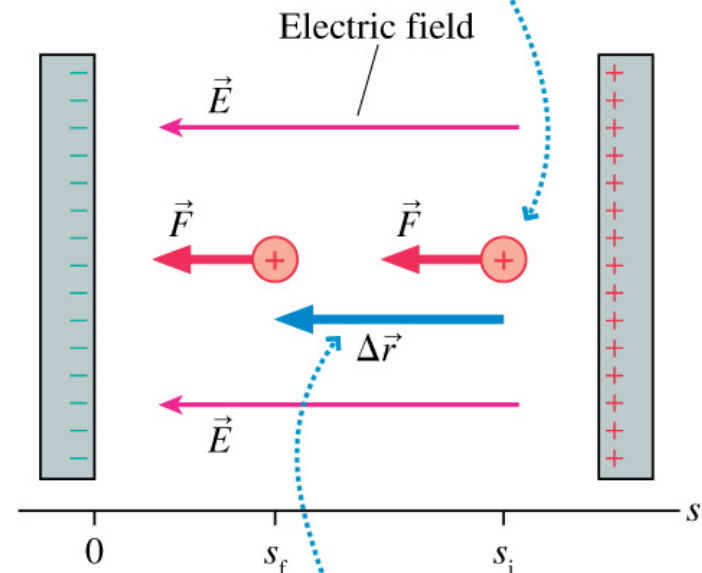


The net force on the particle is down. It gains kinetic energy (i.e., speeds up) as it loses potential energy.

- $W_{\text{elec}} = F \Delta r \cos 0^\circ = qEs_i - qEs_f$

- $\Delta U_{\text{elec}} = U_f - U_i = -W_{\text{elec}} = qEs_f - qEs_i$

The electric field does work on the particle. We can express the work as a change in electric potential energy.



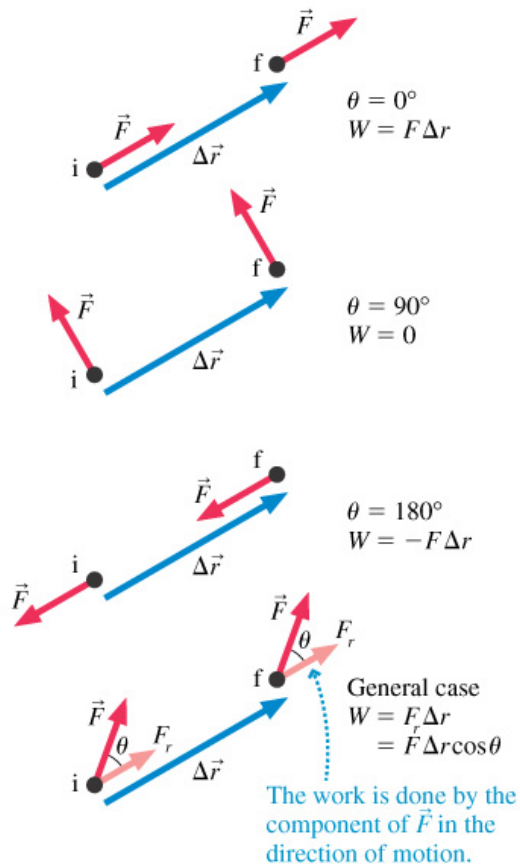
The particle is "falling" in the direction of \vec{E} .

$$U_{\text{elec}} = U_o + qEs$$

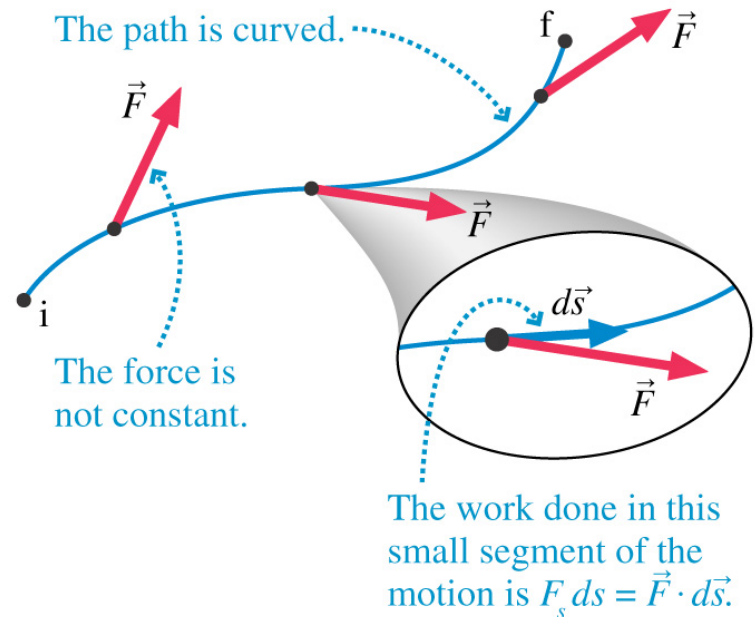
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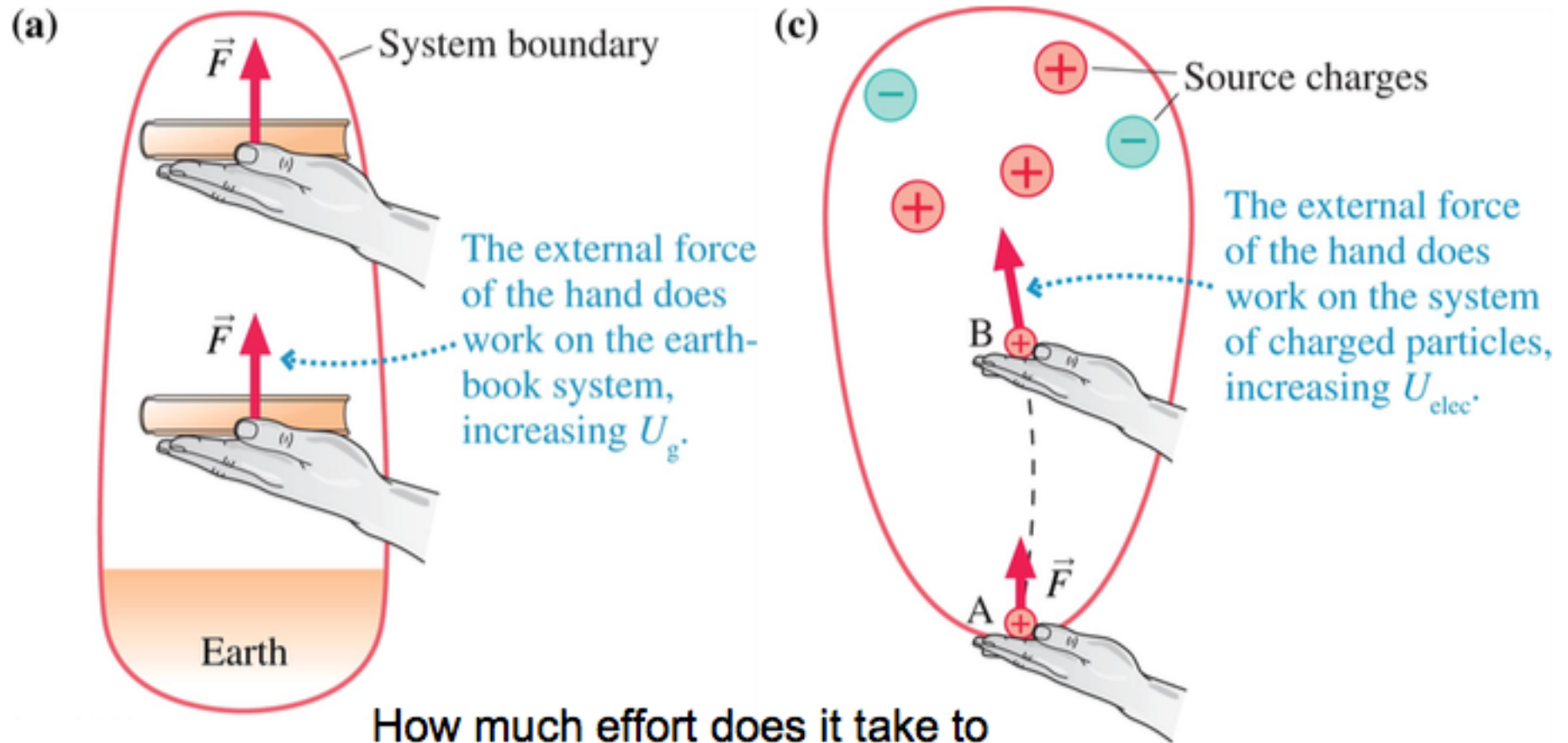


- If \vec{F} or $\Delta \vec{r}$ is not constant, then have to integrate $\vec{F} \cdot d\vec{s}$ over the path travelled



...for a conservative force, the work performed is independent of the path

Potential energy

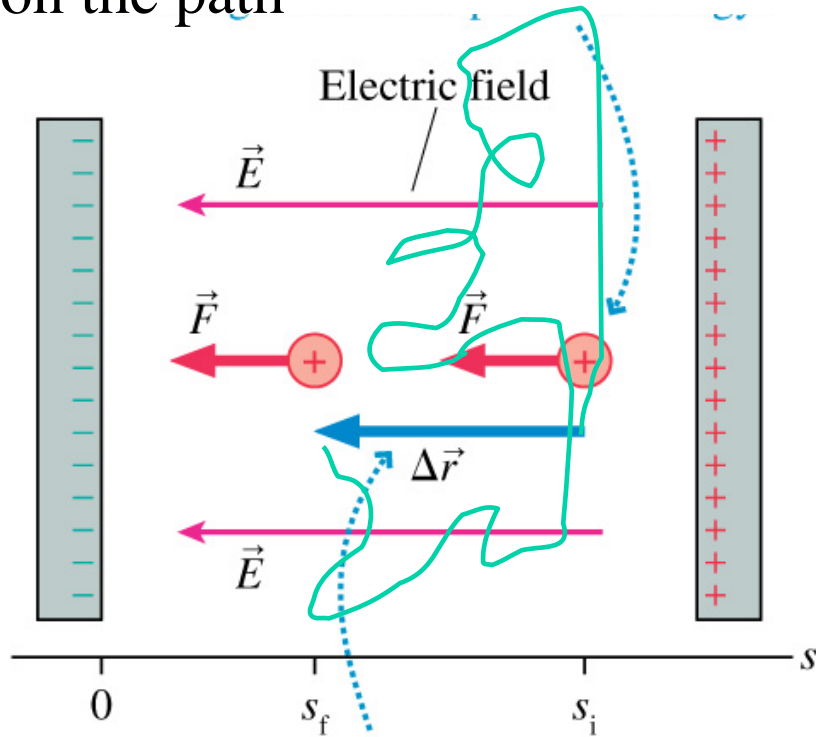


How much effort does it take to move the charge from A to B?

Hard (repulsive): U increases,
Easy (attractive): U decreases

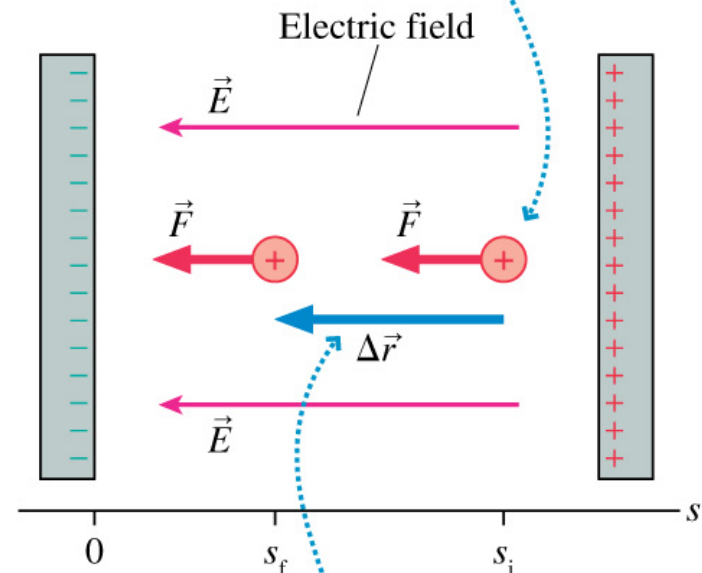
Uniform fields

Note that the work done by the E field, and thus the change in potential energy does not depend on the path



- $W_{\text{elec}} = F \Delta r \cos 0^\circ$
 $= qEs_i - qEs_f$
- $\Delta U_{\text{elec}} = U_f - U_i = -W_{\text{elec}}$
 $= qEs_f - qEs_i$

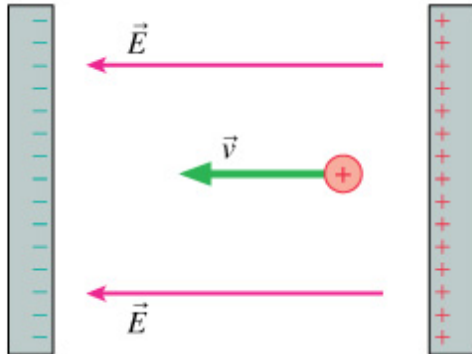
The electric field does work on the particle. We can express the work as a change in electric potential energy.



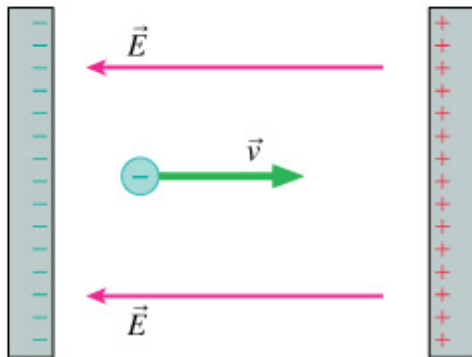
The particle is "falling" in the direction of \vec{E} .

$$U_{\text{elec}} = U_o + qEs$$

Uniform fields



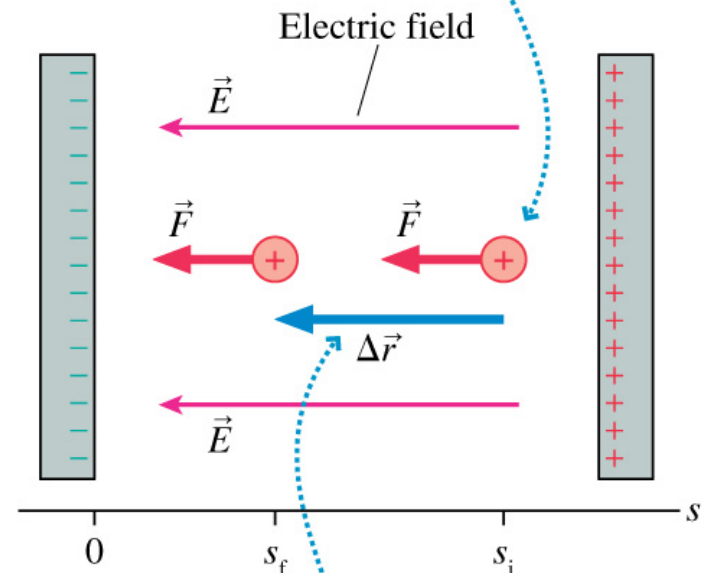
The potential energy of a positive charge decreases in the direction of \vec{E} . The charge gains kinetic energy as it moves toward the negative plate.



The potential energy of a negative charge decreases in the direction opposite to \vec{E} . The charge gains kinetic energy as it moves away from the negative plate.

- $W_{\text{elec}} = F \Delta r \cos 0^\circ$
 $= qEs_i - qEs_f$
- $\Delta U_{\text{elec}} = U_f - U_i = -W_{\text{elec}}$
 $= qEs_f - qEs_i$

The electric field does work on the particle. We can express the work as a change in electric potential energy.

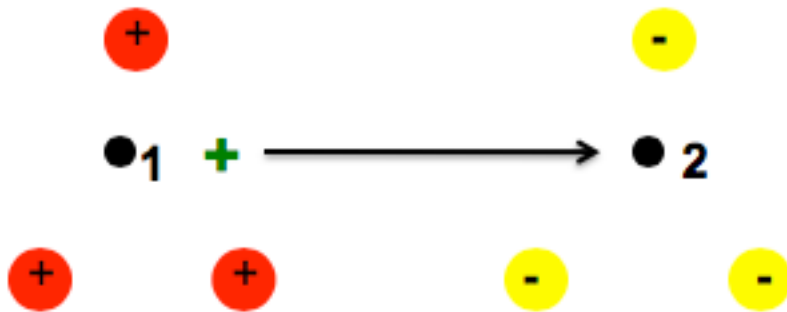


The particle is "falling" in the direction of \vec{E} .

$$U_{\text{elec}} = U_o + qEs$$

iclicker question

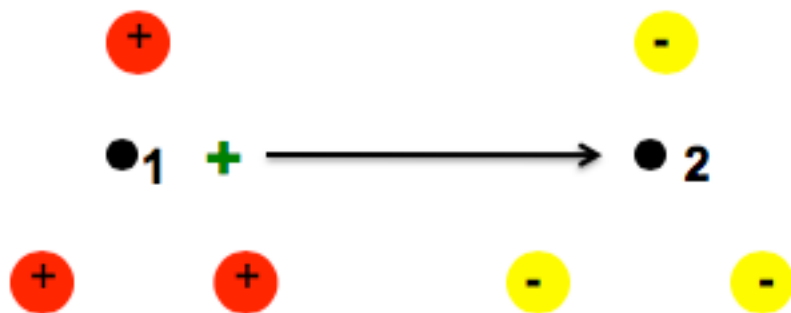
As you move a positive (+) charge from point 1 to point 2 its electric potential energy (U)



- A. Decreases
- B. Increases
- C. Stays the same
- D. Not enough info

iclicker question

As you move a positive (+) charge from point 1 to point 2 its electric potential energy (U)



- A. Decreases
- B. Increases
- C. Stays the same
- D. Not enough info

Potential energy of point charges

- First, let me calculate the work done by charge 1 on charge 2 while charge 2 moves from point x_1 to point x_2

$$W_{elec} = \int_{x_1}^{x_2} \vec{F}_{1on2} \cdot d\vec{x}$$

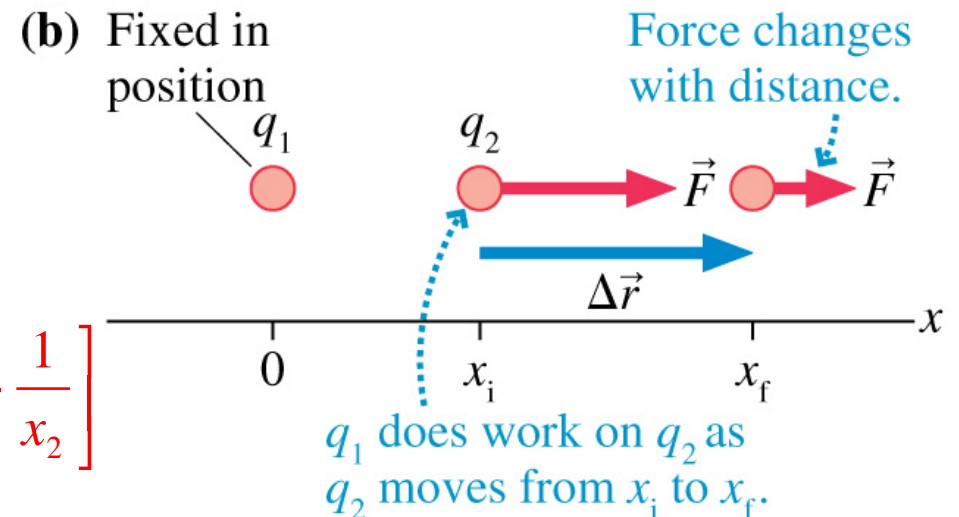
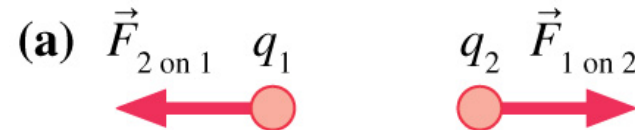
$$W_{elec} = \frac{q_1 q_2}{4\pi\epsilon_o} \int_{x_1}^{x_2} \frac{1}{x^2} dx$$

$$W_{elec} = \frac{q_1 q_2}{4\pi\epsilon_o} \left(-\frac{1}{x} \right)_{x_1}^{x_2} = \frac{q_1 q_2}{4\pi\epsilon_o} \left[\frac{1}{x_1} - \frac{1}{x_2} \right]$$

$$\Delta U_{elec} = U_f - U_i = -W_{i \rightarrow f} = \frac{q_1 q_2}{4\pi\epsilon_o} \left[\frac{1}{x_2} - \frac{1}{x_1} \right]$$

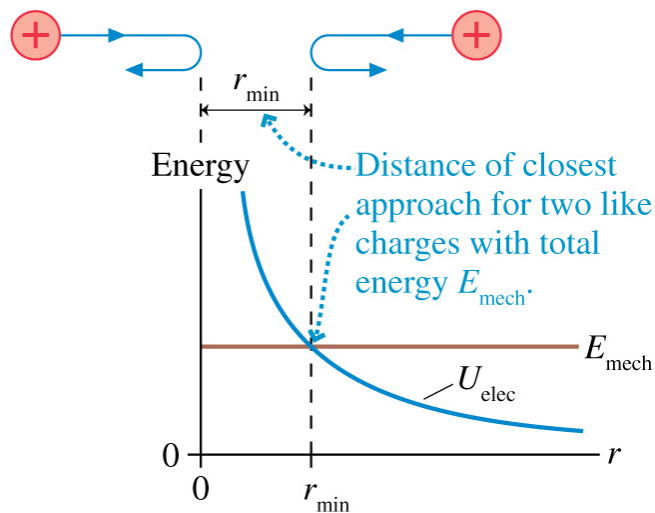
use r instead of x . Set $U_{inf}=0$

$$U_{elec} = \frac{Kq_1 q_2}{r} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r} \quad (\text{two point charges})$$

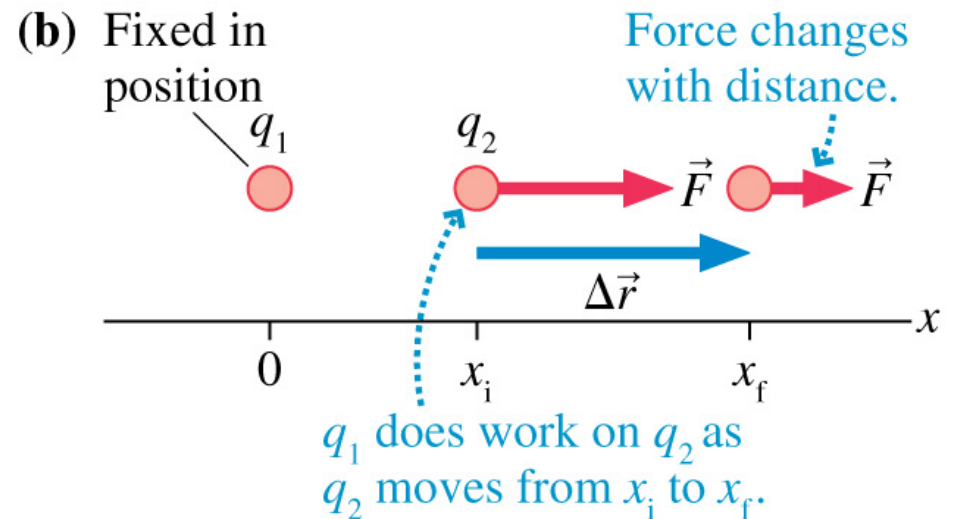
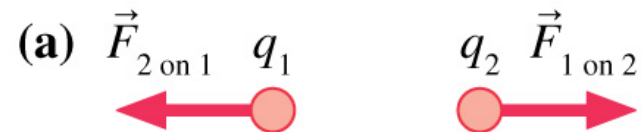
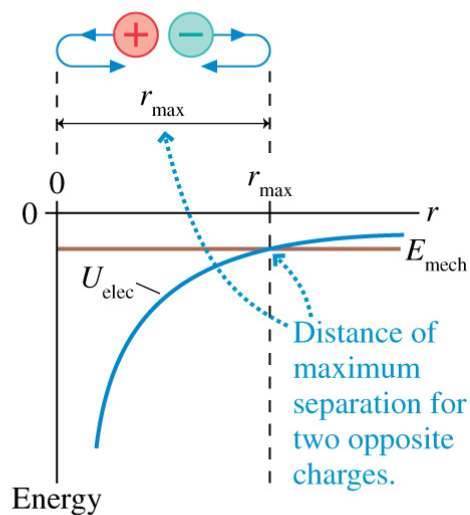


Potential energy of point charges

(a) Like charges



(b) Opposite charges



$$U_{\text{elec}} = \frac{Kq_1q_2}{r} = \frac{1}{4\pi\epsilon_0} \frac{q_1q_2}{r} \quad (\text{two point charges})$$

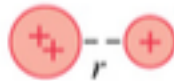
Note that the potential energy between any two point charges is zero at infinite separation

iclicker question

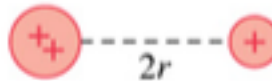
Rank in order, from largest to smallest, the potential energies U_a to U_d of these 4 pairs of charges. Each + symbol represents the same amount of charge.



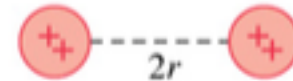
(a)



(b)



(c)



(d)

$$U_{elec} = \frac{Kq_1q_2}{r}$$

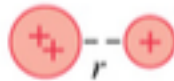
- A. $U_a = U_b > U_c = U_d$
- B. $U_b = U_d > U_a = U_c$
- C. $U_a = U_c > U_b = U_d$
- D. $U_d > U_c > U_b > U_a$
- E. $U_d > U_b = U_c > U_a$

iclicker question

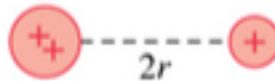
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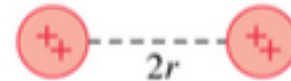
(a)



(b)



(c)



(d)

$$U_{elec} = \frac{Kq_1q_2}{r}$$

A. $U_a = U_b > U_c = U_d$

B. $U_b = U_d > U_a = U_c$

C. $U_a = U_c > U_b = U_d$

D. $U_d > U_c > U_b > U_a$

E. $U_d > U_b = U_c > U_a$