QCD and the Strong Force

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for the QCD conveners
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QCD plays a major role in basically every physics process under discussion in this workshop.

When we talk about precision physics, or discovery physics, we need to understand the role of QCD corrections.

Thus, we have an overlap, and hopefully a synergy, with every physics group in this workshop.

For example, part of our session tonight will be jointly with the EWK group, given the interplay between QCD and EWK corrections for precision measurements.
The charge for the QCD group (like every other group) is to determine the
1. current state of the art
2. what is likely/priority for the next 5 years?
3. what is likely/priority for longer time scale (20 years)?

Of course a) is the easiest, b) is less so and parts of c) are in the realm of pure speculation

We have broken down each question into a series of more definite sub-issues that should be addressed. For each issue, we include a discussion of the current status and outlook, some possible projects, and overlap/synergy with the other physics groups.
Question 1a

- What are the prospects for future higher order calculations at NLO and matched with parton showers? What subtleties remain to be understood for precision measurements?

- Techniques in calculation of pQCD cross sections have reached the point where any reasonable cross section can be calculated in a finite time. The current limit is 2->6 (W+5 jets, ttbar with decays).

- Many existing calculations can also be recycled; 4 jet cross section has been used to calculate photon+3 jets and diphoton+2 jets

- See extra slides
Question 1a

- There remain open questions as to the best scale choice (and uncertainty) for complex multi-parton calculations, since a variety of physical scales may appear in the calculation.
- There are now attempts, such as MINLO, to choose nodal scales (plus appropriate Sudakov factors) in NLO multi-parton calculations that may shed light on this issue.

Projects
- collate cross section predictions where a choice of an optimal scale and range of uncertainty is not obvious (example: tTbB)
- study effect of application of MINLO procedure to these (and other) calculations
- where does this uncertainty cause problems for experimenters?
There have also been great advances in the inclusion of NLO multi-parton matrix elements in parton shower Monte Carlos, in a semi-automatic manner.

We expect that any future NLO calculation can be straightforwardly implemented in a parton shower Monte Carlo.

There have also been developments in addition of NLO parton states of different multiplicities, without double- or under-counting, in such a manner that theoretical final states can be generated similar to what is measured in the data, i.e. an inclusive Higgs sample where the 1 and 2 jet final states are described at NLO, and higher multiplicities are described at LO.

Projects

- detailed comparisons of predictions from different approaches for combining NLO+PS (Powheg, MENLOPS, aMC@NLO) for key physical processes (such as inclusive jet production)
- compare multi-parton NLO PS predictions (MEPS@NLO for the moment) to fixed order predictions, to NLO PS predictions and to data
  - W+jets
  - Higgs+jets
Question 1b

- Once we have the NLO and NNLO calculations, how do we (experimentalists) use them?
- If a theoretical calculation is done, but it can not be used by any experimentalists, does it make a sound? Or create a citation?
- We need public programs and/or public ntuples
- Oftentimes, the program is too complex to be run by non-authors
- In that case, ROOT ntuples may be the best solution
  - see for example experience with Blackhat+Sherpa ntuples
- Computing and storage are an issue both for the authors of these programs and for the users
  - overlap with computing group

- Projects
  - study of B+S ntuple structure; questions of universality/possible improvements
Question 1c

- Survey of the importance of EWK corrections. Do we need an EWK wishlist similar to the now-defunct NLO QCD one?
- Where are combined QCD-EWK corrections important?
- Projects:
  - NLO (QCD+) EWK wishlist
  - Overlap
    - EWK group
- See for example the workshop on EWK Corrections to Hard QCD Processes at the IPPP at Durham (Sep 24-26)
- See http://www.ippp.dur.ac.uk/Workshops/12/EW_LHC
- See also www.pa.msu.edu/~huston/atlas/ippp_ewk_summary.pdf

example: azimuthal angle between tagging jets

\[
\frac{d^2\sigma}{d\phi_{34}} - 1 \% \quad pp \rightarrow H\bar{H} + X \quad \text{Ciccolini, Dittmaier, Krämer} \quad [\text{hep-ph/0306234}]
\]
Question 1d

- The frontier for NNLO is 2->2 processes
- What processes do we need calculated?
- What is the timescale?
- Projects:
  - NNLO wishlist (build on Les Houches wishlist; see extra slides)
  - To date, most NNLO calculations are 2->1 (W/Z/Higgs)
  - Multiple NNLO calculations containing colorless final states (diphoton production, W+Higgs production) have recently been completed
  - Several partonic channels contributing to tt at NNLO have been completed and full result is expected soon
  - Work is proceeding on dijets, W/Z+jet, Higgs+jet
Question 1e

- What are the prospects for including NNLO effects in a parton shower? To what extent are any physics analyses limited by the choice of either NLO+PS or NNLO?

- Are measurements constraining subtle effects (recoil strategies, etc) in parton showering and/or NLO+PS calculations?
  - a la the t\bar{t}bar symmetry at the Tevatron

- A program/technique including NNLO QCD matrix elements in a parton shower Monte Carlo will not be forthcoming in the near future, but in principle, there is nothing that prevents such a development.

- Note that the parton showers themselves are still at LL/NLL. What limitations does this result in?

- Projects
  - do we need a parton shower that is fully NLL?
  - what is needed in parton showering to fully model what is observed in the data?
Question 2a

- Can jet analyses be repeated with different (infra-red safe) jet algorithms and/or jet sizes?

- Both major LHC experiments are using the antikT algorithm (which is good) but different jet sizes (which is bad). Physics analyses can be automated to the extent that there is no reason not to carry them out with several jet sizes and/or several jet algorithms. Each algorithm/size may illustrate different aspects of the underlying physics.
Can jet substructure, in particular for boosted systems, be put to wider use in other physics analyses?

There has been a great deal of attention given to jet substructure, especially for boosted systems. These tools can also be put to use for most physics analyses, again to try to understand the underlying physics better.

Projects
- catalog general substructure tools/frameworks, a la FastJet or SpartyJet. What tools are missing?

Overlaps
- top, bsm, Higgs
Question 2c

- At what future luminosities might existing jet algorithms cease to be robust? What techniques may be introduced to stabilize them?

- The antikt algorithm, and the accompanying techniques, have worked well at the LHC, even with current luminosities resulting in >=30 additional events per crossing. Studies need to be carried out to see at what pileup rates, existing jet algorithms may cease to be robust, and better clustering techniques may need to be developed.

- Projects:
  - how do the existing jet substructure tools perform at high pileup rates (say nPU=100) and what kind of further developments may be necessary?

- Overlaps
  - top, BSM, Higgs
Can particle flow techniques be taken advantage of in future jet algorithms?

Both ATLAS and CMS have used particle flow techniques to improve the jet energy scale determination. Such techniques are considered as crucial for future linear collider experiments, and it may be that new jet algorithms can be developed to take advantage of the commensurate granular resolution inherent in such techniques.

Projects:
- how might jet reconstruction be improved given highly granular readout?
Question 2e

- Can event shapes such as jettiness be useful in future measurements, and should the experimental collaborations study their implementation at the LHC?

- There has already been some work by ATLAS and CMS, but this is an area that needs to be developed further

- Projects:
  - develop it further
Question 3a

- What impact will LHC data have on PDFs?
- Projects:
  - what is the ultimate precision/limitations of collider-only PDFs?
- There has been a great deal of work on understanding PDF predictions and uncertainties at the LHC, in particular by the PDF4LHC working group.
- The DIS data, including both HERA and fixed target are the dominant ‘deciders’ in global fits. Collider cross sections, however, are often directly sensitive to the gluon distribution in a way that DIS data is not. As the statistical and systematic errors improve, the use of LHC data in global fits will accelerate. It is crucial that correlated systematic error information be published for all of this data.
Question 3b

- How much better might an eLHC constrain PDFs? Is the improved precision necessary?

- Projects:
  - what physics processes need the PDF precision that such a machine could provide? Are new fixed target measurements necessary as well?

- The LHC probes PDFs in ranges outside of direct investigation possible in HERA. This will become even more true with higher running energies for the LHC, or a possible successor. An eLHC will serve to directly determine PDFs in this new kinematic regime.

- The information provided will be superior to that determined by the inclusion of collider data in the PDF fits, but it should be investigated how necessary that increased precision might be.
Question 3b+

- What are the prospects for improving the theoretical description of PDFs?
- How important is a good knowledge of the photon PDF?
- What does having a negative gluon imply?

- For example, including QED corrections in the evolution, or even moving beyond NNLO. (See Durham EWK workshop for discussion of QED effects in PDFs.)

- Projects:
  - evaluate importance of QED/EWK corrections for PDFs.

- Overlap
  - EWK group
Question 3c

- What are the prospects for improved measurements of $\alpha_s$ at the LHC and future colliders?

- Measuring $\alpha_s$, and its running, is one of the most fundamental of QCD tests.

- Projects:
  - what are the sensitivities of $\alpha_s$ measurements at the LHC and at future accelerators?
In what situations do we need better resummation techniques? Can we envisage future experimental measurements where severe phase space restrictions will be required?

Resummation techniques have greatly improved in recent years, for a variety of kinematic variables. What is needed, perhaps, is a catalog of situations where a better resummation formalism/technique is needed.

Projects:
- catalog of situations where improvements in resummation are needed.
Question 4b

- To what extent do current formalisms to resum large logarithms in jet-binned cross sections agree? Can we envisage more flexible resummation formalisms to handle more complicated observables?

- Projects:
  - catalog measurements where jet vetoing/binning might be necessary, and estimate the possible effects on the uncertainty

- Often it is necessary to apply jet vetoes/binning in a physics measurement, and thus in the corresponding theoretical QCD calculation. For example, the Higgs production process is known to NNLO, but the application of jet vetoes/binning can significantly increase the size of the uncertainty over that of the inclusive cross section.

- There are now techniques to resum the effects of the vetoes, but it is not clear how the current techniques can be applied to the complex phase space that results from the application of jet algorithms.

- See extra slides

- Overlaps: Higgs
Question 5

- Are there gaps in our understanding of diffractive and hard diffractive physics?

- There are two main directions: (1) diffraction and forward physics as a means to study unresolved issues of QCD and to search for and to investigate any manifestations of new physics and (2) diffraction as a way to study soft physics.

- For (1): one can study Higgs and BSM physics with forward proton tagging. This can serve as a spin-parity analyser/filter, allow for the measurement of the Higgs branching ratio into bottom quark pairs, and allow tests of CP violation in the Higgs sector. For heavier Higgs, it will also be possible to measure the Higgs width. One can also study the spin-parity assignments for any new quarkonium-type states.
Projects:

- how well can we predict/measure processes such as diffractive Higgs production? How does the photon-photon flux in a pp machine compare to that in a future linear collider? For what future physics topics would such measurements be useful?

Overlaps

- Higgs

At the LHC, and any future high energy colliders, there will be a large photon-photon flux, which can be used to produce a number of final states, including WW production, and light charginos. (See Durham EWK workshop.)

For (2): one can continue the study of the violation of factorization for diffractive scattering at ep and pp machines, measure dijet properties for a sample of pure gluon jets, and in general study hard diffractive production of a number of final states.
Question 6

- How hampered are we by our limited understanding of non-perturbative physics?

- Projects:
  - understand sensitivity of top mass definition to non-perturbative effects

- This includes both effects such as jet fragmentation as well as the multiple parton interactions that make up the bulk of the underlying event. Another issue is the definition of kinematic quantities that have been treated in a classical sense to date, but for which increased precision requires a better theoretical basis; perhaps foremost among these is the measurement of the top mass to both the current precision and to the improved precision that will be possible with further LHC running and at future machines.
Many of these issues have been addressed in the Les Houches workshops which have taken place since 1999

- witness the many Les Houches accords
- the next workshop will be before the Minneapolis meeting (June 3-23 2013)

We will try to coordinate some of the common work between the two
Evening session

- **7:30-9:00 West Wing WH10W**
  - last half-hour with EWK group
  - ReadyTalk: 9343617 Passcode: 7907
  - Evo: Universe CPM2012-Energy Frontier HE5-QCD

- See also pQCD computing session 1:15 PM
  - Nu’s Room WH12X
Extra slides
Les Houches NLO wishlist, started in 2005, and incremented in 2007 and 2009 was officially closed in 2011, since all of the calculations on the list were complete, and there are no technical impediments towards calculations of new final states, either with dedicated or semi-automatic calculations.

Note that dedicated calculations can be factors of 10 faster than semi-automatic calculations.
Last to be calculated

● …the authors
ROOT ntuples

- More complex to use than MCFM
  - no manual for example
  - and you don’t produce the events yourself
- ntuples produced separately by Blackhat + Sherpa for
  - so TB’s of disk space
- No jet clustering has been performed; that’s up to the user
  - a difference from MCFM, where the program has to be re-run for each jet size/algorithm
- What algorithms/jet sizes that can be run depends on how the files were generated
  - i.e. whether the right counter-events are present
- For the files on the right at 7 TeV (for $W^+ + 3$ jets), one can use kT, antikT, siscone ($f=0.75$) for jet sizes of 0.4, 0.5, 0.6 and 0.7
- bornLO (stands alone for pure LO comparisons; not to be added with other contributions below)
  - 20 files, 5M events/file, 780 MB/file
- Born
  - 18 files, 5M events/file, 750 MB/file
- loop-lc (leading color loop corrections)
  - 398 files, 100K events/file, 19 MB/file
- loop-fmlc (needed for full color loop corrections)
  - 399 files, 15K events/file, 3 MB/file
- real (real emission terms)
  - 169 files, 2.5 M event/file, 5 GB/file
- vsub (subtraction terms)
  - 18 files, 10M events/file, 2.8 GB/file
For jet clustering, we use SpartyJet, and store the jet results in SJ ntuples and they tend to be big since we store the results for multiple jet algorithms/sizes.

Then we friend the Blackhat +Sherpa ntuples with the SpartyJet ntuples producing analysis ntuples (histograms with cuts) for each of the event categories.

Add all event category histograms together to get the plots of relevant physical observables.

http://projects.hepforge.org/spartyjet/
arXiv:1201.3617 (manual)

SpartyJet is a set of software tools for jet finding and analysis, built around the FastJet library of jet algorithms. SpartyJet provides four key extensions to FastJet: a simple Python interface to most FastJet features, a powerful framework for building up modular analyses, extensive input file handling capabilities, and a graphical browser for viewing analysis output and creating new on-the-fly analyses.
Reweighting

can reweight each event to new

- PDF
- factorization scale
- renormalization scale
- $\alpha_s$ (tied to the relevant PDFs)

based on weights stored in ntuple (and linking with LHAPDF)

so, for example, the events were generated with CTEQ6, and were re-weighted to CTEQ6.6

2.1 Born and real contributions

The new weight is given by

$$w = \text{me\_wgt2} \cdot f(id1, x1, \mu_F)F(id2, x2, \mu_F)\frac{\alpha_s(\mu_R)^n}{(\text{alphas})^n}$$

(1)

with $\mu_F$ the new factorization scale, $\mu_R$ the new factorization scale, $f$ the new PDF, $\alpha_s$ the corresponding running coupling and $n$ the number of strong coupling (the number of jets $n_j$ for the born contribution and $n_j + 1$ for the real contribution). If the factorization scale is not changed, one can simplify the computation (and save the pdf function call):

$$w = \text{weight2} \frac{\alpha_s(\mu_R)^n}{(\text{alphas})^n}$$

(2)

2.2 Virtual contribution

The virtual contribution is treated like the real and born contribution, but the matrix element has a dependence on the renormalization scale parametrized using the additional weights $\text{usr\_wgts}$.

$$w = m \cdot f(id1, x1, \mu_F)F(id2, x2, \mu_F)\frac{\alpha_s(\mu_R)^n}{(\text{alphas})^n}$$

(3)

$$m = \text{me\_wgt2} + \text{usr\_wgts}[0] + \frac{p^2}{2} \text{usr\_wgts}[1]$$

(4)

$$l = \log\left(\frac{\mu_R^2}{\text{ren\_scale}^2}\right)$$

(5)
Reweighting, cont.

2.3 Integrated subtraction

The computation of the new weight for the integrated subtraction is the most complicated. The ROOT file has 16 additional weights to make this possible.

\[
w = m \frac{\alpha_s(\mu_R)^n}{(\text{alphas})^n} \quad (6)
\]

\[
m = \text{me_wgt2} \cdot f(\text{id1}, x1, \mu_F) f(\text{id2}, x2, \mu_F)
+ \left( f_a^1 \omega_1 + f_a^2 \omega_2 + f_a^3 \omega_3 + f_a^4 \omega_4 \right) F_b(x_b)
+ \left( F_b^1 \omega_5 + F_b^2 \omega_6 + F_b^3 \omega_7 + F_b^4 \omega_8 \right) f_a(x_a) \quad (7)
\]

\[
\omega_i = \text{usr_wgts}[i - 1] + \text{usr_wgts}[i + 7] \log \left( \frac{\mu_R^2}{\text{ren_scale}^2} \right) \quad (10)
\]

where

\[
f_a^1 = \begin{cases} 
  a = \text{quark} : & f_a(x_a, \mu_F) \\
  a = \text{gluon} : & \sum_{\text{quarks}} f_q(x_a, \mu_F) 
\end{cases} \quad (11)
\]

\[
f_a^2 = \begin{cases} 
  a = \text{quark} : & f_a(x_a/x'_a, \mu_F) \\
  a = \text{gluon} : & \sum_{\text{quarks}} f_q(x_a/x'_a, \mu_F/x_a) 
\end{cases} \quad (12)
\]

\[
f_a^3 = f_g(x_a, \mu_F) \quad (13)
\]

\[
f_a^4 = \frac{f_g(x_a/x'_a, \mu_F)}{x'_a} \quad (14)
\]

and \( n = n_j + 1 \).
PDF Errors

Better than what is done in MCFM (as far as disk space is concerned); PDF errors are generated on-the-fly through calls to LHAPDF. But then don’t store information for individual eigenvectors.

\[
\begin{align*}
\Delta X^+_{\text{max}} &= \sqrt{\sum_{i=1}^{N} [\max(X_i^+ - X_0, X_i^- - X_0, 0)]^2}, \\
\Delta X^-_{\text{max}} &= \sqrt{\sum_{i=1}^{N} [\max(X_0 - X_i^+, X_0 - X_i^-, 0)]^2}.
\end{align*}
\]
Branches in ntuple

<table>
<thead>
<tr>
<th>branch name</th>
<th>type</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>id</td>
<td>I</td>
<td>id of the event. Real events and their associated counterterms share the same id. This allows for the correct treatment of statistical errors.</td>
</tr>
<tr>
<td>nparticle</td>
<td>I</td>
<td>number of particles in the final state</td>
</tr>
<tr>
<td>px</td>
<td>F[nparticle]</td>
<td>array of the x components of the final state particles</td>
</tr>
<tr>
<td>py</td>
<td>F[nparticle]</td>
<td>array of the y components of the final state particles</td>
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<td>pz</td>
<td>F[nparticle]</td>
<td>array of the z components of the final state particles</td>
</tr>
<tr>
<td>E</td>
<td>F[nparticle]</td>
<td>array of the energy components of the final state particles</td>
</tr>
<tr>
<td>alphas</td>
<td>D</td>
<td>$\alpha_s$ value used for this event</td>
</tr>
<tr>
<td>kf</td>
<td>I</td>
<td>PDG codes of the final state particles</td>
</tr>
<tr>
<td>weight</td>
<td>D</td>
<td>weight of the event</td>
</tr>
<tr>
<td>weight2</td>
<td>D</td>
<td>weight of the event to be used to treat the statistical errors correctly in the real part</td>
</tr>
<tr>
<td>me_wgt</td>
<td>D</td>
<td>matrix element weight, the same as weight but without pdf factors</td>
</tr>
<tr>
<td>me_wgt2</td>
<td>D</td>
<td>matrix element weight, the same as weight2 but without pdf factors</td>
</tr>
<tr>
<td>x1</td>
<td>D</td>
<td>fraction of the hadron momentum carried by the first incoming parton</td>
</tr>
<tr>
<td>x2</td>
<td>D</td>
<td>fraction of the hadron momentum carried by the second incoming parton</td>
</tr>
<tr>
<td>x1p</td>
<td>D</td>
<td>second momentum fraction used in the integrated real part</td>
</tr>
<tr>
<td>x2p</td>
<td>D</td>
<td>second momentum fraction used in the integrated real part</td>
</tr>
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<td>fac_scale</td>
<td>D</td>
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<td>renormalization scale used</td>
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<td>nuwgt</td>
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<tr>
<td>usr_wgts</td>
<td>D[nuwgt]</td>
<td>additional weights needed to change the scale</td>
</tr>
</tbody>
</table>
What’s next for the Les Houches NLO wishlist?

- Nothing: I’m retiring the NLO wishlist
- It’s being replaced by a NNLO wishlist plus a wishlist for EW corrections for hard processes

Below we construct a table of calculations needed at the LHC, and which are feasible within the next few years. Certainly, results for inclusive cross sections at NNLO will be easier to achieve than differential distributions, but most groups are working towards a partonic Monte Carlo program capable of producing fully differential distributions for measured observables.

- $t\bar{t}$ production:
  needed for accurate background estimates, top mass measurement, top quark asymmetry (which is zero at tree level, so NLO is the leading non-vanishing order for this observable, and a discrepancy of theory predictions with Tevatron data needs to be understood). Several groups are already well on the way to complete NNLO results for $t\bar{t}$ production [84, 85, 86, 87].

- $W^+W^-$ production:
  important background to Higgs search. At the LHC, $gg \rightarrow WW$ is the dominant subprocess, but $gg \rightarrow WW$ is a loop-induced process, such that two loops need to be calculated to get a reliable estimate of the cross section. Advances towards the full two-loop result are reported in [88, 89].

- inclusive jet/dijet production:
  NNLO parton distribution function (PDF) fits are starting to become the norm for predictions and comparisons at the LHC. Paramount in these global fits is the use of inclusive jet production to tie down the behavior of the gluon distribution, especially at high $x$. However, while the other essential processes used in the global fitting are known to NNLO, the inclusive jet production cross section is only known at NLO. Thus, it is crucial for precision predictions for the LHC for the NNLO corrections for this process to be calculated, and to be available for inclusion in the global PDF fits. First results for the real-virtual and double real corrections to gluon scattering can be found in [90, 91].
NNLO wishlist: continued

- **V+1 jet production:**
  $W/Z/\gamma + \text{jet}$ production form the signal channels (and backgrounds) for many key physics processes, for both SM and BSM. In addition, they also serve as calibration tools for the jet energy scale and for the crucial understanding of the missing transverse energy resolution. The two-loop amplitudes for this process are known [92, 93], therefore it can be calculated once the parts involving unresolved real radiation are available.

- **V+$\gamma$ production:**
  Important signal/background processes for Higgs and New Physics searches. The two-loop helicity amplitudes for $q\bar{q} \rightarrow W^{\pm}\gamma$ and $q\bar{q} \rightarrow Z^0\gamma$ recently have become available [94].

- **Higgs+1 jet production:**
  As mentioned previously, events in many of the experimental Higgs analyses are separated by the number of additional jets accompanying the Higgs boson. In many searches, the Higgs + 0 jet and Higgs + 1 jet bins contribute approximately equally to the sensitivity. It is thus necessary to have the same theoretical accuracy for the Higgs + 1 jet cross section as already exists for the inclusive Higgs cross section, i.e. NNLO. The two-Loop QCD Corrections to the Helicity Amplitudes for $H \rightarrow 3$ partons are already available [95].
Jet vetos and scale dependence: WWjet

- Often, we cut on the presence of an extra jet
- This can have the impact of improving the signal to background ratio
  - ...and it may appear that the scale dependence is improved
- However, in the cases I know about, the scale dependence was anomalous at NLO without the jet veto, indicating the presence of unc cancelled logs
- The apparent improvement in scale dependence may be illusory

Figure 11: Comparison of WW+jet production cross sections in the LHC setup with $p_{T,jet} > 50\,\text{GeV}$ and for Tevatron with $p_{T,jet} > 20\,\text{GeV}$: The straight lines show the results calculated with the five-flavour PDFs of CTEQ6, the dashed lines those calculated with the four-flavour PDFs of MRST2004F4. Contributions from external bottom (anti-)quarks are omitted, as described in Section 2.2.
Consider tTbB

Here scale dependence looks ok at inclusive NLO.

Perturbative instability for small $p_{jet,veto}$

- veto $\Rightarrow$ negative contribution $-\alpha_s^5 \ln^2(Q_0/p_{jet,veto})$
- IR log dramatically enhances NLO uncertainty
- $p_{jet,veto} < 40$ GeV $\Rightarrow$ NLO-band enters $K < 0$ range
  NLO prediction completely unreliable!
Uncertainties in the face of jet vetos/bins

- For Higgs searches (with decays into WW*), important to divide sample into separate jet bins
  - backgrounds are different
  - physics is different (VBF shows up in 2 jet bin)
- If I calculate the scale uncertainties naively, I get the following
  - Common scale variation for jet bins, e.g. for the Tevatron
    \[
    \frac{\Delta \sigma}{\sigma} = \frac{66.5\% \times (66.5\%)}{28.6\% \times (28.6\%)} + 4.9\% \times (4.9\%) = (14\%)
    \]
    - 0 jets
    - 1 jet
    - \( \geq 2 \) jets
  - Smaller uncertainty in 0-jet bin than in inclusive cross section
- Note that fixed order expansion gets unstable at low \( p_T^{\text{veto}} \)
  - Sudakov double logs
    \[ \ln^2(p_T^{\text{cut}}/m_H) \]
Perturbative Structure of Jet Cross Sections

\[ \sigma_{\text{total}} = \int_{0}^{p_T^{\text{cut}}} dp_T \frac{d\sigma}{dp_T} + \int_{p_T^{\text{cut}}}^{\infty} dp_T \frac{d\sigma}{dp_T} \]

\[ \sigma_0(p_T^{\text{cut}}) + \sigma_{\geq 1}(p_T^{\text{cut}}) \]

\[ \sigma_{\text{total}} = 1 + \alpha_s + \alpha_s^2 + \cdots \]

\[ \sigma_{\geq 1}(p_T^{\text{cut}}) = \alpha_s(L^2 + L) + \alpha_s^2(L^4 + L^3 + L^2 + L) + \cdots \]

\[ \sigma_0(p_T^{\text{cut}}) = \sigma_{\text{total}} - \sigma_{\geq 1}(p_T^{\text{cut}}) \]

\[ = \left[ 1 + \alpha_s + \alpha_s^2 + \cdots \right] - \left[ \alpha_s(L^2 + L) + \alpha_s^2(L^4 + \cdots) + \cdots \right] \]

- Perturbative series in \( \sigma_{\text{total}} \) and \( \sigma_{\geq 1}(p_T^{\text{cut}}) \) have different structures and are unrelated.
- Apparent small uncertainties in \( \sigma_0(p_T^{\text{cut}}) \) arise from cancellation between two series with large corrections.

…should treat perturbation series for \( \sigma_{\geq 0\text{jets}}, \sigma_{\geq 1\text{ jet}}, \sigma_{\geq 2\text{jets}} \) as independent with uncorrelated systematic errors (i.e., add in quadrature)
Realistic Fixed-Order Scale Uncertainties

Using naive scale variation for $\sigma_0$

Using above procedure for $\sigma_0$

- Uncertainties reproduce naive scale variation at large cut values
- Larger uncertainties at small cut values → take into account presence of large logarithmic corrections

\[ E_{\text{cm}} = 7 \text{ TeV} \quad m_H = 165 \text{ GeV} \]

<table>
<thead>
<tr>
<th>$p_T^{\text{cut}}$ [GeV]</th>
<th>(\sigma(p_T^{\text{cut}})) [pb]</th>
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<tbody>
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\(\sigma(p_T^{\text{cut}})\) [pb]

\[ E_{\text{cm}} = 7 \text{ TeV} \quad m_H = 165 \text{ GeV} \]

<table>
<thead>
<tr>
<th>(\Delta \sigma_{\text{total}}/\sigma_{\text{total}})</th>
<th>(\Delta \sigma_0/\sigma_0)</th>
<th>(\Delta \sigma_{1}/\sigma_{1})</th>
<th>(\Delta \sigma_{\geq 2}/\sigma_{\geq 2})</th>
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</thead>
<tbody>
<tr>
<td>naive</td>
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<td>5%</td>
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<tr>
<td>new</td>
<td>10%</td>
<td>17%</td>
<td>29%</td>
</tr>
</tbody>
</table>

\[ p_T^{\text{cut}} = 30 \text{ GeV} \]

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