

your name \_\_\_\_\_

*Physics 321 In Class Exercise (NOT GRADED) - Friday, Oct. 24*

1. Consider a particle of mass  $m$  in an attractive potential,  $U(r) = -\alpha/r$ , with angular momentum  $L$  with just the right energy so that

$$A = m\alpha/L^2$$

where  $A$  comes from the expression

$$r = \frac{1}{(m\alpha/L^2) + A \cos \theta}.$$

The trajectory can then be rewritten as

$$r = \frac{2r_0}{1 + \cos \theta}, \quad r_0 = \frac{L^2}{2m\alpha}.$$

- (a) Show that for this case the total energy  $E$  approaches zero.  
(b) Write this trajectory in a more recognizable parabolic form,

$$x = x_0 - \frac{y^2}{R}.$$

I.e., express  $x_0$  and  $R$  in terms of  $r_0$ .

- (c) Explain how a particle with zero energy can have its trajectory not go through the origin.  
(d) What is the scattering angle for this trajectory?