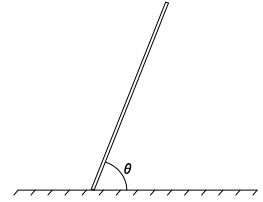


Physics 321 – Spring 2017

Homework #6, due at beginning of class Wednesday Feb 22.

1. [6 pts] A thin uniform stick of wood of length B and mass M is in the process of falling to the floor. It starts at $\theta = 90^\circ$ with $\dot{\theta}$ vanishingly small but negative so it falls to $\theta = 0$. Assume that the end on the floor does not slip, and ignore air resistance.



- (a) Write its kinetic energy as a function of B , M , and $\dot{\theta}$. (θ itself will not appear.)
 - (b) Write its potential energy as a function of B , M , g , θ .
 - (c) Use energy conservation ($\text{KE} + \text{PE} = \text{constant}$) to obtain a relation between $\dot{\theta}$ and θ . Evaluate the constant using the initial conditions at $t = 0$.
 - (d) Take the derivative of your energy conservation equation with respect to time to obtain $\ddot{\theta}$ as a function of θ .
 - (e) Find the horizontal component N_x of the force due to the floor as a function of B , M , g , θ . **Actually B cannot appear because only Mg has dimensions of force.**
 - (f) Find the vertical component N_y of the force due to the floor as a function of B , M , g , θ . **Again B cannot appear.**
 - (g) Write the stick's angular momentum about the point of contact with the floor.
 - (h) Write the torque on the stick due to gravity about the point of contact with the floor. **Don't worry about the overall sign of it.**
 - (i) Use the formula $\tau = dL/dt$ where τ is the torque and L is the angular momentum, to obtain an equation of motion for $\ddot{\theta}$ as a function of θ and check that it agrees with your previous result for that. **You will have to choose the sign correctly to match what you wrote for the torque.**
 - (j) What is the smallest coefficient of friction that will keep the stick from slipping **before it reaches an angle of 45°** ? (Hint: look at the ratio N_x/N_y .)
2. [4 pts] The potential energy of a particle is given by $U(x, y, z) = a \sin(bxy z^2)$ where a and b are constants.
- (a) Find the magnitude of the force at the point $x = y = z = 1$.
 - (b) Find the unit vector in the direction of the force at the point $x = y = z = 1$, assuming $a > 0$ and $b = \pi$.
3. [4 pts] A conservative force is acting in the two-dimensional plane (x, y) . The component of force in the x -direction is $F_x = ax^2y^3$ where a is a constant.
- (a) Find the most general form possible for the potential energy $U(x, y)$.
 - (b) Find the most general form possible for the y -component of the force $F_y(x, y)$.
4. [6 pts] Taylor problem 4.20