

As you come in today pull out a piece of paper and take 1 minute to respond to the following prompts:

Think about a time when you have struggled. How strongly would you agree/disagree with following statements?

1. I didn't give up easily when I felt frustrated.
2. When I felt frustrated I took a step back to make sure my approach made sense.
3. I tried multiple approaches until I found one that worked.
4. I tried new things even if I was uncertain what the outcome might be.
5. When I was struggling I felt comfortable asking someone for help.

- Failure is a routine part of science: computer programs will be buggy, equipment won't work, and experiments will yield weird results. Scientists are characterized by their ability to use these setbacks as opportunities to improve their work.
- As a budding scientist, you can prepare yourself for dealing with failure in the lab by working to develop a healthy attitude towards setbacks in the classroom. This can mean building skills to help you struggle through a difficult problem set or figure out how to move forward from a low grade.

A worked solution to Wednesday's scaling problem is in the lecture slides posted on LON-CAPA and on the course calendar

# Announcements

- Hands-On materials will be online in LON-CAPA before hands-on every week
- Use the LAs/TA in lecture – they're here to help!
- I moved some dates forward on the course calendar, Ch3 reading questions are due next Thursday. Homework stays the same.
- Help room opens next Tuesday! Hours are posted in LON-CAPA.
- If you've indicated you want to do an honors option meet down front at the end of class (so you can know who else is interested!)

# Foothold ideas: Measuring “where”

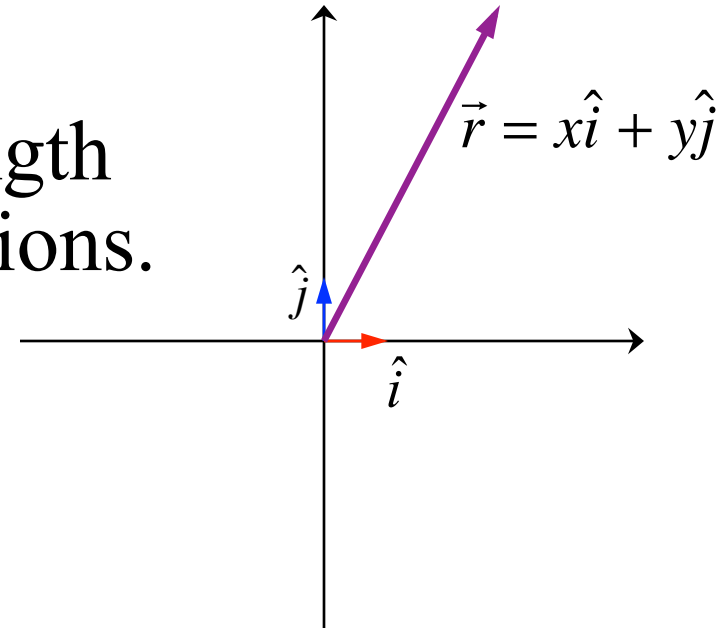


- In order to specify where something is we need a coordinate system. This includes:
  1. Picking an origin
  2. Picking perpendicular directions
  3. Choosing a measurement scale
- Each point in space is specified by three numbers:  $(x, y, z)$ , and a position vector— an arrow showing the displacement from the origin to that position.
- Vectors add like successive displacements or algebraically by  $\vec{A} = A_x \hat{i} + A_y \hat{j}$        $\vec{B} = B_x \hat{i} + B_y \hat{j}$

$$\vec{A} + \vec{B} = (A_x + B_x) \hat{i} + (A_y + B_y) \hat{j}$$

# Notation

- We specify the directions we are talking about by drawing two little arrows of unit length in two perpendicular directions.
- “ $x$ ” and “ $y$ ” are called the coordinates and can be positive or negative.
- Note that if  $x$  is negative, it means  $x\hat{i}$  is a vector pointing in the direction opposite to  $\hat{i}$



Which of the options below is the best match for the red vector shown?

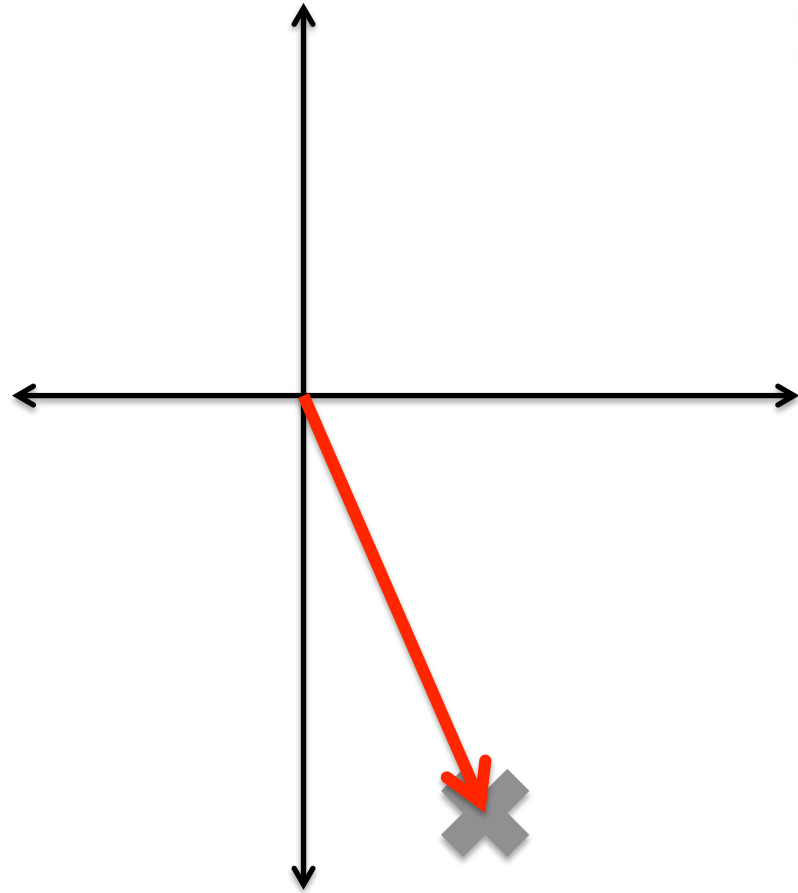


A.  $\begin{pmatrix} 1 \\ -2 \end{pmatrix}$

B.  $\begin{pmatrix} -1 \\ -2 \end{pmatrix}$

C.  $\begin{pmatrix} -1 \\ 2 \end{pmatrix}$

D.  $\begin{pmatrix} 1 \\ 2 \end{pmatrix}$



Which of the options below is the best match for the red vector shown?

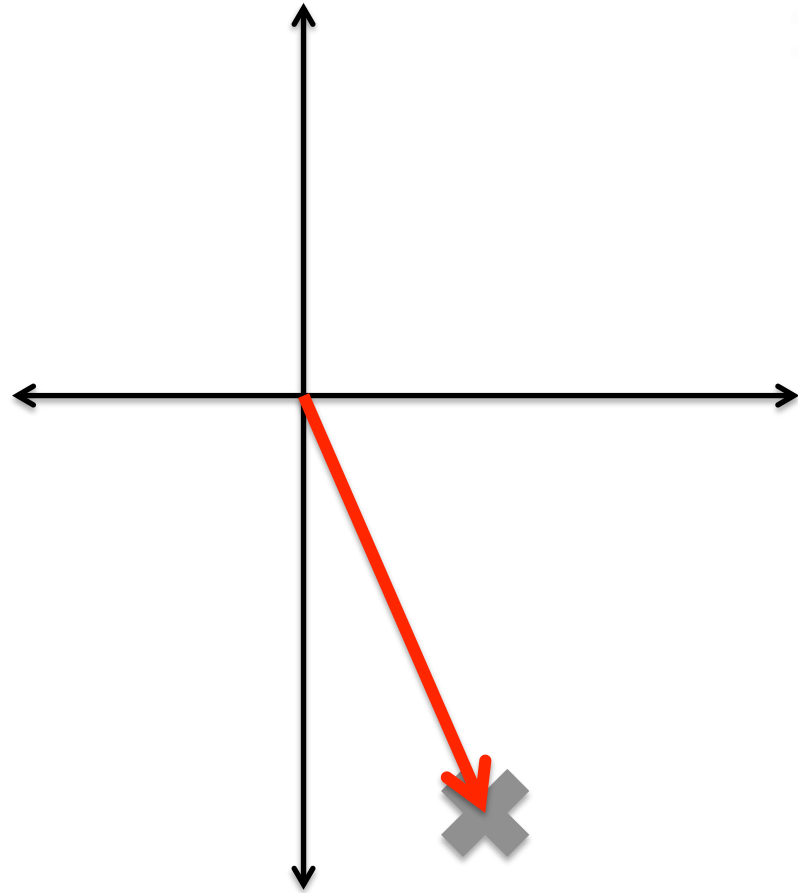


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The point X moves to a distance, 4 times away along the same path. How would you describe it's position now?

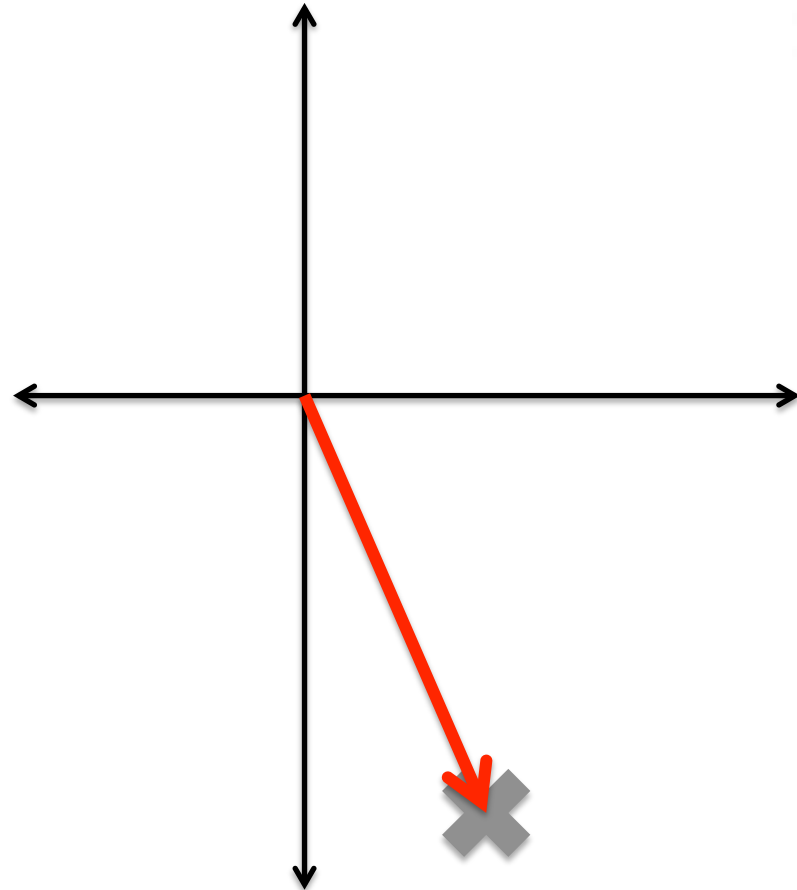
A.  $\begin{pmatrix} 4 \\ -8 \end{pmatrix}$

B.  $\begin{pmatrix} 4 \\ -2 \end{pmatrix}$

C. -4

D. 12

E. None of these





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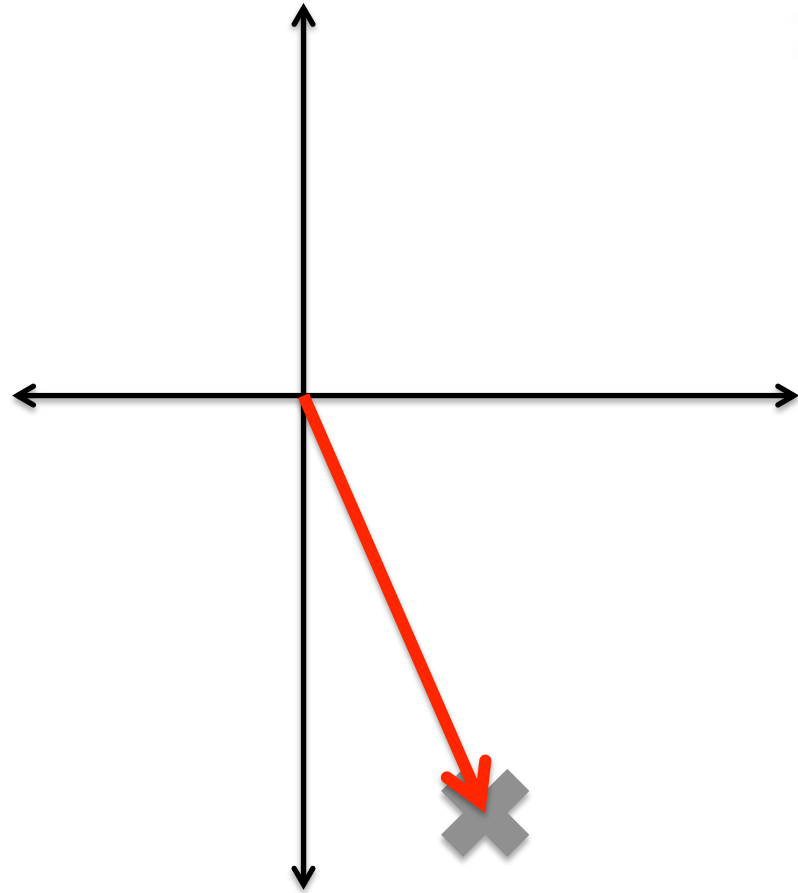
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You have a vector  $\vec{a} = (1, 2, 1)$ .  
What is  $4\vec{a} = ?$

- A. 16
- B. (4, 2, 1)
- C. (4, 8, 4)
- D. 7
- E. None of these



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# The dot product and cross product – What do they really mean?

Nothing really,  
they are a  
mathematical tool  
for modeling the  
world



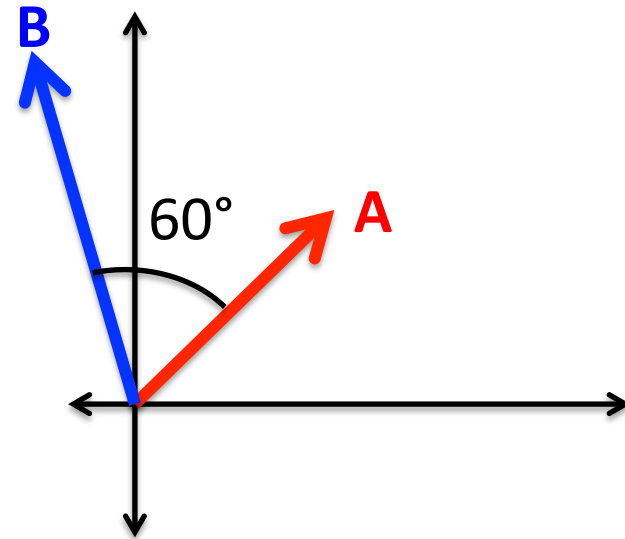
# The dot product and cross product – What do they really mean?

- Dot product: growth in a direction
  - Let's take the x-axis and the y-axis to mean really different things like “bananas” and “oranges”
  - Suppose  $(3,0)$  means “triple your bananas, destroy your oranges)
  - Suppose  $(0,4)$  means “destroy your bananas, quadruple your oranges”
  - So  $(3,0) \cdot (0,4)$  would say to “triple your banana growth, quadruple your orange growth”, but there was no bananas or oranges originally, so it's really say, “destroy all your fruits

Given two vectors  $A$  and  $B$  (shown in the picture), whose directions are separated by 60 degrees. Vector  $A$  has length 3, and vector  $B$  has length 4. What is  $\vec{A} \cdot \vec{B}$  ?

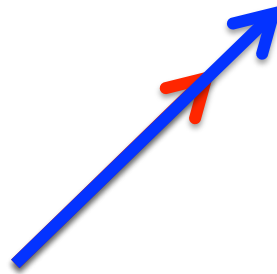


- A. .5
- B. 2
- C. 4
- D. 12
- E. None of these

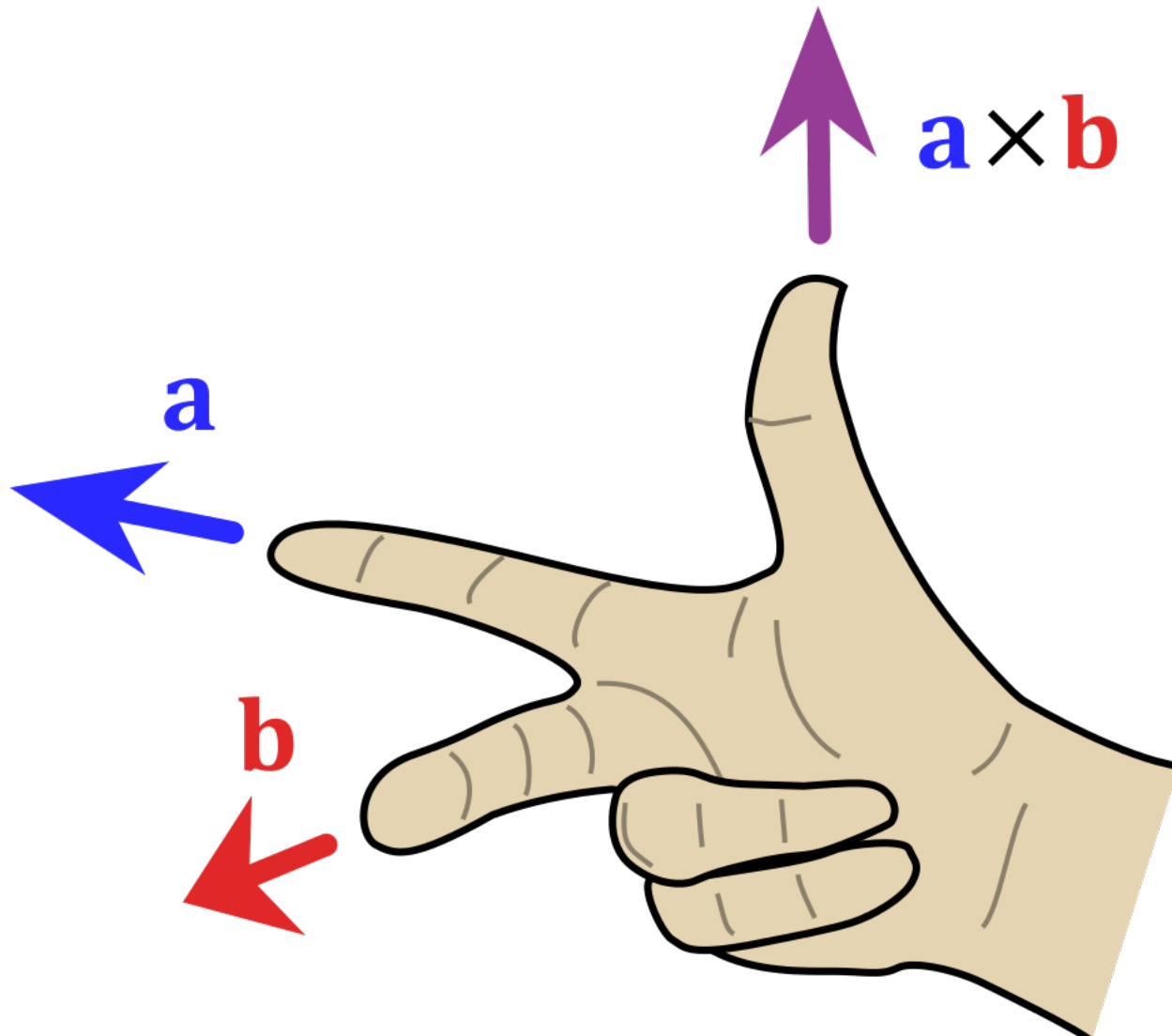


# The dot product and cross product – What do they really mean?

- Cross product: area created between two vectors
- Two vectors aligned?
  - 0 area
- The order is important because you still get a vector.
  - How do you know what direction?



# Right hand rule!

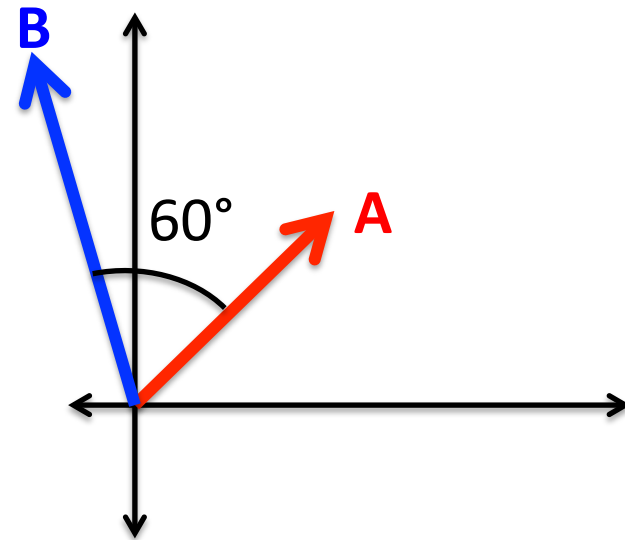




Given two vectors  $\vec{A}$  and  $\vec{B}$  (shown in the picture), whose directions are separated by 60 degrees. Vector  $\vec{A}$  has length 3, and vector  $\vec{B}$  has length 4. What is  $|\vec{A} \times \vec{B}|$ ?



- A. 10.4
- B. 12
- C. 8.5
- D. 6
- E. None of these



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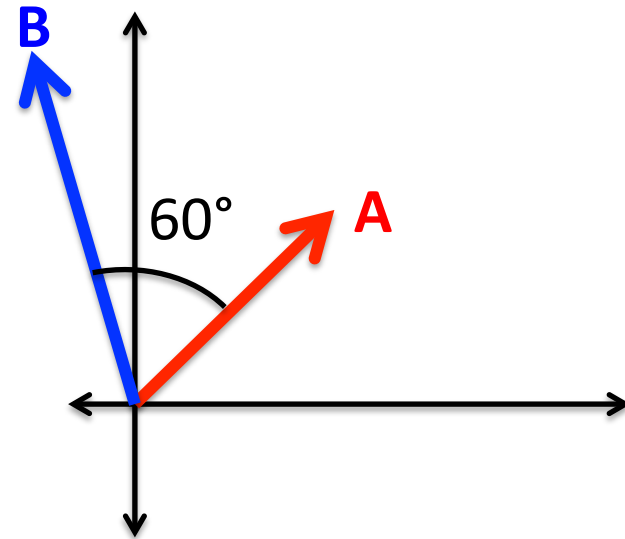
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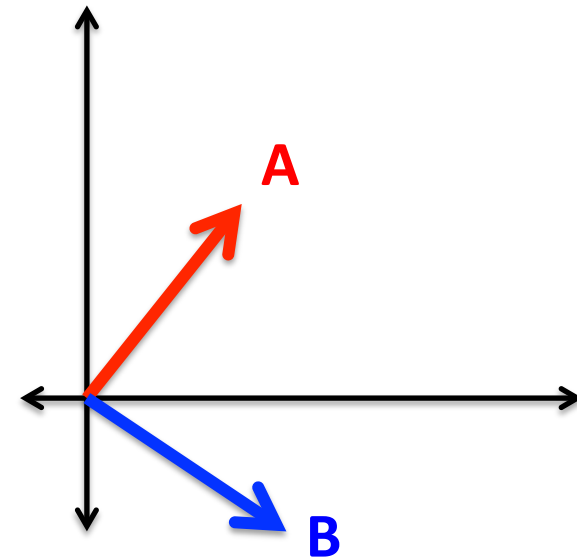
E. None of these



Now consider vectors  $\vec{A}$  and  $\vec{B}$ . What direction will  $\vec{A} \times \vec{B}$  point?



- A. Into the screen
- B. Out of the screen
- C. Up and to the left
- D. Down and to the left
- E. The cross product is zero



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