

Thermal expansion: linear



$$L = L_0 + \Delta L \quad \text{at } (T + \Delta T)$$

A horizontal blue rectangle representing a bar. Above it, the symbol L is written above the bar. To the right of the bar, the text "at $(T + \Delta T)$ " is written.

$$\begin{aligned} \Delta L &\sim \Delta T \\ \Delta L &\sim L_0 \end{aligned} \quad \Rightarrow \quad \Delta L = \alpha L_0 \Delta T$$
$$L = L_0 (1 + \alpha \Delta T)$$

α : coefficient of linear expansion

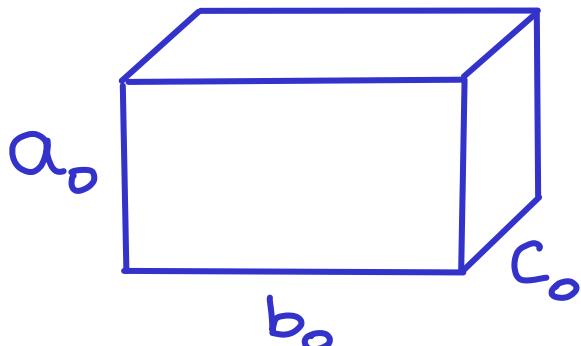
$$\alpha = \frac{\Delta L / L_0}{\Delta T} \quad [\alpha] = \frac{1}{K}, \text{ or } \frac{1}{^{\circ}\text{C}}$$

α : fractional or relative increase in length per unit change in temperature.

Examples :

Aluminium	: 2.39×10^{-5}	$1/\text{ }^{\circ}\text{C}$
Copper	: 1.62×10^{-5}	$1/\text{ }^{\circ}\text{C}$
Steel	: 1.17×10^{-5}	$1/\text{ }^{\circ}\text{C}$
Invar	: 0.12×10^{-5}	$1/\text{ }^{\circ}\text{C}$

Thermal expansion : volumetric



$$V_0 = a_0 b_0 c_0 \text{ at } T$$

$$a = a_0 (1 + \alpha \Delta T)$$

$$b = b_0 (1 + \alpha \Delta T)$$

$$c = c_0 (1 + \alpha \Delta T)$$

$$V = abc = a_0 b_0 c_0 (1 + \alpha \Delta T)^3 =$$

$$= V_0 (1 + 3\alpha \Delta T + \underline{3(\alpha \Delta T)^2} + \underline{(\alpha \Delta T)^3})$$

these two terms
are very small

$$V \approx V_0 (1 + \underline{3\alpha} \Delta T) \\ = \beta$$

$$V = V_0 (1 + \beta \Delta T) \quad \Delta V = \beta V_0 \Delta T$$

$$\beta = \frac{\Delta V / V_0}{\Delta T} \quad [\beta] = \frac{1}{K}, \text{ or } \frac{1}{^{\circ}C}$$

β = coefficient of volume expansion

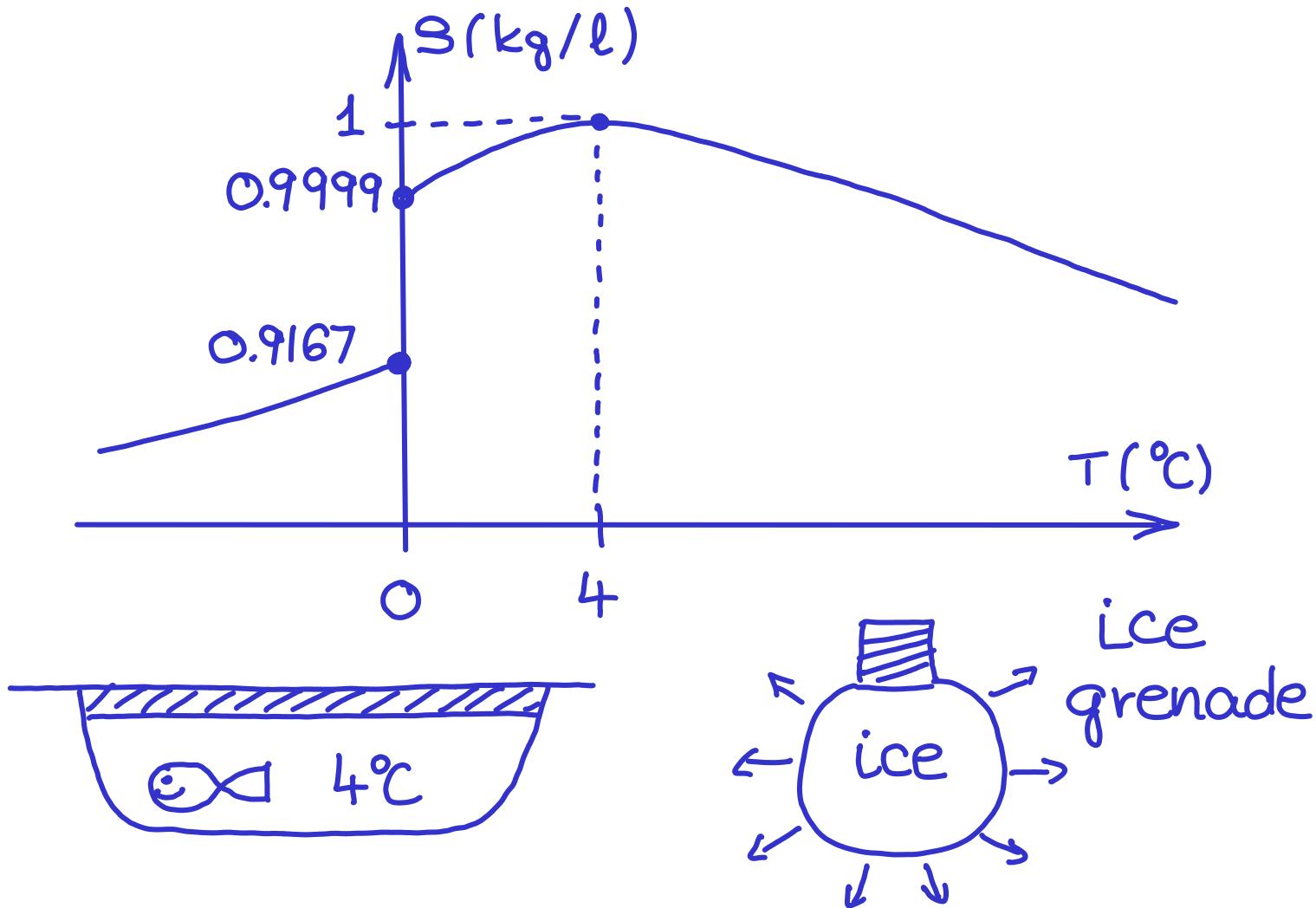
Examples :

petroleum : 9.6×10^{-4} $1/{}^{\circ}C$

water : 2.0×10^{-4} $1/{}^{\circ}C$

Warning : water (and ice) is very unusual.

The very unusual behavior of water

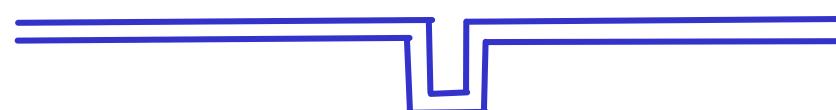


Heat expansion tricks:

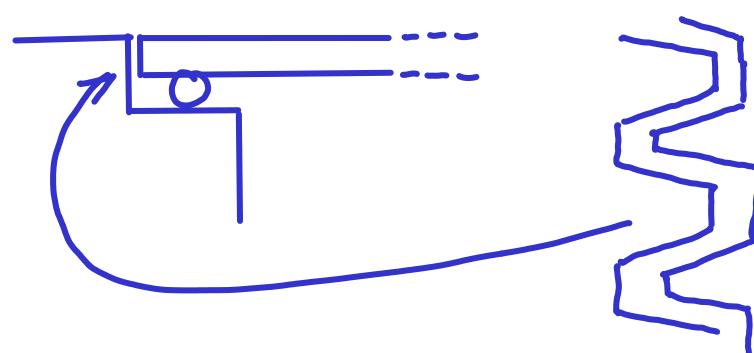
power
lines :



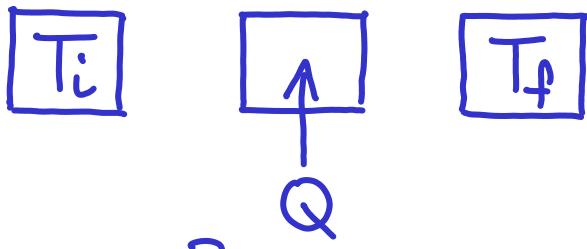
pipes :



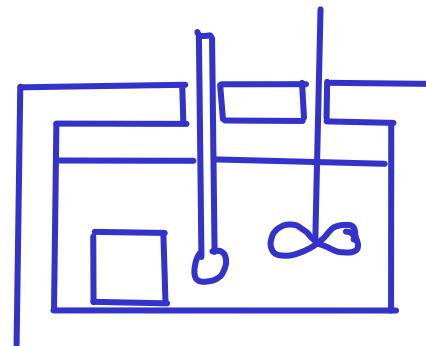
bridges:



Heat and mechanical work



$$Q \xleftarrow{?} \Delta T = (T_f - T_i)$$



calorimeter

Definition: 1 calorie is the amount of heat which raises the temperature of 1 g water by 1°C.

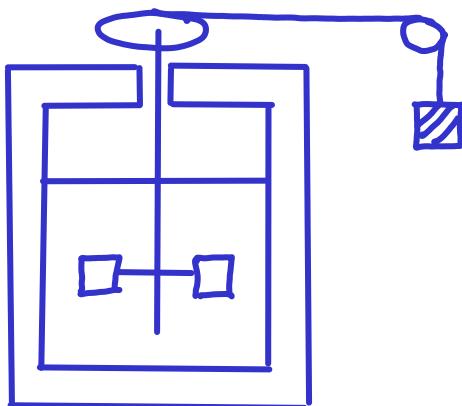
(Warning: 1 Cal = 1000 cal = 1 kcal.

Reminder: 1g is the mass of 1 cm³ water at 4°C temperature.)

Question: what is the relation between heat Q and mechanical work $W = Fd$?

James Prescott Joule (1818-1899):

1843 : 1 cal = 4.186 J



Heat capacity, specific heat

$$\begin{array}{c} T_i \\ \uparrow \\ Q \end{array}$$

$$T_f$$

$$Q = C \cdot \Delta T = C \cdot (T_f - T_i)$$

$$C = \frac{Q}{\Delta T} \quad [C] = \text{J/K}$$

C : heat capacity : amount of heat needed to raise the temperature of the object by 1K. (The object can be complex or composite.)

Homogeneous objects : $Q = cm \Delta T$

$$C = \frac{Q}{m \Delta T} = \frac{C}{m} \quad [C] = \frac{\text{J}}{\text{kg K}}$$

C : specific heat : amount of heat needed to raise the temperature of a unit mass of material.

$$\text{water} : 1 \frac{\text{cal}}{\text{g°C}} = 4186.8 \frac{\text{J}}{\text{kg K}}$$

$$\text{Al} : 0.215 \frac{\text{cal}}{\text{g°C}} = 900 \frac{\text{J}}{\text{kg K}}$$

$$\text{Cu} : 0.0923 \frac{\text{cal}}{\text{g°C}} = 386 \frac{\text{J}}{\text{kg K}}$$

$$\text{Molar heat} = C_m = \frac{C}{n}$$