

# Doppler effect

## Classical Doppler effect:

$$f = f_0 \frac{c \pm v_o}{c \mp v_s}$$

c : speed of sound  
(330-340 m/s)

$v_o$  : observer speed

$v_s$  : source speed

$f_0$  : emitted frequency

f : observed frequency

Air is the carrier medium of sound.  
The source and the observer move  
in this carrier medium.

## Relativistic Doppler effect:

$$\text{up: } f_{\uparrow} = f_0 \sqrt{\frac{c + v}{c - v}} = f_0 \sqrt{\frac{1 + \beta}{1 - \beta}} \quad \left. \begin{array}{l} \text{blue shift} \\ (\beta = v/c) \end{array} \right\}$$

$$\text{down: } f_{\downarrow} = f_0 \sqrt{\frac{c - v}{c + v}} = f_0 \sqrt{\frac{1 - \beta}{1 + \beta}} \quad \left. \begin{array}{l} \text{red shift} \end{array} \right\}$$

c : speed of light ( $c = 3 \cdot 10^8 \text{ m/s}$ )

v : speed of the source and the observer  
with respect to each other.

There is NO carrier medium!

## Doppler effect 2.

Longitudinal Doppler effect:

$f_0$

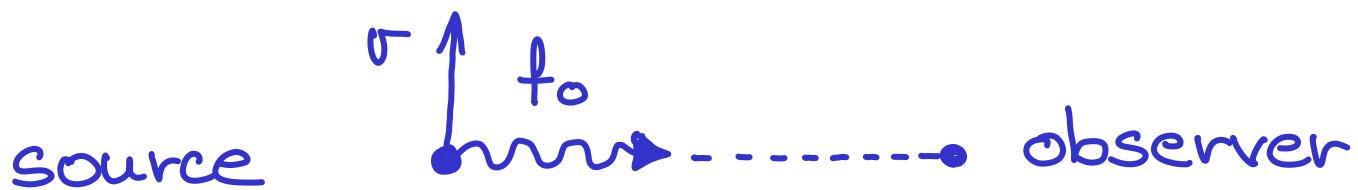
Source -----  $\bullet$  observer  
 $v \leftarrow \rightarrow v$

$f_{\uparrow} = f_0 \cdot \sqrt{\frac{1+\beta}{1-\beta}}$  or  $f_{\downarrow} = f_0 \sqrt{\frac{1-\beta}{1+\beta}}$

blue shift red shift

$$c = \lambda f \Rightarrow \lambda = \frac{c}{f}$$

Transverse Doppler effect



$$f = \frac{f_0}{\gamma} = \sqrt{1-\beta^2} \cdot f_0$$

The source's clock is time dilated,  
the light is redshifted.

The transverse Doppler effect is a  
pure relativistic effect!